

# Data Hiding in Homomorphically Encrypted Medical Images for Verifying Their Reliability in both Encrypted and Spatial Domains

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**Abstract**— In this paper, we propose a new scheme of data hiding of encrypted images for the purpose of verifying the reliability of an image into both encrypted and spatial domains. This scheme couples the Quantization Index Modulation (QIM) and the Paillier cryptosystem. It relies on the insertion into the image, before its encryption, of a predefined watermark, a “pre-watermark”. Message insertion (resp. extraction) is conducted into (resp. from) the encrypted image using a modified version of QIM. It is the impact of this insertion process onto the “pre-watermark” that gives access to the message in the spatial domain, i.e. after the image has been decrypted. With our scheme, encryption/decryption processes are completely independent from message embedding/extraction. One does not need to know the encryption/decryption key for hiding a message into the encrypted image. Experiments conducted on ultrasound medical images show that the image distortion is very low while offering a high capacity that can support different watermarking based security objectives.

## I. INTRODUCTION

Cloud computing services become important solutions for the storage and continuous availability of data supplied by multiple sources. Due to the outsourcing of data and services, they are exposed to many threats that strongly increase security requirements in terms of [1]: confidentiality, availability and reliability (i.e. integrity and authentication). Among available security mechanisms, encryption is commonly used so as to ensure medical data confidentiality. However, once decrypted, one piece of information is no longer protected and it becomes hard to verify its integrity and its origin. From this point of view, encryption appears as an “*a priori*” protection. Watermarking has been proposed as a complementary mechanism that can improve security of medical images. When it is applied to images, watermarking modifies or modulates the image pixels’ gray level values in an imperceptible way, in order to encode or insert some security attributes (i.e. the watermark) into it. As defined, such a protected image can be accessed while remaining protected by these hidden security attributes that can be used for example for verifying the image reliability (i.e., its integrity, its origins and its attachment to one patient). Thus, combining watermarking with encryption may allow us ensuring an *a priori*/ *a posteriori* protection at the same time. In practice, watermarking is usually conducted before encryption or during the encryption/decryption processes.

However, in order to watermark outsourced data without endangering privacy and data confidentiality, different approaches have been proposed so as to embed a message directly into the encrypted image, essentially in the framework of copyright protection. Three categories of approaches can be distinguished according to the availability of the embedded message into the spatial domain (i.e. after decryption process) and/or in the encrypted domain:

- *Message available in the spatial domain (MSD)*- The scheme proposed in [2] exploits homomorphic encryption, which allows modifying an encrypted image for the embedding of a watermark.
- *Message available in the encrypted domain (MED)*- As example, in [3], the image is firstly divided into patches. Before encryption, some patches are replaced by patches computed from their sparse coefficients while the residual errors in-between patches are reversibly embedded into the rest of patches; leaving thus some free space by next is used for message embedding in the encrypted domain
- *Message available in both encrypted and spatial domains (MSED)*- most of these methods are based on partial encryption [4] or invariant encryption [5]. With those methods, only some parts of the host image are encrypted while the rest of it is watermarked. Recently, a novel concept, called VRBE (Vacating Room Before Encryption) has been proposed in [6]. Its principle is to reversibly watermark an image before encrypting it so as to leave some free space into the encrypted domain for message embedding. However, to make possible the retrieval of this free space into the encrypted domain, the image has to be reorganized before encryption. Moreover, the decryption process is modified so as to make possible message extraction in the spatial domain. As example, in [6] watermarkable positions in the encrypted image are placed at the beginning of the bit stream and, at the reception, watermarked positions are not decrypted.

In this paper, we propose a new scheme of MSED type, which principles allow the insertion of some security attributes into an encrypted image; attributes by next available in both encrypted and spatial domains for verifying the image reliability in both domains. Compared to other MSED methods, our approach entirely encrypts the image; and watermarking and encryption/decryption are independent. Indeed, message insertion and extraction processes (resp. encryption and decryption) do not require the knowledge of the encryption key (resp. watermarking key or other extra parameters).

The remainder of this paper is organized as follows. In Section II, we present QIM modulation and Paillier cryptosystem we used to implement our scheme. We describe the proposed system in section III and evaluate its

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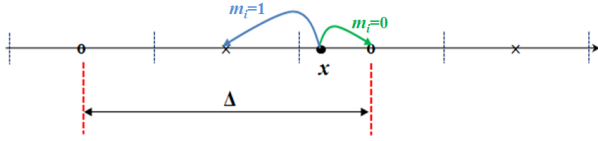


Figure 1. Insertion with QIM mono-dimensional of a binary message into a pixel value  $x$ . Symbols  $\circ$  and  $\times$  denote cells' centers that encode 0 and 1, respectively.

performance through some experiments on ultrasound images in section IV.

## II. CRYPTOGRAPHIC AND WATERMARKING PRIMITIVES

### A. Watermarking primitive: QIM

Quantization Index Modulation [7] relies on quantifying some image components according to a set of quantizers based on codebooks in order to insert a message. More clearly, to one message  $m_i$  issued from a finite set of possible messages  $M = \{m_i\}_{i=0,\dots,q}$ , QIM associates the elements of a codebook  $C_{m_i}$  such as

$$C_{m_i} \cap C_{m_j} = \emptyset, i \neq j. \quad (1)$$

By substituting one component of the image by its nearest element in the codebook  $C_{m_i}$ , one allows the insertion of  $m_i$ . Let us consider one image component such as a pixel value  $x \in \mathbb{N}$  and a binary message  $m_i$ , i.e.  $m_i \in \{0,1\}$ . In this case, two codebooks  $C_0$  and  $C_1$  are defined. They can be built up by uniformly quantizing the dynamic of  $x$  with a quantization step  $\Delta$ , a QIM parameter, as illustrated in Fig. 1. In this example, intervals centered on crosses represent  $C_1$  ( $m_i = 1$ ) whereas intervals centered on circles represent  $C_0$  ( $m_i = 0$ ). Thus,  $x$  will be moved to the nearest cross or circle in order to encode  $m_i$ . Herein, the codebook  $C_{m_i}$  can be defined as

$$C_{m_i} = \{c_{m_i,k}\} = \{(k + m_i/2)\Delta, k \in \mathbb{N}\} \quad (2)$$

and the watermarked version of  $x$ , i.e.  $x_w$ , is given by

$$x_w = Q_\Delta(x, m_i) \text{ where } Q_\Delta(x, m_i) = \min_k (|x - c_{m_i,k}|) \quad (3)$$

Let us consider  $\hat{x}$  a possible attacked version of  $x_w$ . During the extraction step, the knowledge of the interval (or the codebook) to which belongs  $\hat{x}$  is enough to identify the embedded message and, if  $\hat{m}_i$  is the extracted message from  $\hat{x}$  then

$$\hat{m}_i = Q_\Delta^{ext}(\hat{x}) \quad (4)$$

where  $Q_\Delta^{ext}$  is the QIM extraction function defined as:

$$Q_\Delta^{ext}(\hat{x}) = \arg \min_{m_i \in \{0,1\}} \min_{c_{m_i,k} \in C_{m_i}} |c_{m_i,k} - \hat{x}|$$

### B. Homomorphic encryption algorithm: Paillier cryptosystem

In this work, we opted for the asymmetric Paillier cryptosystem because of its additive homomorphic property [8]. It stands on a public-private key pair  $(K_p, K_s)$ , such as:

$$K_p = pq \text{ and } K_s = (p-1)(q-1) \quad (5)$$

where  $p$  and  $q$  are two large prime integers. The Paillier encryption of a plaintext  $m$  into the ciphertext  $c$  using the public key  $K_p$  is given by:

$$c = E[m, r] = (1 + K_p)^m r^{K_p} \bmod K_p^2 \quad (6)$$

where  $r \in \mathbb{Z}_N^*$  is a random integer associated to  $m$  making the Paillier cryptosystem probabilistic or semantically

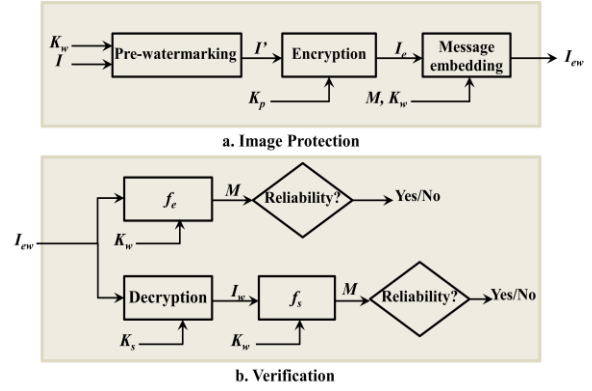


Figure 2. General architecture of our system.  $K_w$  and  $(K_p, K_s)$  are the watermarking key and the emitter or receiver public-private key pair. secure. Based on  $r$ , the encryption of the same plaintext message yields to different ciphertexts even though the encryption key is the same. The decryption of  $c$  using the private key  $K_s$  is as follows

$$m = (c^{K_s} - 1)/K_p \bmod K_p \quad (7)$$

If we consider two plaintexts  $m_1$  and  $m_2$ , the additive homomorphic property of Paillier cryptosystem ensures that

$$E[m_1, r_1] \times E[m_2, r_2] = E[m_1 + m_2, r_1 + r_2] \quad (8)$$

$$E[m_1, r_1]^{m_2} = E[m_1 m_2, r_1^{m_2}] \quad (9)$$

## III. DATA HIDING IN HOMOMORPHIC DOMAIN

### A. System architecture and principle

The architecture of our system is depicted in figure 2. It relies on two main procedures: protection and verification. The first one (Fig. 2a) allows the embedding within an encrypted image of a message  $M$  that will be available in both encrypted and spatial domains (i.e. in the encrypted and decrypted images). Herein,  $M$  is a sequence of bits that encodes some security attributes assessing the image integrity and authenticity in both domains. In order to make possible such embedding, and especially the extraction of  $M$  after the image has been decrypted, our solution relies on a pre-watermarking procedure. This one consists in the QIM embedding into the image  $I$  of a predefined watermark  $W$  before the encryption process. Once  $I$  is pre-watermarked into  $I'$ ,  $I'$  is encrypted into  $I_e$ .  $M$  is then embedded into  $I_e$  leading to the watermarked encrypted image  $I_{ew}$ . It is the impact of the distortion induced by this watermarking operation in the encrypted domain onto  $W$  that will give access to  $M$  in the spatial domain. More clearly, due to the fact the embedding of  $M$  modifies the encrypted image  $I_e$  into  $I_{ew}$ , the resulting decrypted image  $I_w$  will then differ from  $I'$ . It is the differences between the original watermark  $W$  and the extracted one that allows the encoding of  $M$  into  $I_w$ . As illustrated in Fig. 2.b., the access to  $M$  in both encrypted (i.e. from  $I_{ew}$ ) and spatial (i.e. from  $I_w$ ) domains, relies on two extraction functions  $f_e$  and  $f_s$ , respectively. These functions are defined according to the watermarking modulations used in the encrypted and spatial domains. We will come back on this point in the next section. It is important to notice that, in our approach, message insertion/extraction and image encryption/decryption are considered as independent processes. Moreover, all of pre-watermark embedding,

encryption and data hiding processes do not have to be conducted at the same time. In the following, we detail the different steps of our system and how they interact considering image protection and message extraction separately in application to 8 bit grayscale images.

### B. Image Protection

This procedure is constituted of three main steps (see Fig. 2.a): image pre-watermarking, pre-watermarked image encryption, message embedding in the encrypted domain.

#### 1) Pre-watermarking step

Based on the watermarking key  $K_w$ , a watermark  $W$  is first generated. From here on,  $W$  corresponds to a random sequence of  $p$  bits:  $W = \{w_1, \dots, w_j, \dots, w_p\}, w_j \in \{0,1\}$ .  $W$  is then embedded into the image  $I$  as follows:

- i. using  $K_w$ ,  $I$  is secretly splitted into  $N$  non-overlapping and distributed subsets of  $p$  pixels  $\{I_i\}_{i=1,\dots,N}$  with

$$I_i = \{I_i^1, \dots, I_i^j, \dots, I_i^p\}, p \geq 2 \text{ and } I_i^j \in \mathbb{N} \quad (10)$$

where  $I_i^j$  corresponds to the  $j^{\text{th}}$  pixel of  $I_i$ .

- ii.  $W$  is then embedded into each subset  $I_i$  by embedding one bit  $w_j$  within  $I_i^j$  using QIM and a quantization step  $\Delta$  (see Eq. 3)

$$I_i^{j'} = Q_\Delta(I_i^j, w_j), \forall j \in \{1, \dots, p\} \quad (11)$$

The resulting pre-watermarked image  $I'$  is thus given by

$$I' = \{I'_i\}_{i=1,\dots,N} \text{ where } I'_i = \{I_i^1, \dots, I_i^{j'}, \dots, I_i^p\} \quad (12)$$

#### 2) Encryption step

During this step, the previous pre-watermarked image  $I'$  is encrypted into  $I_e$  using the Paillier cryptosystem and the public key  $K_p$ :  $I_e = \{I_{ie}\}_{i=1,\dots,N}$ . Encrypted subsets  $\{I_{ie}\}_{i=1,\dots,N}$  are obtained from the pre-watermarked pixel subsets  $\{I'_i\}_{i=1,\dots,N}$  such as (see Eq 6)

$$I_{ie} = \{I_{ie}^1, \dots, I_{ie}^j, \dots, I_{ie}^p\} \text{ with } I_{ie}^j = E[I_i^{j'}, r_i^j] \quad (13)$$

where  $r_i^j$  is random and associated to  $I_i^{j'}$  (see section II.B)

#### 3) Message embedding step

This process enables an authorized user who knows the watermarking key  $K_w$  to embed into the encrypted image  $I_e$  a message  $M$ , which is a sequence of bits  $\{b_i\}_{i=1,\dots,N}$  uniformly distributed, i.e.  $\Pr(b_i=0)=\Pr(b_i=1)=0.5$ . Based on the knowledge of  $K_w$ , subsets of encrypted pixels  $\{I_{ie}\}_{i=1,\dots,N}$  are retrieved. One bit of  $M$  is embedded per subset  $I_{ie}$  and will be available in both encrypted and spatial domains such as

$$b_i = f_e(I_{ie}) = f_s(I_{iw}) \quad (14)$$

where  $I_{ie}$  is the watermarked version of the subset  $I_{ie}$ ;  $I_{iw}$  is the decrypted version of  $I_{ie}$ .

In this paper, one bit  $b_i$  of  $M$  is embedded in all the pixel  $I_{ie}^j$  of the encrypted subset  $I_{ie}$  using a modified version of QIM. More clearly,  $b_i$  is repeated  $p$  times into the subset  $I_{ie}$ . At the same time, and in order to make  $b_i$  available in the spatial domain, this process should guarantee that the pre-watermark is or not modified. The rule we imposed to make this possible is the following one: if the pre-watermark  $W$  in the decrypted subset  $I_i^{j'}$  is unchanged then a '0' was embedding, on the contrary '1' has been inserted. As a consequence, the embedding process in the encrypted domain should make sure that the pre-watermark bit  $w_j$  into  $I_i^{j'}$  commutes if  $b_i=1$  or remains unchanged if  $b_i=0$ .

As illustrated in Fig. 1, to modify (*resp.* to not) the embedded bit  $w_j$ , the necessary distortion  $d_{wj}$  induced by the insertion process of  $b_i$  into  $I_{ie}^j$  must verify:  $\frac{\Delta}{4} < |d_{wj}| < \frac{3\Delta}{4}$  (*resp.*  $|d_{wj}| < \frac{\Delta}{4}$ ). To guarantee such degree of distortion, we exploit the additive homomorphic property of Paillier cryptosystem. It allows modulating  $I_{ie}^j$  for both the embedding of  $b_i$  and the introduction of a distortion  $d_{wj}$  in the spatial domain. Basically, the watermarked version of  $I_{ie}^j$ ,  $I_{iew}^j$  is obtained by multiplying  $I_{ie}^j$  with an encrypted version of  $d_{wj}$  such as:

$$\begin{aligned} I_{iew}^j &= I_{ie}^j \times E[d_{wj}, r_k] = E[I_i^{j'}, r_i^j] \times E[d_{wj}, r_k] \\ &= E[I_i^{j'} + d_{wj}, r_i^j + r_k] \end{aligned} \quad (15)$$

where  $r_k$  is a random integer that satisfies

$$Q_\Delta^{ext}(I_{ie}^j \times E[d_{wj}, r_k]) = b_i \quad (16)$$

and  $d_{wj}$  verifies

$$\begin{cases} \frac{\Delta}{4} < |d_{wj}| < \frac{3\Delta}{4} & \text{if } b_i = 1 \\ |d_{wj}| < \frac{\Delta}{4} & \text{if } b_i = 0 \end{cases} \quad (17)$$

As it can be seen, by choosing an appropriate random value  $r_k$  one can insert  $b_i$  into an encrypted pixel with QIM (eq. 16); and at the same time, we induce the desired distortion into the spatial domain (eq. 17). Notice that in our implementation, we work with  $d_{wj} = \frac{b_i \Delta}{2}$ . By doing so and considering  $D$  the decryption function of the Paillier cryptosystem, the decryption version of  $I_{iew}^j$ ,  $I_{iw}^j$ , is equal to

$$I_{iw}^j = D[I_{iew}^j] = D[E[I_i^{j'} + \frac{b_i \Delta}{2}, r_i^j + r_k]] = I_i^{j'} + \frac{b_i \Delta}{2} \quad (18)$$

As a consequence, the insertion of  $b_i = '0'$  into  $I_{ie}$  doesn't modify  $I_i^{j'}$  (i.e.  $I_{iw}^j = I_i^{j'}$ ). On the contrary, embedding  $b_i = '1'$  into  $I_{ie}$  implicitly modifies the embedded value  $w_j$  due to the fact that  $I_{iw}^j = I_i^{j'} + \frac{\Delta}{2}$ .

To sum-up, the extraction functions  $f_e$  we use to extract  $b_i$  from one encrypted watermarked pixel subset  $I_{iew}$  is such as

$$b_i = f_e(I_{iew}) = \begin{cases} 1 & \text{if } \sum_{j=1}^p Q_\Delta^{ext}(I_{iew}^j) > \frac{p}{2} \\ 0 & \text{else} \end{cases} \quad (19)$$

While, in the spatial domain, the extraction function  $f_s$  is

$$b_i = f_s(I_{iw}) = \begin{cases} 0 & \text{if } Q_\Delta^{ext}(I_{iw}^j) = w_j \forall j \in \{1, \dots, p\} \\ 1 & \text{otherwise} \end{cases} \quad (20)$$

#### C. Message extraction step

As said previously, the message  $M$  can be extracted in both encrypted and spatial domains. In the encrypted domain, according to  $K_w$ , the encrypted image ( $I_{ew}$ ) is firstly splitted into subsets of  $p$  encrypted pixels  $\{I_{iew}\}$ . Then,  $f_e$  (Eq. 19) is used to extract from each of them one bit of the message  $M$ . Once the image is decrypted using  $K_s$ ,  $M$  is simply read with the help of  $f_s$  (see eq. 20) applied to the pixel subsets  $\{I_{iw}\}$  of the decrypted image ( $I_w$ ).

## IV. EXPERIMENTAL RESULTS AND DISCUSSION

Experiments were conducted on 100 8 bit depth ultrasound images of 576×688 pixels. Two indicators are considered to evaluate the performance of our system: capacity and watermark imperceptibility.

**Capacity:** Because one bit of message is embedded per pixel subset, the capacity one can insert into an image depends on the dimensions of the pixel subsets and of the image. Indeed, the achieved capacity rate is equal to  $1/p$  bpp (bit per pixel). Working with  $p=1$  leads to a capacity of 1bpp or equivalently to a message of about 396 Kbits. This capacity is large enough for the insertion of some security attributes assessing the image reliability. For instance,  $M$  may contain an authenticity code (e.g. about 1000 bits by combining the French National Identifier with the Unique Identifier of DICOM the standard for medical images [9]), and an integrity proof which can be a secret pseudorandom binary sequence [10]. The integrity of the encrypted or decrypted image can thus be checked based on verifying the presence of this sequence within the image. Moreover, one can better enhance the robustness of the embedded message in the encrypted domain by working with  $p>2$ ; allowing repeating the message at least 3 times.

**Distortion:** As our algorithm introduces in average the same image distortion in each pixel block, we decided to use the Peak Signal to Noise Ratio (PSNR) to measure the distortion between the image  $I$  and its watermarked and deciphered version  $I_w$ . The lower bound of PSNR can be theoretically determined according to  $\Delta$ . Let us assume that the pixels of the image (i.e.  $I$ ) are uniformly distributed over the cells of QIM codebooks (see Fig.1). This means that the probability that one subset pixel  $I_i^j$  belongs to the cell that encodes '0' (resp. '1') is 0.5. Since  $W$  is a binary sequence uniformly distributed, the probability that the pixel  $I_i^j$  belongs to the cell that encodes  $w_i$  is 0.5. As can be seen in Fig 1, the maximum distortions one may introduce to embed  $w_i$  into  $I_i^j$  by moving it to the center of the nearest cell that encodes  $w_i$  are  $\Delta/4$  and  $\Delta/2$  in the cases where  $I_i^j$  "naturally" encodes  $w_i$  or not, respectively. Knowing that, we can consider that the maximum distortion induced by the insertion process of  $w_i$  into  $I_i^j$  is thus  $d_{ms} = \frac{1}{2}(\frac{\Delta}{4} + \frac{\Delta}{2}) = \frac{3}{8}\Delta$ . After the insertion of  $M$  into the encrypted image, only subsets that encode  $b_i = '1'$  are modified (see eq.18). Due to fact that the distortion induced by the insertion of  $b_i = '1'$  into  $I_i^j$  is  $\Delta/2$  and that the probability that  $b_i = '1'$  is 0.5, the distortion induced by the insertion of  $b_i$  into  $I_{ie}^j$  is then  $d_{me} = \frac{\Delta}{4}$ . Therefore, the maximum distortion induced per pixel by our data hiding scheme is  $d_m = d_{ms} + d_{me} = \frac{5}{8}\Delta$ . Consequently, the PSNR lower-bound can be refined as

$$PSNR_{Pait}(I, I_{wd}) \geq 20 \log_{10} \left( \frac{408}{\Delta} \right) \quad (21)$$

We give in Fig.3 the variation of this limit for different values of  $\Delta$ . In practice, achieved PSNR values are much greater (see Fig.3). They are about 51.15 dB, 44.2dB and 37.8dB for  $\Delta = \{2, 4, 8\}$ , respectively. This can be explained by the fact that, in practice, the pixels of the image source are not uniformly distributed over the cells of QIM codebooks. With our system, an information loss thus occurs. But, this loss remains small in particular when  $\Delta < 5$ . In healthcare, Chen *et al.* reported in [11] that some loss can be tolerated until the PSNR stays in the range of 40 and 50dB.

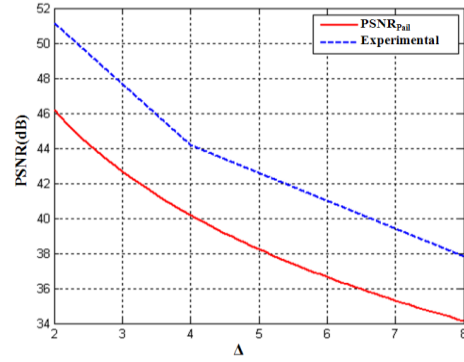


Figure 3. Lower theoretical PSNR bound ( $PSNR_{Pait}$ ) and obtained experimental PSNR values for different values of  $\Delta$ .

## V. CONCLUSION

In this work, we have proposed a new data hiding scheme of encrypted images that allows accessing a message in both the encrypted and spatial domains. This message can be used for verifying the image reliability even though it is encrypted. Its originality stands on the use of a pre-watermark which makes the insertion /extraction processes independent of the encryption/decryption processes, and vice versa. We have also provided an implementation of our scheme based on QIM modulation and Paillier cryptosystem. It provides an important capacity rate while minimizing image distortion. Future works will focus on making this implementation more robust to attacks like lossy image compression (ex. JPEG) and on enhancing the quality of the watermarked images.

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