





Lecture 5.3 - Supervised Learning Classification - Decision Regions

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(Bishop 1.5, 4.1)





Classification through decision regions

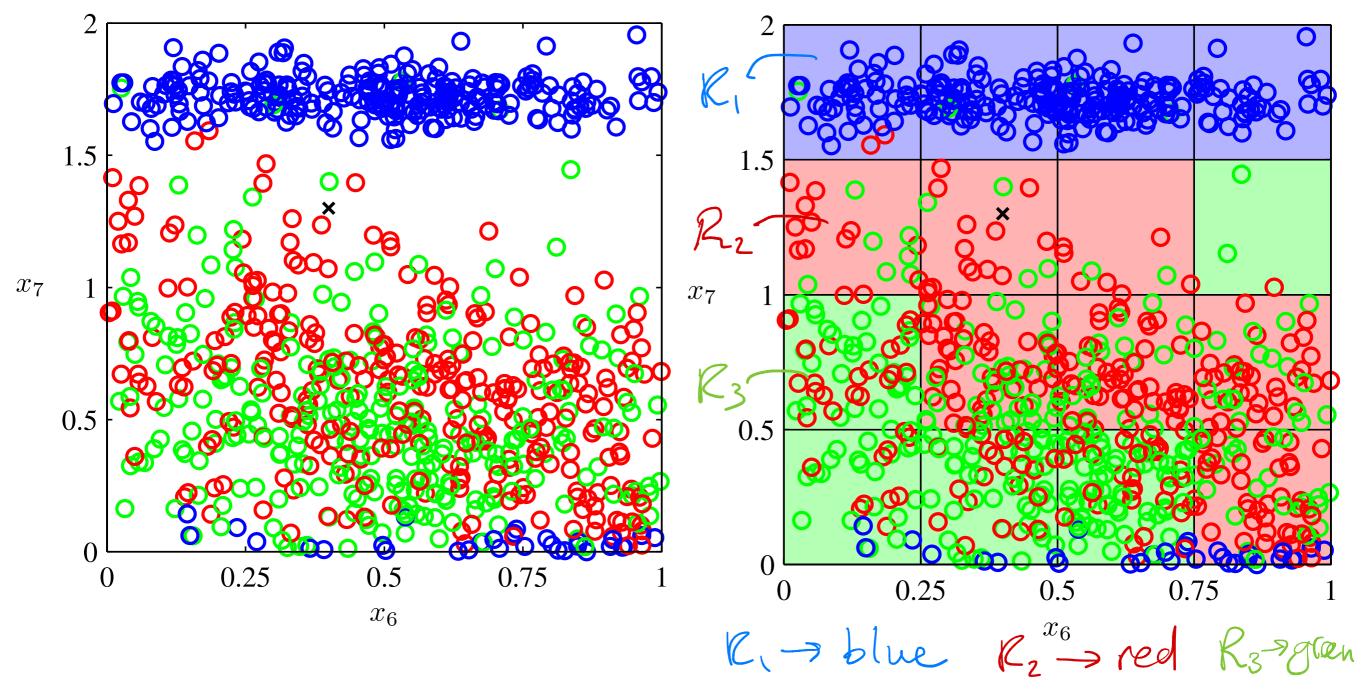
- Input: $\mathbf{x} = (x_1, ..., x_D)^T$
- Target: $t \in \{C_1, C_2, -\infty, C_k\}$
 - 2-class targets: $t = C_1$, $t = C_2$ t = 0, t = 1
 - Multi-class targets e.g. K=5 , $t=C_3 \Leftrightarrow \begin{pmatrix} 0 \\ 0 \\ 1 \\ 0 \end{pmatrix}$ rategy:

Strategy:

- Divide input space \mathbb{R}^D into K decision regions. \mathcal{R}_{k}
- Assign each decision region to a class
- Boundaries of decision regions are called decision boundaries/surfaces.

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Classification through Decision Regions



Figures: 3 class problem with decision boundaries. (Bishop 1.19 & 1.20)

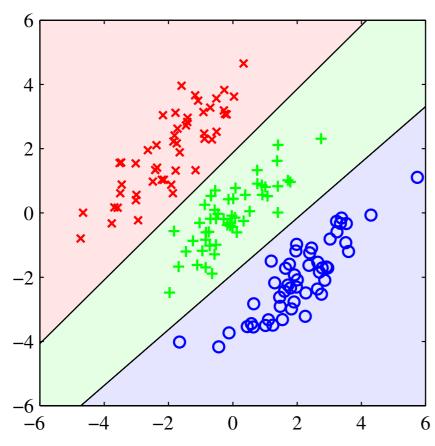
K=3

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Linear Classification

- Linear Classification: consider only *linear* decision boundaries
- For D dimensional input space: 26×10^{10} decision surface is a 10-1 dimensional hyperplane

Datasets whose classes can be separated *exactly* by linear decision surfaces are called



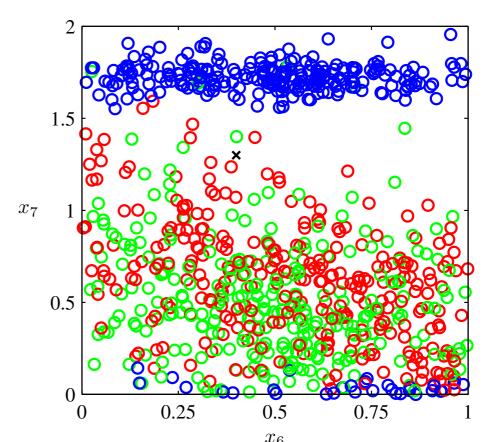


Figure: Linearly separable dataset (Bishop 4.5)

Figure: Not linearly separable dataset (Bishop 1.19)

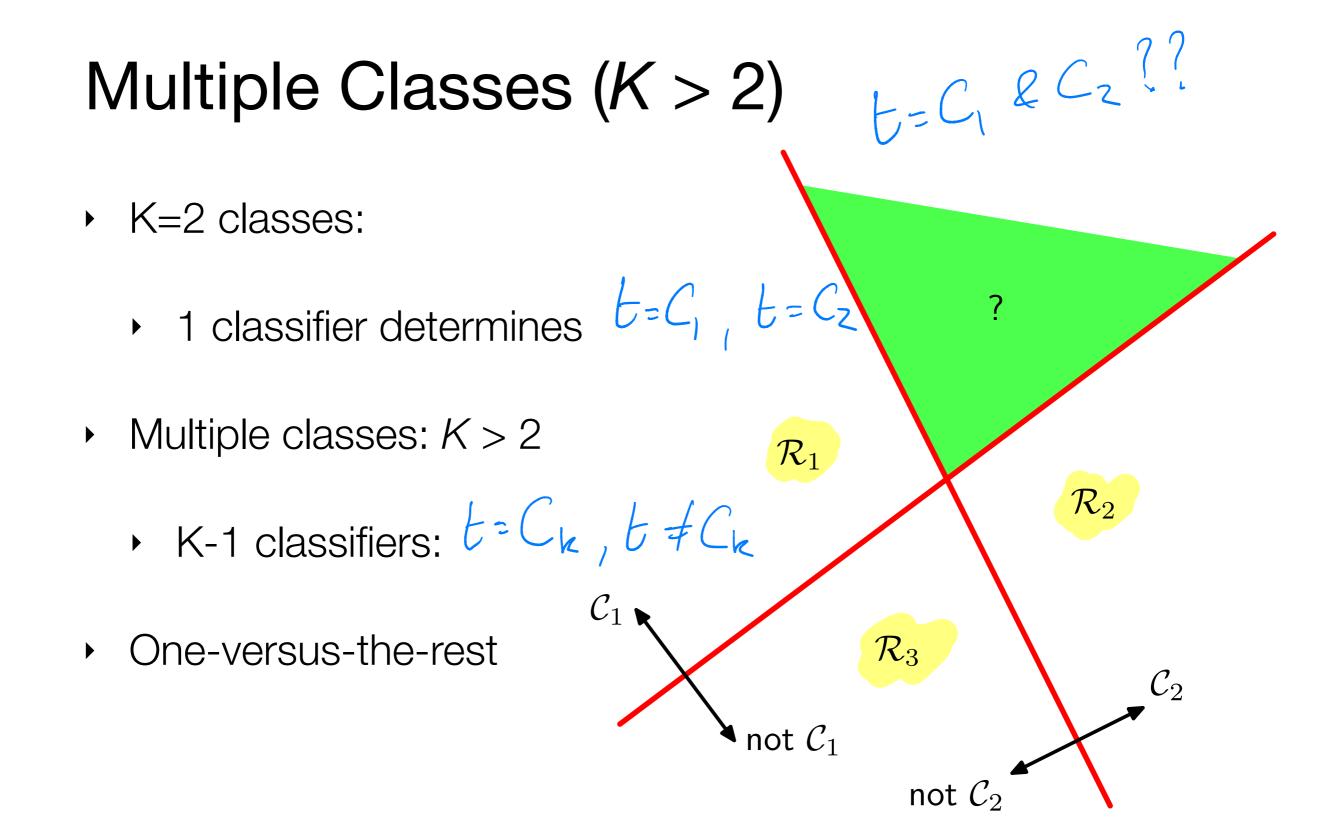


Figure: one-versus-the-rest classifiers (Bishop 4.2)

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Multiple Classes (K > 2)

• K(K-1)/2 classifiers: $\psi_{ij}(x) \rightarrow t = C_i$ or $t = C_j$

 Points are classified according to majority vote of classifiers

one-versus-one

 \mathcal{R}_1 \mathcal{R}_3 \mathcal{R}_3 \mathcal{C}_3 ass classifier! \mathcal{C}_2

Solution: Make one K-class classifier! (See later)

Figure: one-versus-one classifiers (Bishop 4.2)

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