

## Class 21: Review

### Exam 2

Exam 2 will be in class on Thursday, 9 Nov. Make sure to go over the notes about the exam posted in Class 20.

### Main Topics for Review

Today we review the topics that we learned after Exam 1 with the exception of number theory (which will not be included in Exam 2).

- State Machines and how to argue about correctness of programs.
- Recursive Definitions and how to prove statements about them using structural induction.
- Infinite Sets and Cardinalities, and how to show sets are finite, infinite, countable, or uncountable.

### State Machines

$M = (S, G \subset S \times S, q_0 \in S)$  defines a state machine.

$P$  is a *preserved invariant* if:

$$\forall q \in S. (P(q) \wedge (q \rightarrow r) \in G) \implies P(r)$$

**Invariant Principle:** If  $P$  is a *preserved invariant* and  $P(q_0)$  is true, then property  $P$  is true for all **reachable states**.