

Uvin Abeysinghe – Database Systems – 789931 – Assignment 3

Question 1

- a) Page - oriented Nested L oops Join. Consider A as the outer relation.

$\text{Cost} = \text{NPages}(A) + \text{Npages}(A) * \text{Npages}(B)$
 $\text{Cost} = 10,000 + 10,000 * 1,000$
 $\text{Cost} = 10,010,000$

- b) Block - oriented Nested L oops Join. Consider A as the outer relation.

$\text{Cost} = \text{NPages}(A) + \text{ceil}(\text{NPages}(A)/(\text{BLOCK_SIZE}-2)) * \text{NPages}(B)$
 $\text{Cost} = 10,000 + \text{ceil}(10,000/(502-2)) * 1000$
 $\text{Cost} = 30,000$

- c) Sort-Merge Join

$\text{Cost} = \text{NPages}(A) + \text{NPages}(B) + 2 * \text{NPages}(A) * \text{ceil}(1 + \log \text{BLOCKSIZE} - 1 \text{ceil}(\text{NPages}(A)/\text{BLOCKSIZE})) + 2 * \text{NPages}(B) * \text{ceil}(1 + \log \text{BLOCKSIZE} - 1 \text{ceil}(\text{NPages}(B)/\text{BLOCKSIZE})) +$
 $\text{Cost} = 10,000 + 1,000 + 2 * 10,000 * \text{ceil}(1 + \log 501 \text{ceil}(10,000/502)) + 2 * 1,000 * \text{ceil}(1 + \log 501 \text{ceil}(1,000/502))$
 $\text{Cost} = 11000 + 4 * 10,000 + 4 * 1,000 = 55,000$

- d) Hash Join

$\text{Cost} = 3 * (\text{NPages}(A) + \text{NPages}(B))$
 $\text{Cost} = 3 * (10,000 + 1,000)$
 $\text{Cost} = 33,000$

- e) What would the lowest possible I/O cost be for joining A and B using any join algorithm and how much buffer space would be needed to achieve this cost??
Explain briefly

$\text{Cost} = \text{NPages}(B) + \text{ceil}(\text{NPages}(B)/(\text{BLOCK_SIZE}-2)) * \text{NPages}(A)$
 $\text{Cost} = 1,000 + \text{ceil}(1,000/1,002) * 10,000$
 $\text{Cost} = 11,000 \quad \text{Buffer size} = 1,002 \text{ pages}$

The lowest possible I/O costs given by the block oriented nested loop join with B (smallest relation) as the outer loop and all the pages of B in the buffer. However, having A in the buffer and in the outer loop would give the same cost but will need a larger buffer size.

Question 2

- a) Compute the estimated result size and the reduction factor (selectivity) of this query

$$RF(\text{title} = \text{"CEO"}) = 1 / (\text{Number of distinct values in column}) = 1/10$$

$$RF(\text{level} > 15) = (\text{Highest value} - 15) / (\text{Highest value} - \text{Lowest value}) = (20 - 15) / (20 - 0) = 5/20 = 1/4$$

$$\text{Result Size} = \text{NTuples}(R) * \text{product of RF} = 100,000 * 1/10 * 1/4 = 2,500$$

- b) Compute the estimated cost of the best plan assuming that a *clustered B+ tree* index on (*title*, *level*) is (the only index) available. Suppose there are 200 index pages, and the index uses Alternative 2. Discuss and calculate alternative plans.

$$\text{Cost} = (\text{NPages}(\text{INDEX}) + \text{NPages}(R)) * \text{product of RF}(\text{title}, \text{level})$$

$$\text{Cost} = (200 + 1,000) * 1/10 * 1/4 = 30$$

The only alternative left to do is use a heap scan (since no other indexes) on the relation, which will cost the number of pages in the relation, so the cost will be 1000 (since 1000 pages)

- c) Compute the estimated cost of the best plan assuming that an *unclustered B+ tree* index on (*level*) is (the only index) available. Suppose there are 200 index pages, and the index uses Alternative 2. Discuss and calculate alternative plans.

$$\text{Cost} = (\text{NPages}(\text{INDEX}) + \text{NTuples}(R)) * \text{product of RF}(\text{level})$$

$$\text{Cost} = (200 + 100,000) * 1/4 = 25,050$$

The only alternative left to do is use a heap scan (since no other indexes) on the relation, which will cost the number of pages in the relation, so the cost will be 1000 (since 1000 pages)

- d) Compute the estimated cost of the best plan assuming that an *unclustered Hash* index on (*title*) is (the only index) available. The index uses Alternative 2. Discuss and calculate alternative plans.

$$\text{Cost} = \text{NTuples}(R) * \text{product of RF}(\text{title}) * 2.2$$

$$\text{Cost} = 100,000 * 1/10 * 2.2 = 22,000$$

The only alternative left to do is use a heap scan (since no other indexes) on the relation, which will cost the number of pages in the relation, so the cost will be 1000 (since 1000 pages)

- e) Compute the estimated cost of the best plan assuming that an *unclustered Hash* index on (*level*) is (the only index)) available. The index uses Alternative 2. Discuss and calculate alternative plans.

Has to do a heap scan since hash index cannot be used for ranges

Cost = NTuples(R)

Cost = 1,000

The only way is use a heap scan (since no other indexes) on the relation, which will cost the number of pages in the relation, so the cost will be 1000 (since 1000 pages) so no alternatives.

Question 3

- a) Compute the estimated result size and the reduction factors (selectivity) of this query

E.did = D.did

$RF = 1 / (\text{MAX}(\text{Distinct values in E.did}, \text{Distinct values in D.did})) = 1/5,000$

D.did = F.did

$RF = 1 / (\text{MAX}(\text{Distinct values in D.did}, \text{Distinct values in F.did})) = 1/5,000$

E.sal >= 59,000

$RF(\text{level} > 59,000) = (\text{Highest value} - 59,000) / (\text{Highest value} - \text{Lowest value})$

$RF(\text{level} > 59,000) = (60,000 - 59,000) / (60,000 - 10,000) = 1/50$

E.hobby = 'yodeling'

$RF = 1 / \text{Distinct values in E.hobby} = 1/200$

Result Size = $50,000 * 5,000 * 5,000 * 1/5,000 * 1/5,000 * 1/50 * 1/200 = 5$

b)

1) Result Size of Dept + Finance = $5,000 * 5,000 * 1/5,000 = 5,000$ tuples = 50 Pages

Cost of joining Dept & Finance = $\text{NPages}(\text{Dept}) + \text{Npages}(\text{Dept}) * \text{Npages}(\text{Finance})$
 $= 50 + 50 * 50$
 $= 2550$

Cost of joining with Emp = $\text{Npages}(\text{Result}) * \text{Npages}(\text{Emp}) = 50 * 500 = 25,000$

Therefore total cost = $25,000 + 2550 = 27,550$

2) Result Size of Dept + Finance = $5,000 * 5,000 * 1/5,000 = 5,000$ tuples = 50 Pages

Cost of joining Dept & Finance = $(NPages(Dept) + Npages(Finance)) * 3$
 $= (50 + 50) * 3$
 $= 300$

Cost of joining with Emp = $Npages(Result) + Npages(Emp) + (4-1) * Npages(Result) + 4 * Npages(Emp)$

/*4-1 since its already read before*/

$= 50 + 500 + 3(50) + 4(500) = 4(50) + 5(500) = 2,700$

Therefore total cost = $2,700 + 300 = 3,000$

3) Result Size of Emp + Dept = $50,000 * 5,000 * 1/5,000 = 50,000$ tuples = 500 Pages

/*no need to sort Emp since its already sorted*/

Cost of joining Emp & Dept = $50 + 500 + 50 + 4 * 50 = 800$

Cost of joining with Finance = $Npages(Finance) + 2 * (Npages(Result) + Npages(Finance))$
 $= 50 + 2 * (500 + 50) = 1150$

Therefore total cost = $800 + 1,150 = 1,950$

4) Result Size of Emp + Dept = $50,000 * 5,000 * 1/5,000 = 50,000$ tuples = 500 Pages

Cost of joining Emp & Dept = $3 * (Npages(Emp) + Npages(Dept)) = 3 * (500 + 50) = 1650$

Cost of joining with Finance = $Npages(Finance) + Npages(Result) = 50 + 500 = 25000$

Therefore total cost = $1650 + 25000 = 26650$