#### 1 Overture SYNTAX AND SEMANTICS

$$v \in \mathbb{F}_p, \ w \in \text{String}, \ \iota \in \text{Clients} \subset \mathbb{N}$$

$$\varepsilon ::= r[w] | s[w] | m[w] | p[w] | expressions$$
$$v | \varepsilon - \varepsilon | \varepsilon + \varepsilon | \varepsilon * \varepsilon$$

$$x ::= r[w]@\iota | s[w]@\iota | m[w]@\iota | p[w] | out@\iota$$
 variables

$$\pi ::= m[w]@\iota := \varepsilon @\iota \mid p[w] := e@\iota \mid out@\iota := \varepsilon @\iota \mid \pi; \pi \quad protocols$$

$$(\sigma, x := \varepsilon \mathfrak{G}_l) \Rightarrow \sigma\{x \mapsto \llbracket \sigma, \varepsilon \rrbracket_l\} \qquad \frac{(\sigma_1, \pi_1) \Rightarrow \sigma_2 \qquad (\sigma_2, \pi_2) \Rightarrow \sigma_3}{(\sigma_1, \pi_1; \pi_2) \Rightarrow \sigma_3}$$

#### 2 Overture ADVERSARIAL SEMANTICS

$$(\sigma, x := \varepsilon @ \iota) \implies_{\mathcal{A}} \sigma \{x \mapsto \llbracket \sigma, \varepsilon \rrbracket_{\iota} \} \qquad \iota \in H$$

$$(\sigma, x := \varepsilon @ \iota) \implies_{\mathcal{A}} \sigma \{x \mapsto \llbracket rewrite_{\mathcal{A}}(\sigma_{C}, \varepsilon) \rrbracket_{\iota} \} \qquad \iota \in C$$

$$(\sigma, assert(\varepsilon_{1} = \varepsilon_{2})@ \iota) \implies_{\mathcal{A}} \sigma \qquad \text{if } \llbracket \sigma, \varepsilon_{1} \rrbracket_{\iota} = \llbracket \sigma, \varepsilon_{2} \rrbracket_{\iota} \text{ or } \iota \in C$$

$$(\sigma, assert(\phi(\varepsilon))@ \iota) \implies_{\mathcal{A}} \bot \qquad \text{if } \llbracket \sigma, \varepsilon_{1} \rrbracket_{\iota} = \llbracket \sigma, \varepsilon_{2} \rrbracket_{\iota} \text{ or } \iota \in C$$

$$(\sigma_{1}, \pi_{1}) \implies_{\mathcal{A}} \sigma_{2} \qquad (\sigma_{2}, \pi_{2}) \implies_{\mathcal{A}} \sigma_{3} \qquad \qquad \underbrace{(\sigma_{1}, \pi_{1}) \implies_{\mathcal{A}} \bot}_{(\sigma_{1}, \pi_{1}; \pi_{2}) \implies_{\mathcal{A}} \bot}$$

$$\underbrace{(\sigma_{1}, \pi_{1}; \pi_{2}) \implies_{\mathcal{A}} \sigma_{3}}_{(\sigma_{1}, \pi_{1}; \pi_{2}) \implies_{\mathcal{A}} \bot}$$

$$\underbrace{(\sigma_{1}, \pi_{1}; \pi_{2}) \implies_{\mathcal{A}} \bot}_{(\sigma_{1}, \pi_{1}; \pi_{2}) \implies_{\mathcal{A}} \bot}$$

#### 3 Overture CONSTRAINT TYPING

$$\phi ::= x | \phi + \phi | \phi - \phi | \phi * \phi$$

$$E ::= \phi \equiv \phi | E \wedge E$$

We write  $E_1 \models E_2$  iff every model of  $E_1$  is a model of  $E_2$ . Note that this relation is reflexive and transitive.

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The motivating idea is that we can interpret any protocol  $\pi$  as a set of equality constraints  $\lfloor \pi \rfloor$  and use an SMT solver to verify properties relevant to correctness, confidentiality, and integrity. Further, we can leverage entailment relation is critical for efficiency—we can use annotations to obtain a weakened precondition for relevant properties. That is, given  $\pi$ , program annotations or other cues can be used to find a minimal E with  $\lfloor \pi \rfloor \models E$  for verifying correctness and security.

# 3.0.1 Example: Correctness of 3-Party Addition.

```
\begin{array}{llll} \text{m}[s1]@2 & := & (s[1] - r[local] - r[x])@1 \\ \text{m}[s1]@3 & := & r[x]@1 \\ \text{m}[s2]@1 & := & (s[2] - r[local] - r[x])@2 \\ \text{m}[s2]@3 & := & r[x]@2 \\ \text{m}[s3]@1 & := & (s[3] - r[local] - r[x])@3 \\ \text{m}[s3]@2 & := & r[x]@3 \\ \text{p}[1] & := & (r[local] + m[s2] + m[s3])@1 \\ \text{p}[2] & := & (m[s1] + r[local] + m[s3])@2 \\ \text{p}[3] & := & (m[s1] + m[s2] + r[local])@3 \\ \text{out}@1 & := & (p[1] + p[2] + p[3])@1 \\ \text{out}@2 & := & (p[1] + p[2] + p[3])@2 \\ \text{out}@3 & := & (p[1] + p[2] + p[3])@3 \\ \end{array}
```

Letting  $\pi$  be this protocol, we can verify correctness as:

$$[\pi] \models \text{out@3} \equiv s[1]@1 + s[2]@2 + s[3]@3$$

### 3.1 Confidentiality Types

$$\begin{array}{ll} \text{DepTy} & \frac{E\text{NCODE}}{E \models \phi \equiv \phi' \oplus \texttt{r}[w]@\iota \quad \oplus \in \{+,-\} \quad R, E \vdash \phi' : T} \\ & \frac{E \models \phi \equiv \phi' \oplus \texttt{r}[w]@\iota\}, E \vdash \phi : \{c(\texttt{r}[w]@\iota, T)\} \\ & \frac{R, E \vdash \lfloor e@\iota \rfloor : T}{R, E \vdash x := e@\iota : (x : T)} & \frac{R_1, E \vdash \pi_1 : \Gamma_1 \quad R_2, E \vdash \pi_2 : \Gamma_2}{R_1; R_2, E \vdash \pi_1; \pi_2 : \Gamma_1; \Gamma_2} \end{array}$$

*Definition 3.1.*  $R, E \vdash \pi : \Gamma$  is *valid* iff it is derivable and  $|\pi| \models E$ .

$$\frac{\iota \in C}{\Gamma, C \vdash \Gamma(\mathbb{m}[w]@\iota)} \qquad \frac{\Gamma, C \vdash T_1 \cup T_2}{\Gamma, C \vdash T_1} \qquad \frac{\Gamma, C \vdash \{\mathbb{m}[w]@\iota\}}{\Gamma, C \vdash \Gamma(\mathbb{m}[w]@\iota)}$$
 
$$\frac{\Gamma, C \vdash \{r[w]@\iota\} \qquad \Gamma, C \vdash \{c(r[w]@\iota, T)\}}{\Gamma, C \vdash T}$$

THEOREM 3.2. If  $R, E \vdash \pi : \Gamma$  is valid and for all H, C it is not the case that  $\Gamma, C \vdash \{s[w]@\iota\}$  for  $\iota \in H$ , then  $\pi$  satisfies gradual release.

## 3.1.1 Examples.

```
m[s1]@2 := (s[1] - r[local] - r[x])@1
m[s1]@3 := r[x]@1

// m[s1]@2 : { c(r[x]@1, { c(r[local]@1, {s[1]@1} ) }

// m[s1]@3 : { r[x]@1 }
```

m[x]@1 := s2(s[x], -r[x], r[x])@2

 $// m[x]@1 : { c(r[x]@2, { s[x]@2 }) }$ 

 $// m[y]@1 : { c(r[y]@2, { s[y]@1 }) }$ 

m[y]@1 := OT(s[y]@1,-r[y],r[y])@2

// m[x]@1 == s[x]@2 + -r[x]@2

// m[y]@1 == s[y]@1 + -r[y]@2

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```

# **3.2 Compositional Type Verification in** *Prelude*

(\*Need to fix the following to allow reduction of x. – Chris\*)

$$\frac{e_1 \Rightarrow \varepsilon \qquad e_2 \Rightarrow \iota \qquad R_1, E \Vdash \lfloor \varepsilon @ \iota \rfloor : (R_2, T)}{R_1, E \vdash x := e_1 @ e_2 : (x : T, R_1; R_2, E \land x \equiv \lfloor \varepsilon @ \iota \rfloor)}$$

$$\frac{\text{Encode}}{e_1 \Rightarrow \varepsilon \qquad e_2 \Rightarrow \iota \qquad e_3 \Rightarrow \phi \qquad E \models \lfloor \varepsilon @ \iota \rfloor \equiv \phi \qquad R_1, E \Vdash \phi : (R_2, T)}{R_1, E \vdash x := e_1 @ e_2 \text{ as } e_3 : (x : T, R_1; R_2, E \land x \equiv \phi)}$$

$$\frac{\text{App}}{R_1, E \vdash x := e_1 @ e_2 \text{ as } e_3 : (x : T, R_1; R_2, E \land x \equiv \phi)}$$

$$\frac{e_1 \Rightarrow v_1 \cdots e_n \Rightarrow v_n \qquad \rho = \lfloor v_1/x_1 \rfloor \cdots \lfloor v_n/x_n \rfloor \qquad E \models \rho(E_1)}{R_1, E \vdash f(e_1, \dots, e_n) : (\rho(\Gamma), R_1; \rho(R), E \land \rho(E_2))}$$

$$\frac{\text{Seq}}{R_1, E_1 \vdash \pi_1 : (\Gamma_2, R_2, E_2) \qquad R_2, E_2 \vdash \pi_2 : (\Gamma_3, R_3, E_3)}{R_1, E_1 \vdash \pi_1; \pi_2 : (\Gamma_2; \Gamma_3, R_3, E_3)}$$

Sig
$$C(f) = x_1, \dots, x_n, \mathbf{c} \qquad \rho = [v_1/x_1] \cdots [v_n/x_n] \qquad \emptyset, \rho(E_1) \vdash \mathbf{c} : (\rho(\Gamma), \rho(R), \rho(E_2))$$

$$f : \{E_1\} \ x_1, \dots, x_n \ \{\Gamma, R, E_2\}$$

*Definition 3.3.* sig is *verified* iff f : sig(f) is valid for all  $f \in dom(sig)$ .

The following theorem holds for protocols with default preprocessing.

THEOREM 3.4. If sig is verified and  $\emptyset$ ,  $\emptyset \vdash e : (\Gamma, R, E)$  then  $e \Rightarrow \pi$  and  $R, E \vdash \pi : \Gamma$  is valid.

 $\Gamma, R, E \vdash_{\iota} \varepsilon : T \cdot \varsigma_2$ 

# 3.3 Integrity Types

 $\Gamma, \varnothing, E \vdash_{\iota} \mathsf{m[w]} : \Gamma(\mathsf{m[w]}@\iota)$ 

Value Secret Rando  $\Gamma, \emptyset, E \vdash_{\iota} v : \emptyset \cdot \text{High} \qquad \Gamma, \emptyset, E \vdash_{\iota} s[w] : \{s[w]@_{\ell}\} \cdot \mathcal{L}(\iota) \qquad \Gamma, \emptyset, E \vdash_{\iota} r[w] : \{r[w]@_{\ell}\} \cdot \mathcal{L}(\iota)$   $Mesg \qquad \qquad PubM \qquad \qquad \Gamma, R, E \vdash_{\iota} \varepsilon : T \cdot \varsigma_{1} \qquad \varsigma_{1} \leq \varsigma_{2}$ 

 $\Gamma, \emptyset, E \vdash_{\iota} p[w] : \Gamma(p[w])$ 

ENCODE  $\frac{\Gamma, \emptyset, E \vdash_{\iota} \varepsilon : T \cdot \varsigma \qquad E \models \lfloor \varepsilon @_{\iota} \rfloor = \phi \oplus r[w] @_{\iota}' \qquad \oplus \in \{+, -\}}{\Gamma, r[w] @_{\iota}, E \vdash_{\iota} \varepsilon : \{c(r[w] @_{\iota}', \Gamma(\phi))\} \cdot \varsigma}$ 

 $\frac{\Gamma, R_1, E \vdash_{\iota} \varepsilon_1 : T_1 \cdot \varsigma \qquad \Gamma, R_2, E \vdash_{\iota} \varepsilon_2 : T_2 \cdot \varsigma \qquad \oplus \in \{+, -, *\}}{\Gamma, R_1; R_2, E \vdash_{\iota} \varepsilon_1 \oplus \varepsilon_2 : T_1 \cup T_2 \cdot \varsigma}$ 

$$\frac{\Gamma, R, E \vdash_{\iota} \varepsilon : T \cdot \mathcal{L}(\iota)}{\Gamma, R, E \vdash_{\iota} \varepsilon : E \otimes_{\iota} : \Gamma; x : T \cdot \mathcal{L}(\iota), E'} \qquad \frac{Assert}{E \models_{\iota} \varepsilon_{1}@_{\iota} = [\varepsilon_{2}@_{\iota}]} \\ \frac{E \vdash_{\iota} \varepsilon_{1}@_{\iota} = [\varepsilon_{2}@_{\iota}]}{\Gamma, R, E \vdash_{\iota} ssert(\varepsilon_{1} = \varepsilon_{2})@_{\iota} : \Gamma, E}$$

$$\frac{\Gamma_{1}, R_{1}, E_{1} \vdash \pi_{1} : \Gamma_{2}, E_{2}}{\Gamma_{1}, R_{1}; R_{2}, E_{1} \vdash \pi_{1}; \pi_{2} : \Gamma_{3}, E_{3}} \qquad \frac{\Gamma_{1}, R_{1}, E_{1} \vdash \pi_{1} : \Gamma_{2}, E_{2}}{\Gamma_{1}, R_{1}; R_{2}, E_{1} \vdash \pi_{1}; \pi_{2} : \Gamma_{3}, E_{3}} \qquad \frac{\Gamma_{1}, R_{1}, E_{1} \vdash \pi_{1} : \Gamma_{2}, E_{2}}{\Gamma_{1}, R_{1}, E_{1} \vdash \pi_{1} : \Gamma_{2}, E_{2}} \qquad E_{1} \models E_{1}' \qquad E_{2} \models E_{2}'$$

 $\frac{\text{MAC}}{E \models \texttt{m[wm]}@\iota = \texttt{m[wk]}@\iota + (\texttt{m[delta]}@\iota * \texttt{m[ws]}@\iota)} \qquad \Gamma(\texttt{m[ws]}@\iota) = T \cdot \varsigma$   $\frac{\Gamma, R, E \vdash \texttt{assert(m[wm]} = \texttt{m[wk]} + (\texttt{m[delta]} * \texttt{m[ws]}))@\iota : \Gamma; \texttt{m[ws]}@\iota : T \cdot \text{High}, E$ 

#### 4 Prelude SYNTAX AND SEMANTICS

 $\ell \in \text{Field, } y \in \text{EVar, } f \in \text{FName} \\ e ::= v \mid r[e] \mid s[e] \mid m[e] \mid p[e] \mid e \ binop \ e \mid \text{let } y = e \ \text{in } e \mid \\ f(e, \ldots, e) \mid \{\ell = e; \ldots; \ell = e\} \mid e.\ell \\ c ::= m[e]@e := e@e \mid p[e] := e@e \mid \text{out}@e := e@e \mid \text{assert}(e = e)@e \mid \\ f(e, \ldots, e) \mid c; c \mid \text{pre}(E) \mid \text{post}(E) \\ \\ binop ::= + \mid -\mid *\mid ++ \\ v ::= w \mid \iota \mid \varepsilon \mid \{\ell = v; \ldots; \ell = v\} \\ fn ::= f(y, \ldots, y)\{e\} \mid f(y, \ldots, y)\{c\} \\ \phi ::= r[e]@e \mid s[e]@e \mid m[e]@e \mid p[e] \mid \text{out}@e \mid \phi + \phi \mid \phi - \phi \mid \phi * \phi \\ E ::= \phi \equiv \phi \mid E \land E \\$ 

```
\frac{e[v/y] \Rightarrow v'}{\text{let } y = v \text{ in } e \Rightarrow v'}
                                       C(f) = y_1, \dots, y_n, \ e \qquad e_1 \Rightarrow v_1 \cdots e_n \Rightarrow v_n \qquad e[v_1/y_1] \cdots [v_n/y_n] \Rightarrow v
f(e_1, \dots, e_n) \Rightarrow v
              \frac{e_1 \Rightarrow \nu_1 \cdots e_n \Rightarrow \nu_n}{\{\ell_1 = e_1; \dots; \ell_n = e_n\} \Rightarrow \{\ell_1 = \nu_1; \dots; \ell_n = \nu_n\}} \qquad \frac{e \Rightarrow \{\dots; \ell = \nu; \dots\}}{e \cdot \ell \Rightarrow \nu} \qquad \frac{e_1 \Rightarrow w_1 \qquad e_2 \Rightarrow w_2}{e_1 + e_2 \Rightarrow w_1 w_2}
                                                                                        e_1 \Rightarrow \varepsilon_1 \qquad e_2 \Rightarrow \varepsilon_2 \qquad e \Rightarrow \iota
                     \frac{e_1 \Rightarrow \varepsilon_1 \quad e_2 \Rightarrow \varepsilon_2 \quad e \Rightarrow \iota}{(\pi, (E_1, E_2), \mathsf{on}, \mathsf{assert}(e_1 = e_2)@e) \Rightarrow (\pi; \mathsf{assert}(\varepsilon_1 = \varepsilon_2)@\iota, (E_1, E_2 \land \lfloor \varepsilon_1@\iota \rfloor = \lfloor \varepsilon_2@\iota \rfloor), \mathsf{on})}
                                       \frac{e_1 \Rightarrow \varepsilon_1 \qquad e_2 \Rightarrow \varepsilon_2 \qquad e \Rightarrow \iota}{(\pi, (E_1, E_2), \mathsf{off}, \mathsf{assert}(e_1 = e_2)@e) \Rightarrow (\pi; \mathsf{assert}(\varepsilon_1 = \varepsilon_2)@\iota, (E_1, E_2, \mathsf{off})}
                      \frac{e_1 \Rightarrow w \qquad e_2 \Rightarrow \iota_1 \qquad e_3 \Rightarrow \varepsilon \qquad e_4 \Rightarrow \iota_2}{(\pi, (E_1, E_2), \mathsf{on}, \mathsf{m} \llbracket e_1 \rrbracket @ e_2 := e_3 @ e_4) \Rightarrow (\pi; \mathsf{m} \llbracket w \rrbracket @ \iota_1 := \varepsilon @ \iota_2, (E_1 \land \mathsf{m} \llbracket w \rrbracket @ \iota_1 = \lfloor \varepsilon @ \iota_2 \rfloor, E_2), \mathsf{on})}
                                          \frac{e_1 \Rightarrow w \qquad e_2 \Rightarrow \iota_1 \qquad e_3 \Rightarrow \varepsilon \qquad e_4 \Rightarrow \iota_2}{(\pi, (E_1, E_2), \mathsf{off}, \mathsf{m}[e_1]@e_2 := e_3@e_4) \Rightarrow (\pi; \mathsf{m}[w]@\iota_1 := \varepsilon@\iota_2, (E_1, E_1), \mathsf{off})}
                                                                        (\pi, (E_1, E_2), \mathsf{on}, \mathsf{pre}(E)) \Rightarrow (\pi, E_1, E_2 \land E, \mathsf{off})
                                                                     (\pi, (E_1, E_2), \mathsf{off}, \mathsf{post}(E)) \Rightarrow (\pi, (E_1 \land E, E_2), \mathsf{on})
175
                  (\pi_1, (E_{11}, E_{12}), sw_1, c_1) \Rightarrow (\pi_2, (E_{21}, E_{22}), sw_2) \qquad (\pi_2, (E_{21}, E_{22}), sw_2, c_2) \Rightarrow (\pi_3, (E_{31}, E_{32}), sw_3)
                                                                     (\pi_1, (E_{11}, E_{12}), sw_1, \mathbf{c}_1; \mathbf{c}_2) \Rightarrow (\pi_3, (E_{31}, E_{32}), sw_3)
                                                                                                     C(f) = y_1, \ldots, y_n, \mathbf{c}
                        e_1 \Rightarrow v_1 \cdots e_n \Rightarrow v_n \qquad (\pi_1, (E_{11}, E_{12}), sw_1, \mathbf{c}[v_1/y_1,] \cdots [v_n/y_n]) \Rightarrow (\pi_2, (E_{21}, E_{22}), sw_2)
                                                              (\pi_1, (E_{11}, E_{12}), sw_1, f(e_1, \dots, e_n)) \Rightarrow (\pi_2, (E_{21}, E_{22}), sw_2)
              5 EXAMPLES
                         encodegmw(in, i1, i2) {
                              m[in]@i2 := (s[in] xor r[in])@i2;
                              m[in]@i1 := r[in]@i2
                         }
                         andtablegmw(b1, b2, r) {
                               let r11 = r xor (b1 xor true) and (b2 xor true) in
                              let r10 = r \times r  (b1 xor true) and (b2 xor false) in
                              let r01 = r \times r  (b1 xor false) and (b2 xor true) in
                              let r00 = r xor (bl xor false) and (b2 xor false) in
                              \{ \text{ row1} = \text{r11}; \text{ row2} = \text{r10}; \text{ row3} = \text{r01}; \text{ row4} = \text{r00} \}
```

```
}
197
198
          andgmw(z, x, y) \{
199
            pre();
200
            let r = r[z] in
201
202
            let table = andtablegmw(m[x], m[y], r) in
203
            m[z]@2 := OT4(m[x], m[y], table, 2, 1);
204
            m[z]@1 := r@1;
            post(m[z]@1 xor m[z]@2 == (m[x]@1 xor m[x]@2) and (m[y]@1 xor m[y]@2))
205
          }
206
207
208
          xorgmw(z, x, y)  {
            m[z]@1 := (m[x] xor m[y])@1; m[z]@2 := (m[x] xor m[y])@2;
209
          }
210
211
212
          decodegmw(z) {
            p["1"] := m[z]@1; p["2"] := m[z]@2;
213
214
            out@1 := (p["1"] xor p["2"])@1;
            out@2 := (p["1"] \times p["2"])@2
          }
          encodegmw("x",2,1);
          encodegmw("y",2,1);
          encodegmw("z",1,2);
220
          andgmw("g1", "x", "z");
221
          xorgmw("g2","g1","y");
222
          decodegmw("g2")
224
          pre();
          post(out@1 == (s["x"]@1 and s["z"]@2) xor s["y"]@1)
226
227
       secopen(w1,w2,w3,i1,i2) {
228
            pre(m[w1++"m"]@i2 == m[w1++"k"]@i1 + (m["delta"]@i1 * m[w1++"s"]@i2 /\
229
                m[w1++"m"]@i2 == m[w1++"k"]@i1 + (m["delta"]@i1 * m[w1++"s"]@i2));
230
            let locsum = macsum(macshare(w1), macshare(w2)) in
231
            m[w3++"s"]@i1 := (locsum.share)@i2;
232
            m[w3++"m"]@i1 := (locsum.mac)@i2;
233
            auth(m[w3++"s"],m[w3++"m"],mack(w1) + mack(w2),i1);
234
            m[w3]@i1 := (m[w3++"s"] + (locsum.share))@i1
235
       }
236
237
238
       _{open(x,i1,i2)}
239
         m[x++"exts"]@i1 := m[x++"s"]@i2;
240
         m[x++"extm"]@i1 := m[x++"m"]@i2;
241
         assert(m[x++"extm"] == m[x++"k"] + (m["delta"] * m[x++"exts"]));
242
         m[x]@i1 := (m[x++"exts"] + m[x++"s"])@i2
243
       }`
244
245
```

293 294

```
246
       _{sum}(z, x, y, i1, i2) \{
247
            pre(m[x++"m"]@i2 == m[x++"k"]@i1 + (m["delta"]@i1 * m[x++"s"]@i2 /\
248
                m[y++"m"]@i2 == m[y++"k"]@i1 + (m["delta"]@i1 * m[y++"s"]@i2));
249
            m[z++"s"]@i2 := (m[x++"s"] + m[y++"s"])@i2;
            m[z++"m"]@i2 := (m[x++"m"] + m[y++"m"])@i2;
251
            m[z++"k"]@i1 := (m[x++"k"] + m[y++"k"])@i1;
253
            post(m[z++"m"]@i2 == m[z++"k"]@i1 + (m["delta"]@i1 * m[z++"s"]@i2)
       }
255
       sum(z,x,y) \{ sum(z,x,y,1,2); sum(z,x,y,2,1) \}
256
257
258
       open(x) \{ open(x,1,2); open(x,2,1) \}
259
260
       sum("a", "x", "d");
261
       open("d");
262
       sum("b", "y", "e");
263
       open("e");
       let xys =
            macsum(macctimes(macshare("b"), m["d"]),
                   macsum(macctimes(macshare("a"), m["e"]),
267
                           macshare("c")))
       let xyk = mack("b") * m["d"] + mack("a") * m["e"] + mack("c")
269
270
       secopen("a", "x", "d", 1, 2);
271
          secopen("a", "x", "d", 2, 1);
272
          secopen("b", "y", "e", 1, 2);
273
          secopen("b", "y", "e", 2, 1);
275
          let xys =
            macsum(macctimes(macshare("b"), m["d"]),
                   macsum(macctimes(macshare("a"), m["e"]),
277
                           macshare("c")))
279
          in
          let xyk = mack("b") * m["d"] + mack("d") * m["d"] + mack("c")
281
          secreveal(xys,xyk,"1",1,2);
282
          secreveal(maccsum(xys,m["d"] * m["e"]),
283
                     xyk - m["d"] * m["e"],
284
                     "2",2,1);
285
         out@1 := (p[1] + p[2])@1;
286
         out@2 := (p[1] + p[2])@2;
287
288
289
290
291
292
```