

WIRELESS CHANNEL CHARACTERIZATION

① Wireless CHANNEL Model

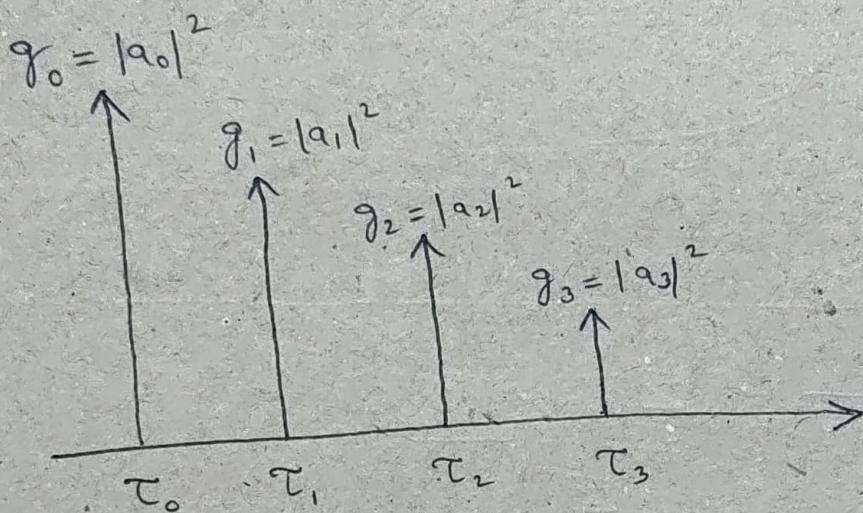
$$h = \sum_{i=0}^{L-1} a_i \delta(t - \tau_i)$$

where,

$L \rightarrow$ NO. of Multipath components

$a_i \rightarrow$ Attenuation of the i^{th} MP component

$\tau_i \rightarrow$ Delay of the i^{th} MP component



$g_i \rightarrow$ Gain of the i^{th} MP component

\rightarrow How many MP components ? 4

\rightarrow What is the LEAST DELAY ?

Earliest arriving component τ_0

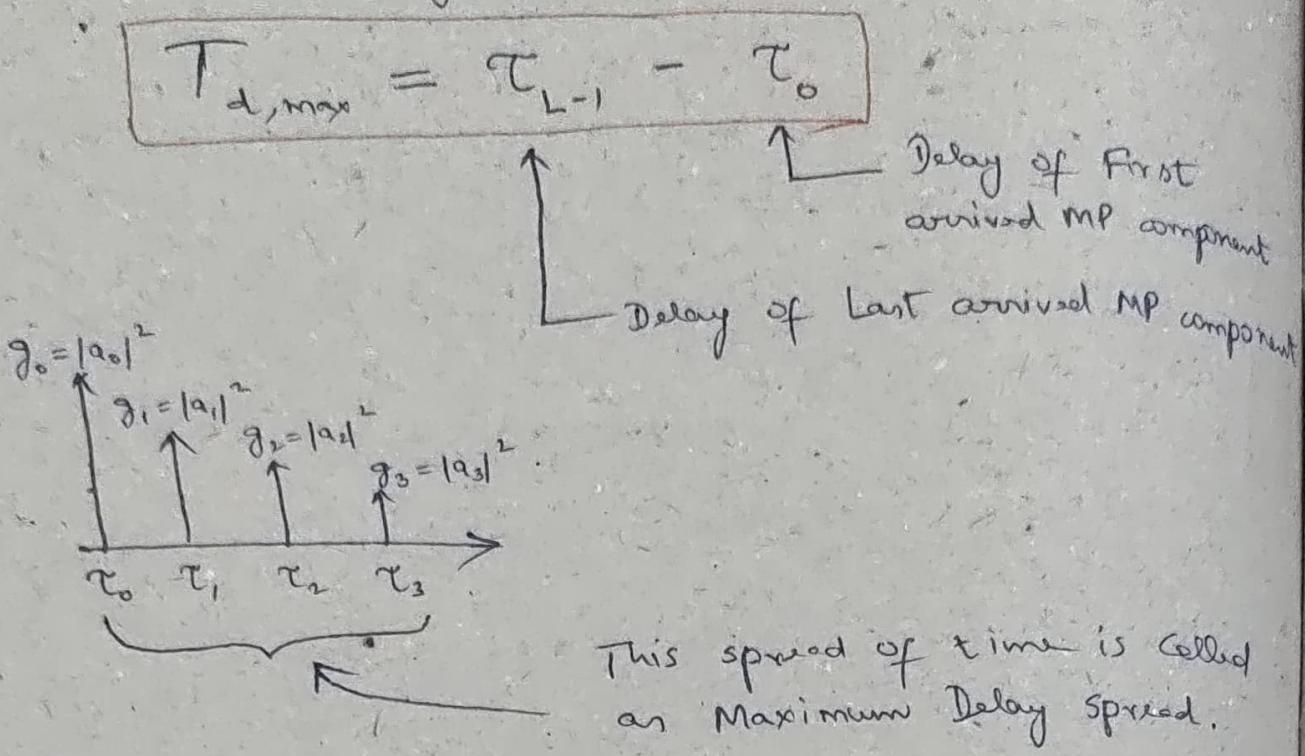
\rightarrow What is the MAXIMUM DELAY ?

Last arrived component τ_3

The MP components are arriving over a SPREAD OF TIME. Or in other words, the delays are SPREAD OVER TIME. This is termed as DELAY SPREAD.

• How to characterize the DELAY SPREAD ?

(i) Maximum Delay Spread



(ii) Root Mean Square (Rms) delay Spread

$$\text{Let } \bar{\tau} = \frac{\sum_i g_i \tau_i}{\sum_i g_i}$$

where $\bar{\tau}$ = Mean / Average of delays

$\bar{\tau}$ = Weighted average of delays

$$T_{d,rms} = \sqrt{\frac{\sum_i g_i (\tau_i - \bar{\tau})^2}{\sum_i g_i}}$$

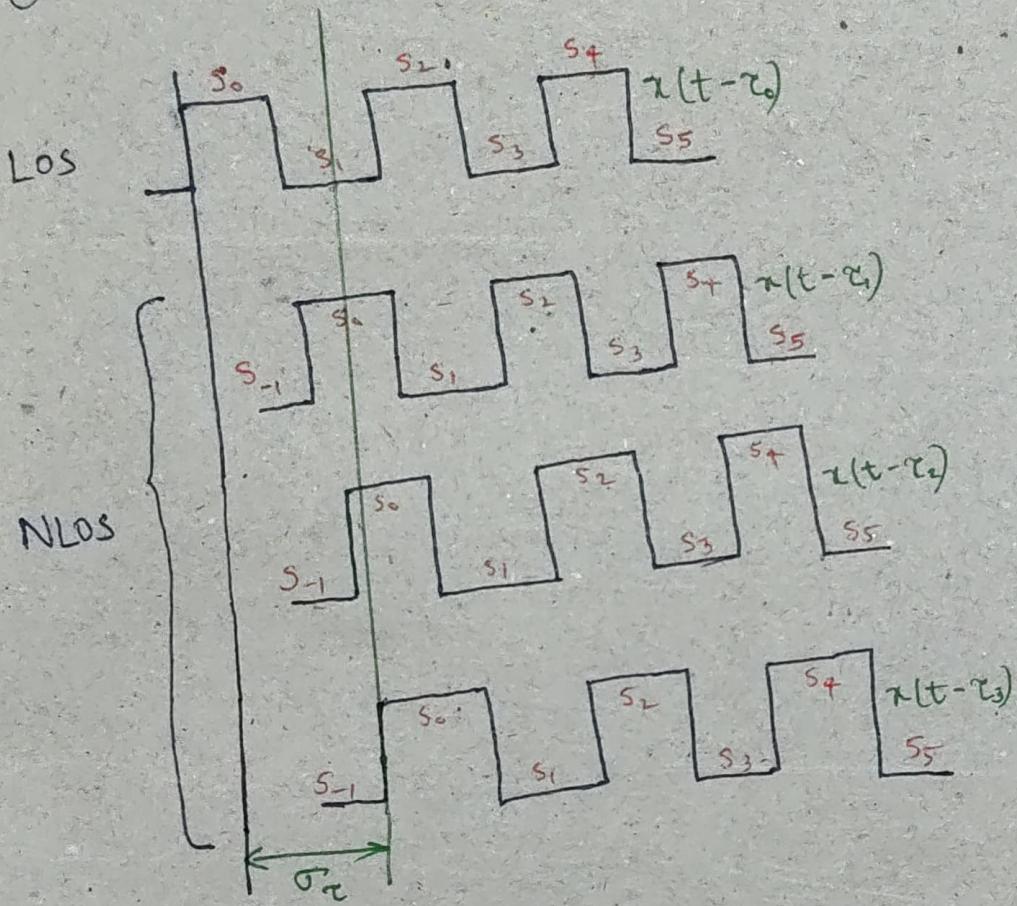
where, $(\tau_i - \bar{\tau})^2$ → Square of the Weighted deviation

① What is the typical delay / delay spread in wireless channel?

$$\approx \frac{\text{Order of distance in the wireless channel}}{\text{Velocity of Em wave}} = \frac{1 \text{ km}}{3 \times 10^8 \text{ m/s}} \approx 3.3 \mu\text{s.}$$

Typical delay spread $\approx 2-3 \mu\text{s.}$

② What is the IMPACT of delay spread?



$s_{-1}, s_0, s_1, s_2, s_3, s_4, s_5 \rightarrow \text{SYMBOLS}$

At receiver, different symbols Superpose / Adds up / gets aligned and interfere with each other.

Such large delay spread leads to Inter-Symbol Interference (ISI).

○ When does ISI occur?

Let $T_d \rightarrow$ Delay Spread

$T_s \rightarrow$ Symbol Time

* ISI occurs when $T_d \geq \frac{1}{2} T_s$

* In contrast, NO ISI when $T_d < \frac{1}{2} T_s$

Typically, Delay spread, $T_d = 2 - 3 \mu s$.

Let us Set $T_d = 2 \mu s$.

$$T_d \geq \frac{1}{2} T_s \Rightarrow T_s \leq 2 T_d$$

$$\Rightarrow T_s \leq 4 \mu s$$

Therefore, we can say ISI occurs when $T_s \leq 4 \mu s$.

○ No-ISI channel Model.

$$y(k) = h \underbrace{x(k)}_{\text{Current Symbol}} + n(k)$$

↓
Single Channel coefficient

$y(k)$ depends only on current symbol

○ ISI channel Model.

$$y(k) = h(0)x(k) + h(1)x(k-1) + \dots + h(L-1)x(k-(L-1)) + n(k)$$

↑
L channel
Taps
Current
Symbol
← Previous
Symbol

$$= h * x + n$$

↑
Linear convolution

$y(k)$ depends on the current symbol as well as the previous symbols.

① Coherence Bandwidth (B_c).

We have, ISI occurs when $T_s \leq 4\mu s = 2T_d$

From Fig, we have,

$$\text{Symbol Time, } T_s = \frac{1}{2 \times \frac{B}{2}} = \frac{1}{B}$$

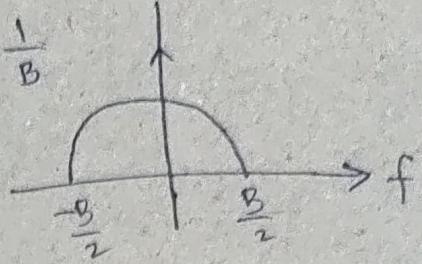


Fig. Single Carrier

$$\Rightarrow \frac{1}{B} \leq 4\mu s = 2T_d$$

$$\Rightarrow B \geq \frac{1}{2T_d} = \frac{1}{4\mu s} = 250 \text{ Hz} = B_c.$$

\Rightarrow ISI occurs if $B \geq 250 \text{ Hz}$.

This is termed as Coherence Bandwidth of Channel.

ISI occurs if

$$\left. \begin{array}{l} T_d \geq \frac{1}{2} T_s \\ B \geq B_c = \frac{1}{2T_d} \end{array} \right\} \text{Equivalent Conditions.}$$

One can define

$$B_c \approx \frac{1}{2T_d}$$

$$\Rightarrow B_c \propto \frac{1}{T_d}$$

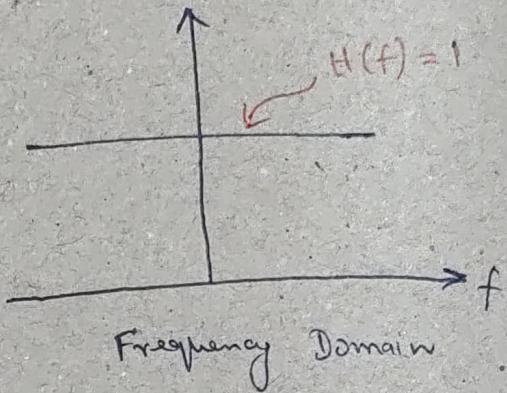
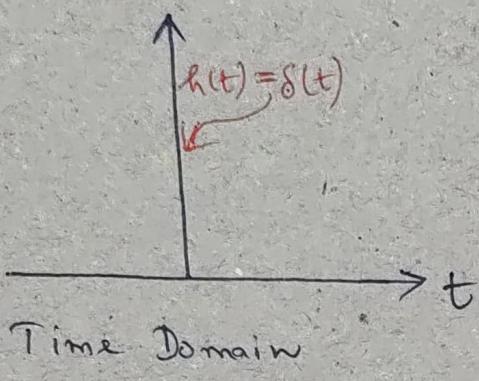
(ii) Coherence Bandwidth is inversely proportional to Delay spread.

As Delay spread increases, Coherence Bandwidth decreases.

CASE 1 : Delay spread $\overline{T_d} = 0$

$$\Rightarrow h(t) = \delta(t) \leftarrow \text{IMPULSE IN TIME DOMAIN}$$

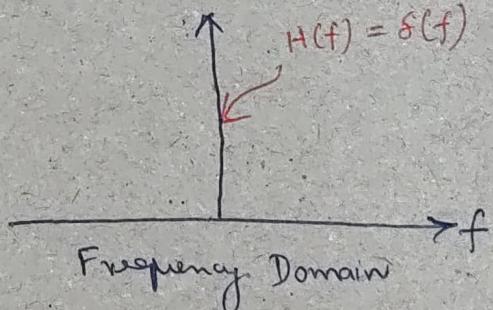
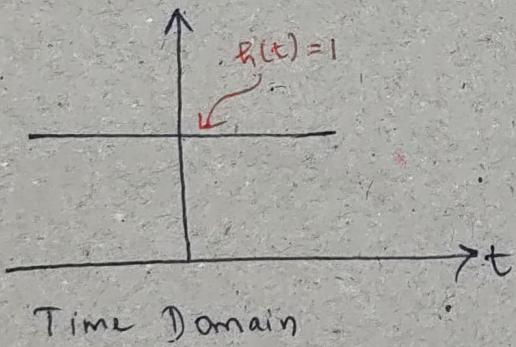
Fourier Transform $|H(f)| = 1$

$$\Rightarrow \text{BW} = B_c = \infty$$


CASE 2 : Delay spread $\overline{T_d} = \infty$

$$\Rightarrow h(t) = 1$$

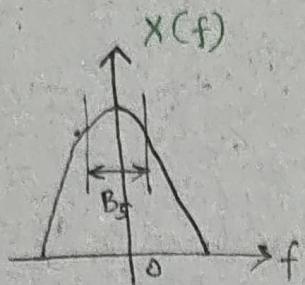
Fourier Transform $|H(f)| = \delta(f) \leftarrow \text{IMPULSE IN FREQUENCY DOMAIN}$

$$\Rightarrow \text{BW} = B_c = 0$$


FREQUENCY DOMAIN

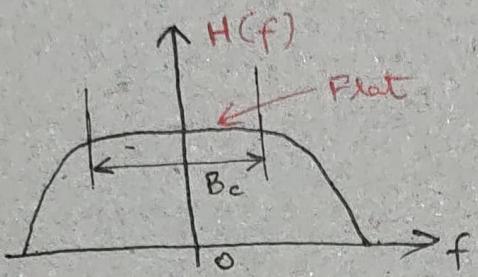
INTERPRETATION of B_c

(i)

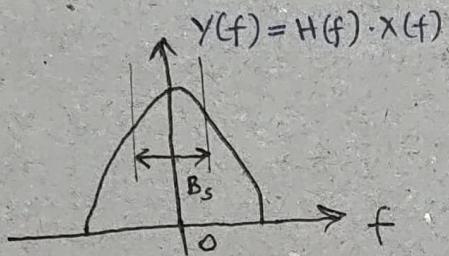


Input signal spectrum

$B_s \rightarrow$ Signal Bandwidth
 $B_c \rightarrow$ Coherence Bandwidth



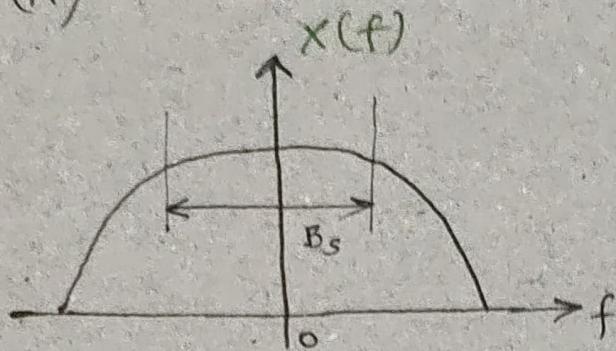
Wireless Channel Response



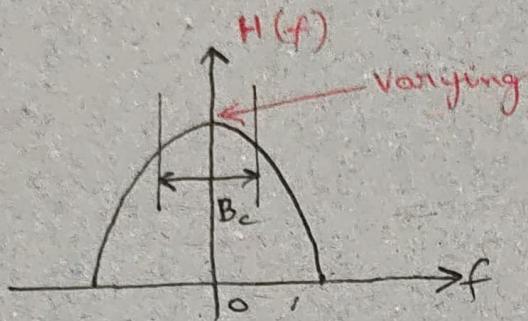
Undistorted Received Signal Spectrum.

- ① When $B_s < B_c$, Output spectrum is UNDISTORTED.
- ② Channel response is FLAT over signal bandwidth.
Such a channel is termed as FLAT FADING.
which implies NO ISI.

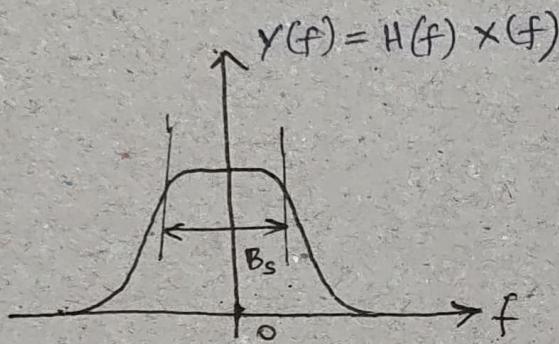
(ii)



Input Signal Spectrum



Wireless Channel Response



Distorted Received Signal Spectrum.

- ① When $B_s \geq B_c$, Output spectrum is DISTORTED.
- ② Channel response is VARYING Over signal bandwidth.
Such a channel is termed as FREQ. SELECTIVE FADING.
which implies ISI.

SUMMARY...

FLAT FADING

$$T_d < \frac{1}{2} T_s$$

NO ISI

$$B_s < B_c$$

Output spectrum is UNDISTORTED

Output depends only on current input symbol

$$y(z) = h_n(z) + n(z)$$

FREQUENCY SELECTIVE FADING

$$T_d \geq \frac{1}{2} T_s$$

ISI occurs

$$B_s \geq B_c$$

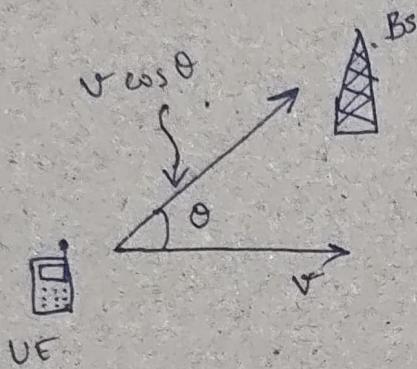
Output spectrum is DISTORTED

Output depends on current input symbol as well as previous input symbols

$$\begin{aligned} y(z) = & h(0) \pi(z) \\ & + h(1) \pi(z-1) \\ & \vdots \\ & + \\ & h(L-1) \pi(z-(L-1)) \\ & + \\ & n(z) \end{aligned}$$

DOPPLER SHIFT

When the UE is moving towards / away from the BS, there is a change in the frequency, which is termed as the DOPPLER SHIFT.



$$f_D = \frac{v \cos \theta}{c} \times f_c$$

where,

When $\theta = 0^\circ$, f_D = Positive Maximum

$\theta \rightarrow$ Angle between Velocity & Line joining UE to BS

$\theta = 90^\circ$, $f_D = 0$

$v \rightarrow$ Velocity of UE

$\theta = 180^\circ$, f_D = Negative Maximum

$c \rightarrow$ Velocity of light

$f_c \rightarrow$ Carrier frequency.

EXAMPLE

Consider a vehicle moving at 60 Kmph. at an angle of $\theta = 30^\circ$ with carrier frequency of $f_c = 2 \text{ GHz}$. Compute the Doppler shift of the received signal.

$$f_D = \frac{v \cos \theta}{c} f_c$$

$$= \frac{60 \times \frac{5}{18} \times \cos 30^\circ}{3 \times 10^8} \times 2 \times 10^9$$

$$= 96.22 \text{ Hz}$$

IMPACT OF DOPPLER SHIFT ON CHANNEL

As the UE moving towards / away from the BS, the distance b/w them decreases / increases respectively. And the delay also decreases / increases respectively.

(i) Delay becomes function of time.

* Consider the path is.

The Time varying delay $\tau_i(t)$ is given by

$$\tau_i(t) = \frac{d_i - (v \cos \theta)t}{c}$$

where, $d_i \rightarrow$ Original distance

$(v \cos \theta)t \rightarrow$ New distance

The Time varying channel $h(t)$ is given by

$$h(t) = \sum_{i=0}^{L-1} a_i \delta(t - \tau_i(t))$$

$$= \sum_{i=0}^{L-1} a_i \delta\left(t - \frac{d_i - v \cos \theta t}{c}\right)$$

Because of Doppler, Channel is time-varying!

This is termed as TIME SELECTIVE CHANNEL.

Therefore, Doppler is leading to a
TIME SELECTIVE CHANNEL.

① How fast is channel varying?

Let T_c denote the time over which channel is constant. This is termed as the COHERENCE TIME. (T_c).

$$T_c = \frac{1}{4 f_D} \propto \frac{1}{f_D}$$

(i) Coherence Time is inversely proportional to Doppler shift.

From the previous example, we have $f_D = 96.22 \text{ Hz}$

$$\Rightarrow T_c = \frac{1}{4 \times 96.22 \text{ Hz}} = \underline{\underline{2.6 \text{ ms}}}$$

(ii) Channel is approximately constant for 2.6 ms.

INFERENCES.

- ① Higher the velocity, higher would be the Doppler shift, since $f_D \propto V$
- ② This implies
 - ③ Channel is changing FASTER.
 - ④ Channel is constant over a Very small period of time
 - ⑤ Coherence Time is SMALL!

○ Doppler Bandwidth (B_D)

$$\begin{aligned}B_D &= 2 f_D \\&= 2 \times 96.22 \text{ Hz} \\&= \underline{\underline{192.44 \text{ Hz}}}\end{aligned}$$

WKT,

$$\begin{aligned}T_c &= \frac{1}{4 f_D} \\&= \frac{1}{2 B_D} \propto \frac{1}{B_D}\end{aligned}$$

(ii) Coherence Time is inversely proportional
to Doppler Bandwidth.