

WORKSHEET-1 ANSWER KEYS

STATISTICS AND PROBABILITY

1. (B) 0.135

Solution: $P(6) = \text{No. of times 6 appeared} / \text{Total no. of outcomes} = 190 / (1402) = \mathbf{0.1355}$

2. (D) 0.53

Solution: $P(\text{Odd Numbers}) = \text{Sum of frequencies of odd numbers} / \text{total number of records}$
 $= (52+44+20+56+40) / 400 = \mathbf{0.53}$

3. (C) 0.745

Solution: $P(>9000) = \text{No. of tyres lasting more than 9000 miles} / \text{total no. of tyres}$
 $= (375+445) / 1100 = \mathbf{0.745}$

4. (B) 0.577

Solution: $P(4000-14000) = \text{No. of tyres lasting from 4000 to 14000 miles} / \text{total no. of tyres}$
 $= (260+375) / 1100 = \mathbf{0.577}$

5. (C) 0.6

Solution: $P_1(\text{no. is greater than 4}) = \text{No. of favorable outcomes} / \text{No. of total outcomes} = 5/10 = 1/2$
 $P_2(\text{no. is odd} \cap \text{no. is greater than 4}) = 3/10$
 $P(P_2|P_1) = (3/10) \div (5/10) = 3/5 = \mathbf{0.6}$

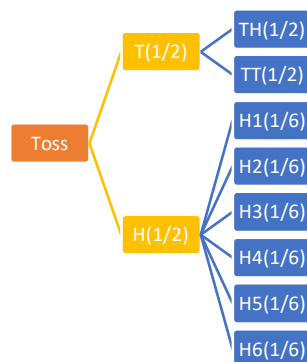
6. (A) 0.33

Solution: $P_1(\text{no. is less than 4}) = \text{No. of favorable outcomes} / \text{No. of total outcomes} = 3/8$
 $P_2(\text{even} \cap \text{less than 4}) = 1/8$
 $P(P_2|P_1) = (1/8) \div (3/8) = 1/3 = \mathbf{0.33}$

7. (C) 0.33

Solution: Let, **E** = Sum of nos. is 7, **F** = 6 appears on at least one die
 $P(E) = \text{No. of favorable outcomes} / \text{No. of total outcomes} = 6/36 = 1/6$
 $P(E \cap F) = 2/36 = 1/18$
 $P(F|E) = P(E \cap F) \div P(E) = (1/18) \div (1/6) = 1/3 = \mathbf{0.33}$

8. (B) 0.22



Let,

E = Event that die shows a number greater than 4

F = Event that there is at least one head

$P(E \cap F) = P(H5, H6) = P(H5) + P(H6) = (1/2) * (1/6) + (1/2) * (1/6) = 1/6$

$P(F) = P(H1, H2, H3, H4, H5, H6, TH) = 6 * (1/2 * 1/6) + (1/2 * 1/2) = 3/4$

$P(E|F) = P(E \cap F) / P(F) = (1/6) \div (3/4) = 2/9 = \mathbf{0.22}$

9. (A) 0.66

Total No. of ways of standing of three people = $3! = 6$

Total No. of ways of standing if Ross is at one end = $2! + 2! = 4$

$P(\text{Ross is at one of the ends}) = 4/6 = \mathbf{0.66}$

10. (A) 0.33

Sample space, **S** = {GG, GB, BG, BB}

E = Event that at least one of the two children is girl

F = Event that both the children are girls

$P(E) = P(GG, GB, BG) = 3/4$

$P(E \cap F) = P(GG) = 1/4$

$P(F|E) = P(E \cap F) / P(E) = (1/4) \div (3/4) = 1/3 = \mathbf{0.33}$

11. (C) 0.5

Sample space, **S** = {GG, GB, BG, BB}

E = Event that elder child is boy

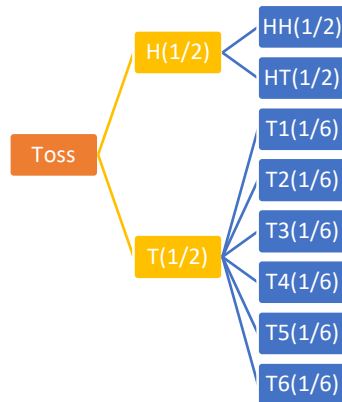
F = Event that both the children are boys

$$P(E) = P(BB, BG) = 2/4 = 1/2$$

$$P(E \cap F) = P(BB) = 1/4$$

$$P(F|E) = P(E \cap F)/P(E) = (1/4) \div (1/2) = 1/2 = \mathbf{0.5}$$

12. (A) 0.166



Sample Space, $S = \{HH, HT, T1, T2, T3, T4, T5, T6\}$

$$\begin{aligned} P(\text{getting a no. greater than 4 on die}) &= P(T5, T6) \\ &= P(T5) + P(T6) \\ &= (1/2 * 1/6) + (1/2 * 1/6) \\ &= 1/6 \\ &= \mathbf{0.166} \end{aligned}$$

13. (D) 0.25

Refer the figure and sample space of Q 12.

$$\begin{aligned} P(\text{getting an odd no. on the die}) &= P(T1, T3, T5) \\ &= P(T1) + P(T3) + P(T5) \\ &= (1/2 * 1/6) + (1/2 * 1/6) + (1/2 * 1/6) \\ &= 1/4 \\ &= \mathbf{0.25} \end{aligned}$$

14. (D) 0.06

Sample Space, $S = \{11, 12, 13, 14, 15, 16, 21, 22, 23, 24, 25, 26, 31, 32, 33, 34, 35, 36, 41, 42, 43, 44, 45, 46, 51, 52, 53, 54, 55, 56, 61, 62, 63, 64, 65, 66\}$

E = Event that two numbers on dice are different

F = Sum of nos. on two dice is less than 4

$$P(E) = 30/36 = 5/6$$

$$\begin{aligned} P(E \cap F) &= \text{No. of outcomes whose sum is less than 4 and nos. on two dice are different} / \text{Total no. of outcomes} \\ &= 2/36 = 1/18 \end{aligned}$$

$$P(F|E) = P(E \cap F) \div P(E) = (1/18) \div (5/6) = 1/15 = \mathbf{0.06}$$

15. (B) 2/3

Let $C1$ be the event that you choose a regular coin, and let $C2$ be the event that you choose the two-headed coin.

Note that $C1$ and $C2$ form a partition of the sample space. We already know that

$$P(H|C1) = 0.5$$

$$P(H|C2) = 1$$

Thus, we can use the law of total probability to write

$$P(H) = P(H|C1).P(C1) + P(H|C2).P(C2) = 1/2 * 2/3 + 1 * 1/3 = \mathbf{2/3}$$