

## Appendix E. Mechanical PVDR Form



# ASC2018 Mechanical PVDR Form

School/Team: University of Waterloo / Midnight Sun Solar Car Team Entry # 24

## Mechanical PVDR/Table of Contents

1.	History of team and vehicle (one paragraph)	page <u>3</u>
2.	<b>Type of vehicle:</b> Single-Occupant ( <u>  </u> ), Multi-Occupant ( <u>x</u> ) check one	
3.	Vehicle weight (estimate) ( <u>550</u> ); Units ( <u>x</u> ) kg ( <u>  </u> ) lbs,	
4.	Vehicle description shall be presented by profile and top view drawings showing the placement of major components such as driver, battery, ballast box, crush zone, seat belts mounting points, etc, along with overall dimensions including wheel base and tread	page <u>3</u>
5.	<b>Frame/chassis and roll cage type:</b> tubular frame ( <u>x</u> ), composite ( <u>  </u> ), check one. Drawing shall show the driver positioned in the frame/chassis, compliance with Regs. 10.3,10.3.B,10.3.C, and description of method of construction	page <u>3</u>
6.	<b>Roll cage:</b> Profile and frontal drawings shall show compliance with Regs 10.3.F and 10.3.G	page <u>6</u>
7.	<b>Seat Belts:</b> 5 point ( <u>x</u> ), 6 point ( <u>  </u> ), check one Drawing shall indicate location of mounting points and compliance with Reg. 10.3.E	page <u>6</u>
8.	<b>Braking system:</b> Front wheel only ( <u>x</u> ), Front-rear ( <u>  </u> ), check one. Schematic and description of primary braking system shall show compliance with Regs.10.5 and 10.6	page <u>6</u>
9.	<b>Steering system type:</b> rack and pinion ( <u>x</u> ), other ( <u>  </u> ), check one. Description shall include component selection and specs	page <u>11</u>
10.	<b>Front suspension:</b> type: a-arm ( <u>x</u> ), other ( <u>  </u> ), check one Description shall include drawing/photos, component selection and engineering analysis demonstrating proper selection and sizing of rod ends with shear loads	page <u>13</u>
11.	<b>Rear Suspension:</b> type: a-arm ( <u>  </u> ), swing arm ( <u>x</u> ), other, check one. Description shall include drawing/photos with component selection and specs, and engineering analysis demonstrating proper selection and sizing of rod ends with shear loads	page <u>13</u>
12.	Description of method of analysis to be used to prove structural integrity For loading conditions as per Appendix D, Section D.1	page <u>13</u>

Mechanical contact: Name: Devon Copeland  
 Email address: devon.copeland@uwmidsun.com  
 Phone: 226-792-7383

Project Manager: Name: Tak Alguire  
 Email address: tak.alguire@uwmidsun.com



Midnight Sun Solar Car Team  
University of Waterloo

MSXII  
**Preliminary Vehicle Design Report**  
Mechanical

Prepared by:  
Minghao Ji  
[minghao.ji@uwmidsun.com](mailto:minghao.ji@uwmidsun.com)  
October 15, 2017

## Contents

1	History	3
2	Contacts	3
3	Overview	3
4	Chassis	3
4.1	Design . . . . .	3
4.2	Manufacturing . . . . .	6
4.3	Roll cage . . . . .	6
5	Seat belts	6
6	Braking system	6
6.1	Primary brakes . . . . .	6
6.2	Parking brake . . . . .	11
7	Steering system	11
8	Suspension	13
8.1	Front suspension . . . . .	13
8.2	Rear suspension . . . . .	13
9	Finite element analysis	13
9.1	Front suspension . . . . .	14
9.1.1	Clevises . . . . .	14
9.1.2	Upper control arms . . . . .	14
9.1.3	Lower control arms . . . . .	14
9.1.4	Uprights . . . . .	14
9.1.5	Spindles . . . . .	14
9.1.6	Upper bearing plates . . . . .	15
9.1.7	Coilover control arm tabs . . . . .	15
9.1.8	Coilover mounting plates . . . . .	15
9.2	Rear suspension . . . . .	15
9.2.1	Clevises . . . . .	15
9.2.2	Coilover tabs . . . . .	15
9.3	Steering . . . . .	15
9.3.1	Steering arms . . . . .	15
9.3.2	Tie rods . . . . .	15
9.4	Results . . . . .	15
A	Loading conditions	17
A.1	Braking . . . . .	17
A.2	Acceleration . . . . .	17
A.3	Cornering . . . . .	18
A.4	Bump . . . . .	19
A.5	Superposition . . . . .	19
A.6	Summary . . . . .	20
B	FEA images for chassis	22
C	FEA images for suspension and steering	27

## List of Figures

1	Top view showing major dimensions and system positions . . . . .	4
2	Side view showing major dimensions and system positions . . . . .	5
3	Chassis, front view . . . . .	6
4	Chassis, top view . . . . .	7
5	Chassis, side view . . . . .	7
6	Welding jig on rotating mount . . . . .	8
7	Chassis with roll cage elements highlighted . . . . .	8
8	Chassis mounting points for seat belts . . . . .	9
9	Single seat belt tab . . . . .	9
10	Side view of seat belt geometry . . . . .	10
11	Top view of seat belt geometry . . . . .	10
12	Schematic of primary braking system . . . . .	11
13	View of dual-primary calipers and parking caliper on front suspension upright . . . . .	12
14	View of steering assembly . . . . .	12
15	View of front suspension assembly (parking brake caliper obstructed by hub) . . . . .	13
16	View of rear suspension assembly . . . . .	14
17	Free body diagram of vehicle braking . . . . .	18
18	Free body diagram of vehicle cornering . . . . .	19
19	Suspension coordinate system . . . . .	21
20	Front bumper collision . . . . .	22
21	Front bumper 30 degree collision . . . . .	22
22	Front bumper 60 degree collision . . . . .	22
23	Side bumper collision . . . . .	23
24	Rear bumper collision . . . . .	23
25	Hood 60 degree collision . . . . .	23
26	Hood 30 degree collision . . . . .	23
27	Side 60 degree collision . . . . .	24
28	Side 30 degree collision . . . . .	24
29	Roof top collision . . . . .	24
30	Vehicle rest front subframe loading . . . . .	24
31	Vehicle rest front subframe stress . . . . .	25
32	Vehicle rest rear subframe stress . . . . .	25
33	Torsion test, deformation . . . . .	25
34	Torsion test, stress . . . . .	26
35	Coilover clevis . . . . .	27
36	Upper control arm clevis . . . . .	27
37	Lower control arm clevis . . . . .	27
38	Upper control arm . . . . .	28
39	Lower control arm . . . . .	28
40	Upright . . . . .	28
41	Spindle . . . . .	29
42	Upper bearing plate . . . . .	29
43	Coilover control arm tab . . . . .	29
44	Coilover mounting plate . . . . .	30
45	Rear suspension clevis . . . . .	30
46	Rear suspension coilover tab . . . . .	31
47	Steering arm . . . . .	31
48	Tie rod . . . . .	32

## List of Tables

1	Table of major vehicle dimensions . . . . .	3
2	Summary of FEA results for suspension and steering components . . . . .	16
3	Important vehicle parameters . . . . .	17
4	Summary of worst case loading conditions . . . . .	20

## 1 History

Midnight Sun was founded in 1988 at the University of Waterloo. The team has produced 11 solar-powered vehicles since its inception, numbered MSI through MSXI. MSX and its predecessors have been traditional Challenger class cars. MSXI was the team's first attempt at a Cruiser class vehicle, which ultimately suffered from design issues relating to its monocoque design. With MSXII, the team has regrouped and designed a new Cruiser vehicle from the ground up, focussing strongly on reliability, safety, and manufacturability.

## 2 Contacts

Questions regarding the mechanical design and implementation of MSXII should be directed to one of the following contacts:

Name	Title	Phone	Email
Tak Alguire	Project Manager	519-574-4610	tak.alguire@uwmidsun.com
Minghao Ji	Engineering Manager	519-500-1292	minghao.ji@uwmidsun.com
Devon Copeland	Mechanical Lead	226-792-7383	devon.copeland@uwmidsun.com

## 3 Overview

MSXII is a dual-occupant Cruiser class vehicle. Its structural design uses a steel alloy tube chassis with non-structural fibreglass body panels. The majority of the vehicle's powertrain systems are located behind the occupant cell, including the battery pack, power junction box, motor controllers, and EV charger. The vehicle is rear-wheel driven by two hub-mounted DC motors. The locations of these components are marked in Figure 1 and Figure 2. Major vehicle dimensions are summarized in Table 1.

## 4 Chassis

### 4.1 Design

The chassis is a tube structure enclosing the occupant cell with small front and rear subframes to support suspension hardpoints. Smaller non-structural tube members will extend from the main frame to provide support to body panels as necessary. The majority of tubes are round, with square tubes being used only for elements intended to mount suspension and powertrain components (battery pack, motor controllers). Chassis elements

Wheelbase	2.60 m
Track	1.60 m
Max length	4.68 m
Max width	2.02 m
Max height	1.23 m

Table 1: Table of major vehicle dimensions

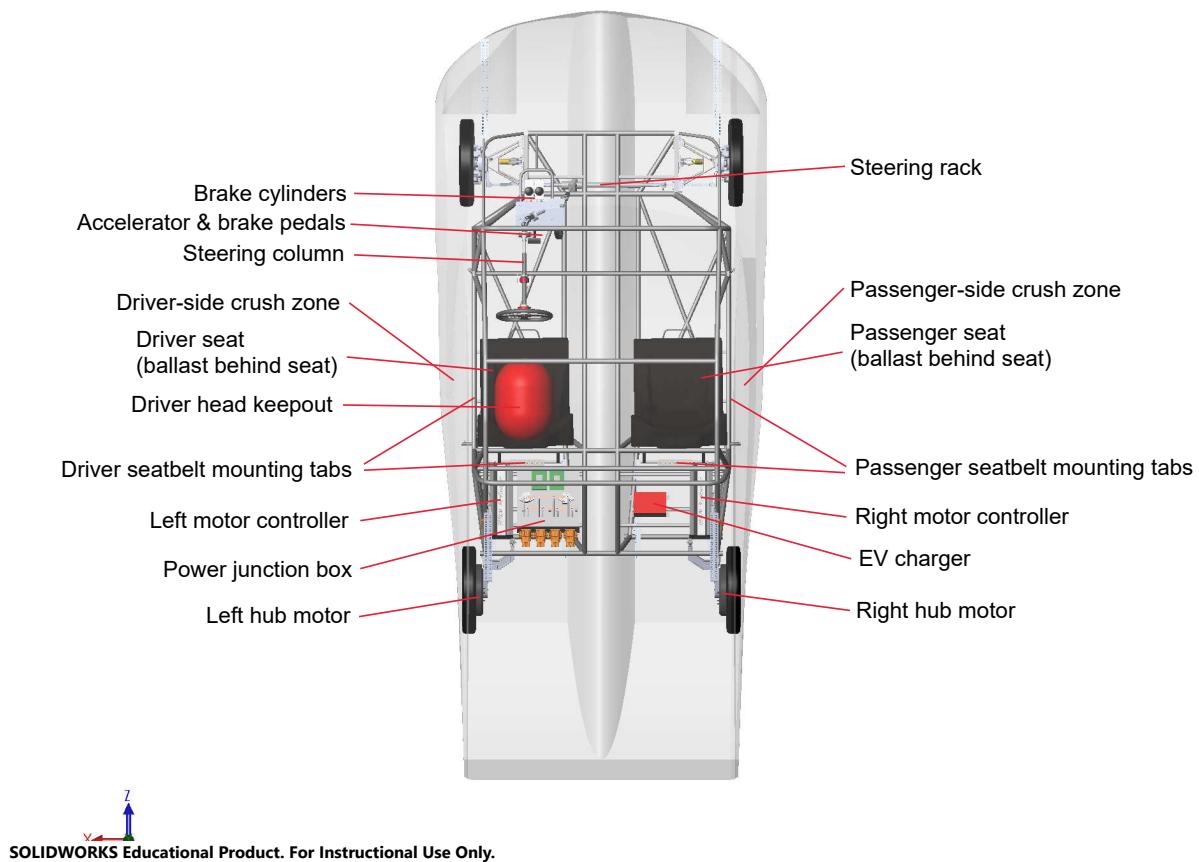


Figure 1: Top view showing major dimensions and system positions

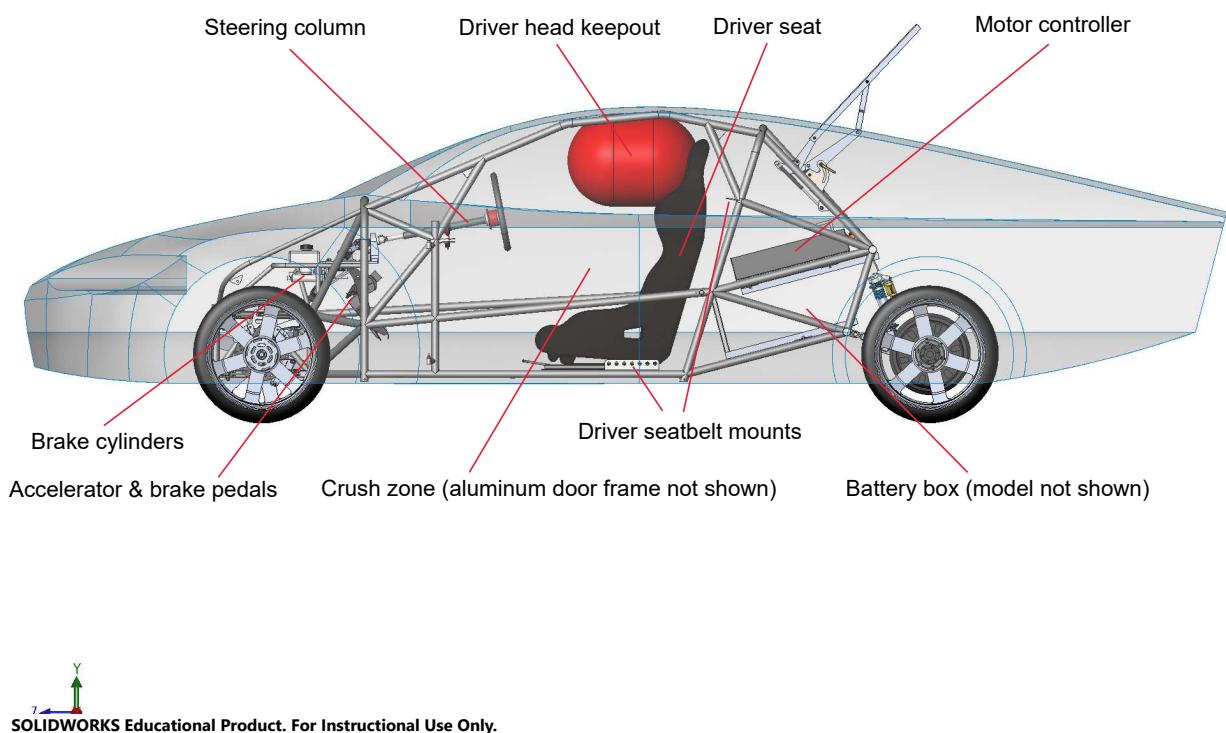


Figure 2: Side view showing major dimensions and system positions

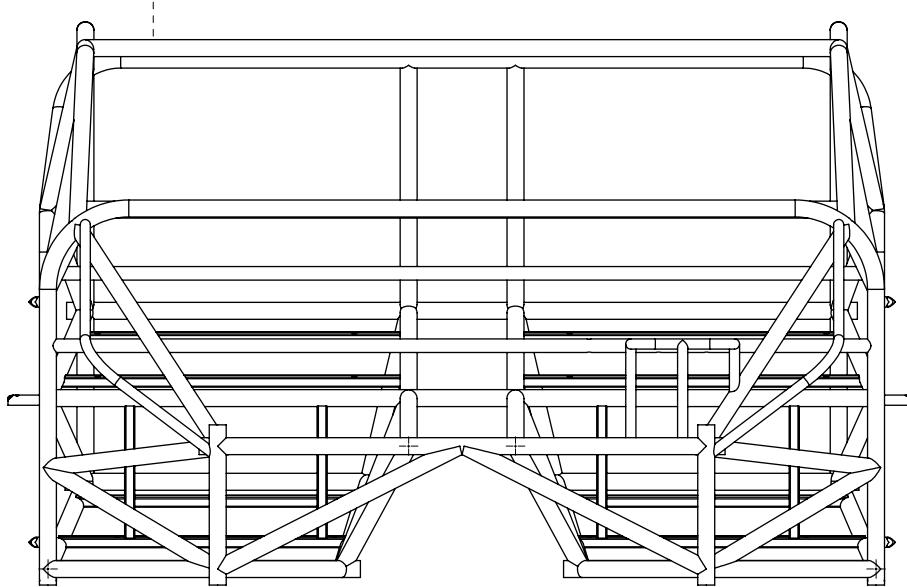


Figure 3: Chassis, front view

use SAE 4130N chromoly tubes with diameters or side lengths ranging from 0.750" to 1.250", and wall thicknesses ranging from 0.035" to 0.065". Isometric drawings of the chassis are shown in Figures 3, 4, and 5.

## 4.2 Manufacturing

Bending, cutting, and profiling of tubes was done by an external supplier. Welding of the chassis was done by a professional welder using GTAW, with support from team members for jigging and assembly. A complete welding jig was designed in CAD and manufactured using 80/20 aluminum extrusion tubing, shown in Figure 6. Custom tube clamps were machined by the team to slot into jig members and fully support all chassis elements through multiple stages of assembly and welding.

## 4.3 Roll cage

The roll cage is integrated into the design of the chassis members enclosing the occupant cell. For the purposes of ASC regulations, the roll cage can be considered to include the A and B pillar hoops and elements connecting these two hoops lengthwise through the car. For clarity, these elements have been highlighted in Figure 7.

## 5 Seat belts

MSXII is equipped with 5-point seat belts for both occupants. Seat belt hardpoints are mounted to metal tabs welded to chassis members, shown in Figure 8. Figure 9 shows one of these tabs. Figures 10 and 11 demonstrate compliance with ASC regulations 10.3.E.

## 6 Braking system

### 6.1 Primary brakes

The primary braking system is designed with dual redundant front braking, consisting of two identical systems with separate master cylinders, hydraulic lines, and calipers to each of the left and right wheels. The master cylinders are operated in unison via a single mechanical brake pedal. A schematic of the primary system is shown in Figure 12.

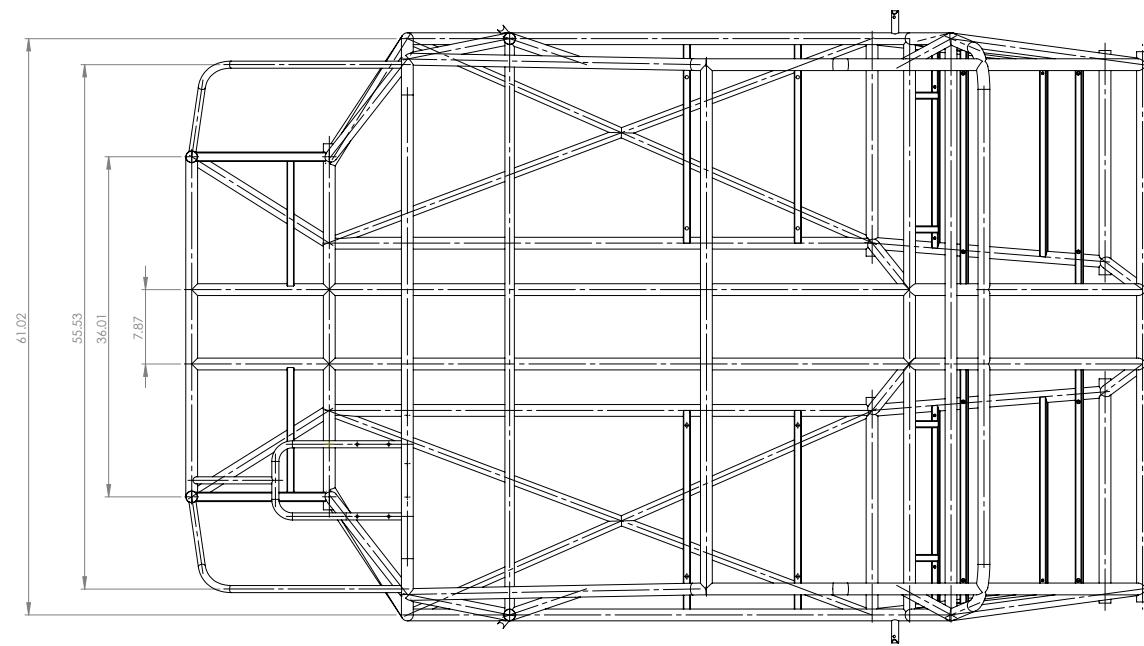


Figure 4: Chassis, top view

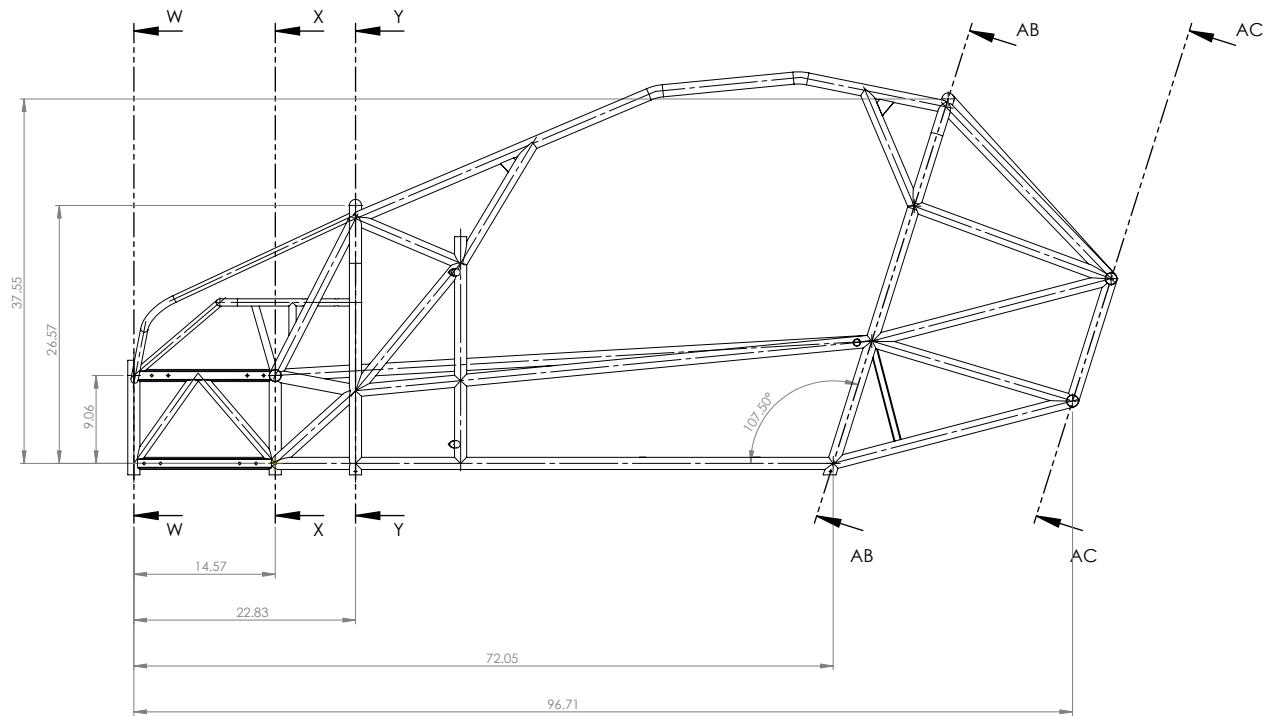
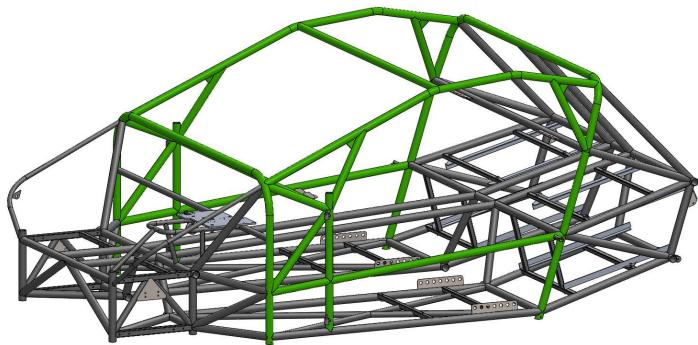


Figure 5: Chassis, side view

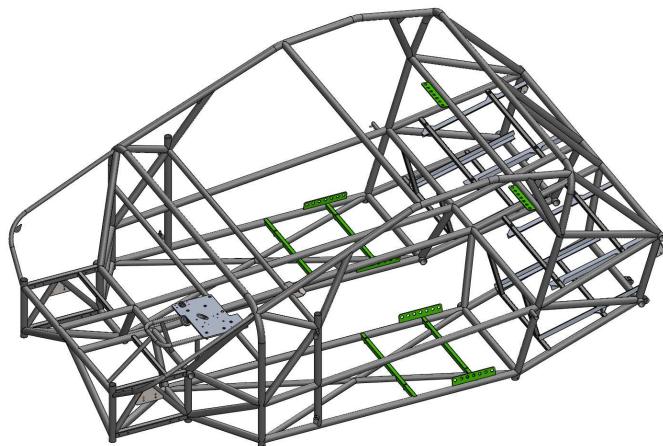


Figure 6: Welding jig on rotating mount



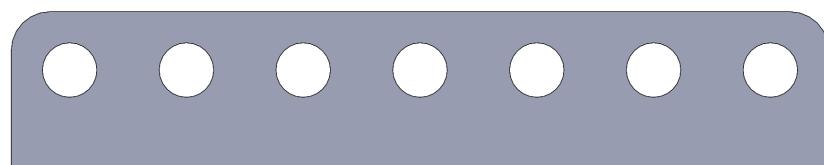
SOLIDWORKS Educational Product. For Instructional Use Only.

Figure 7: Chassis with roll cage elements highlighted



SOLIDWORKS Educational Product. For Instructional Use Only.

Figure 8: Chassis mounting points for seat belts



SOLIDWORKS Educational Product. For Instructional Use Only.

Figure 9: Single seat belt tab

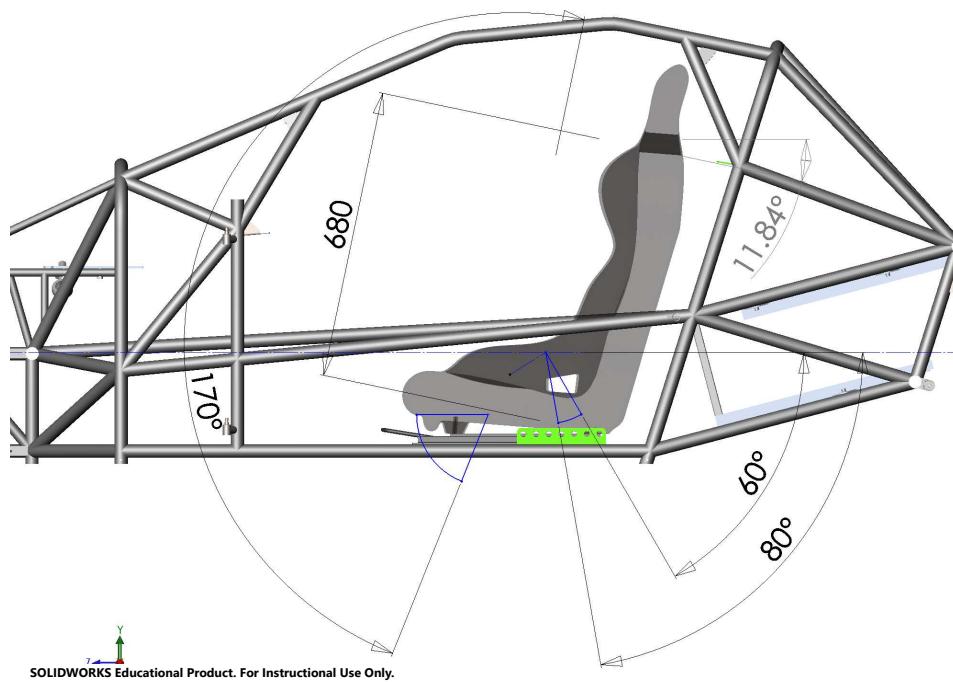


Figure 10: Side view of seat belt geometry

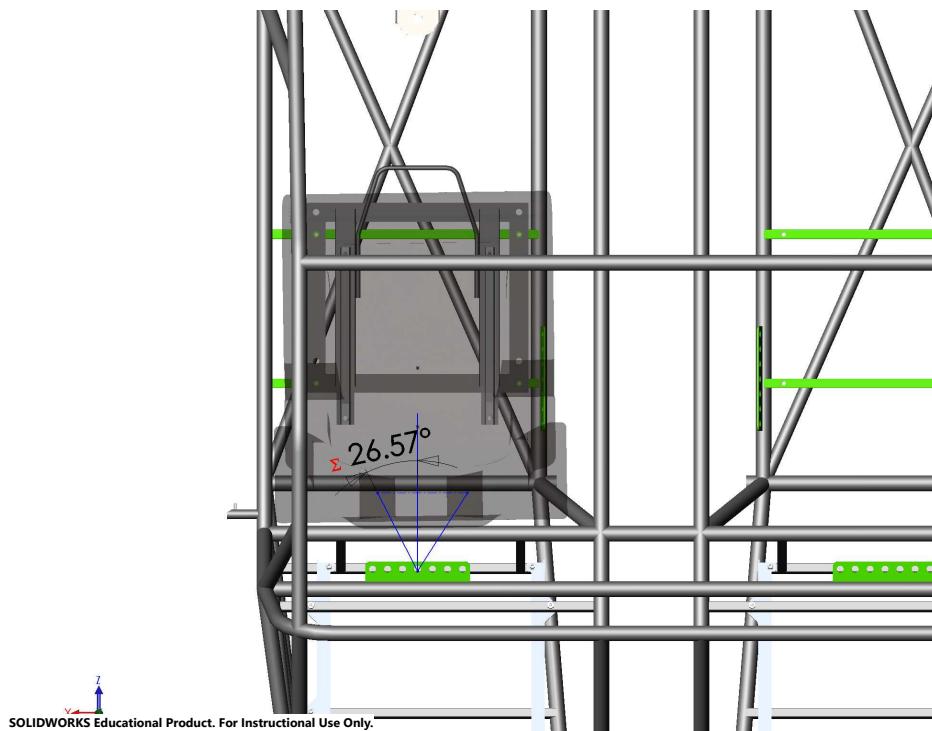


Figure 11: Top view of seat belt geometry

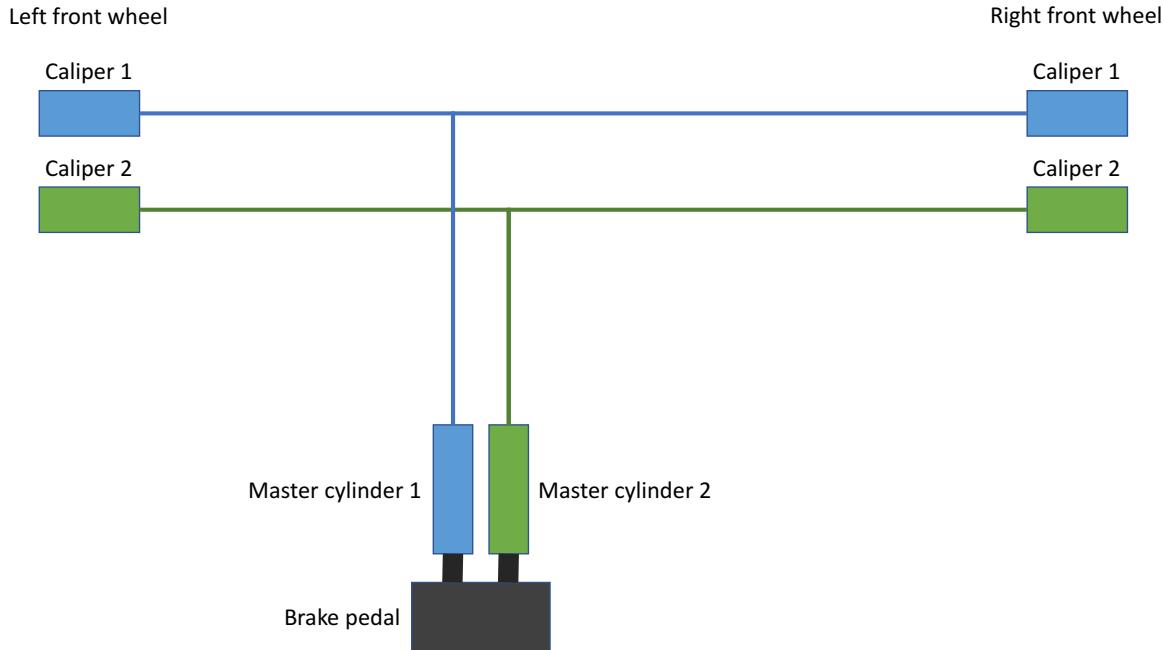


Figure 12: Schematic of primary braking system

Front brake calipers are Willwood parts 120-8374 (left) and 120-8373 (right). Willwood's website indicates the caliper pads have  $2 \text{ in}^2$  ( $12.9 \text{ cm}^2$ ) contact area and 0.30" (7.6 mm) depth including the backing plate.

The master cylinders are Willwood part 206-3374. They have a 3/8"-24 outlet size which will need to be connected via a suitable brake line to the M10 x 1.25 inlets of the calipers. Brake lines will be DOT-approved hose assemblies sized for 3/8"-24 on one end and M10 on the other end via a banjo joint. The brake pedal is Willwood part 340-15079 and is mounted in the standard configuration to the left of the accelerator pedal.

Brake rotors will be custom-machined to the disk thickness and diameter supported by the Willwood calipers. All mounting geometry on the suspension upright for primary calipers are designed to position the primary calipers in the optimal positions to meet braking specifications.

## 6.2 Parking brake

The parking brake will be implemented by a cable-actuated caliper mounted at one of the front wheels. The caliper is the Tolomatic ME10LA, part number 0732-0003. It will share the same brake disk as the primary braking system but is otherwise mechanically independent. Due to unresolvable dimensioning differences between the Tolomatic and Willwood calipers, the parking brake caliper cannot be mounted perfectly as per the manufacturer's recommendations and will have only 80% overlap with the brake disk. However, this is expected to provide more than sufficient countertorque to keep the vehicle stationary as per ASC regulations 10.6.

Figure 13 shows a front suspension upright with all three calipers mounted (two primary and one parking).

## 7 Steering system

The steering system uses a rear-steering, left-hand-drive rack and pinion from Helix (part number 188754). The system uses a collapsible steering column from Sweet Mfg., part number 405-10310. The linkage uses dual U-joints to circumvent interfering brake system components and is shown in Figure 14.

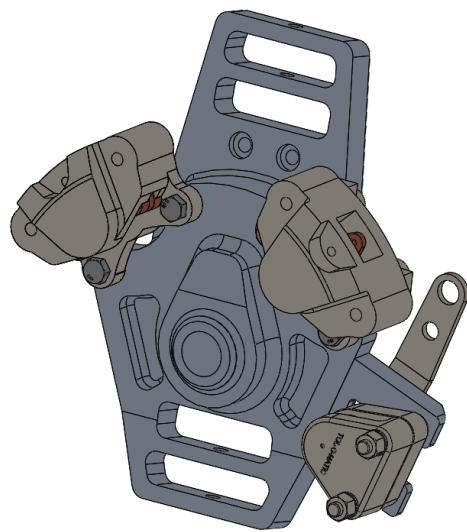


Figure 13: View of dual-primary calipers and parking caliper on front suspension upright



SOLIDWORKS Educational Product. For Instructional Use Only.

Figure 14: View of steering assembly

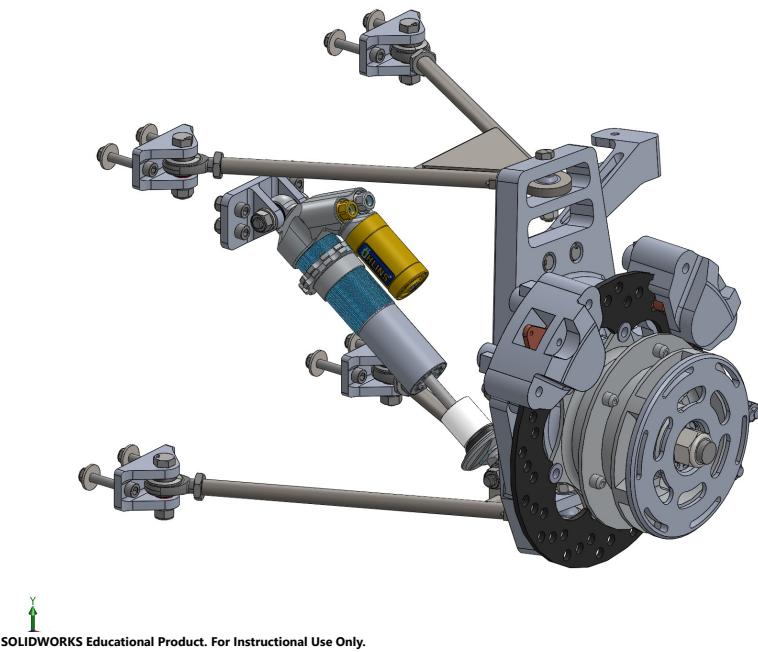


Figure 15: View of front suspension assembly (parking brake caliper obstructed by hub)

## 8 Suspension

### 8.1 Front suspension

The front suspension uses dual A-arms with an outboard dampener and coilover spring. The upper and lower control arms are custom-built from 4130 chromoly tubes. The dampener and coilover are a single integrated assembly supplied by Öhlins, sold as the TTX25, which is marketed for Formula SAE vehicles. Figure 15 shows the front suspension assembly.

The front suspension lower control arm bears the majority of the shear stress from road forces. Based on hand calculations for a cantilever beam, the worst-case von Mises stress is 183 MPa. This dictates the sizing of the rod end.

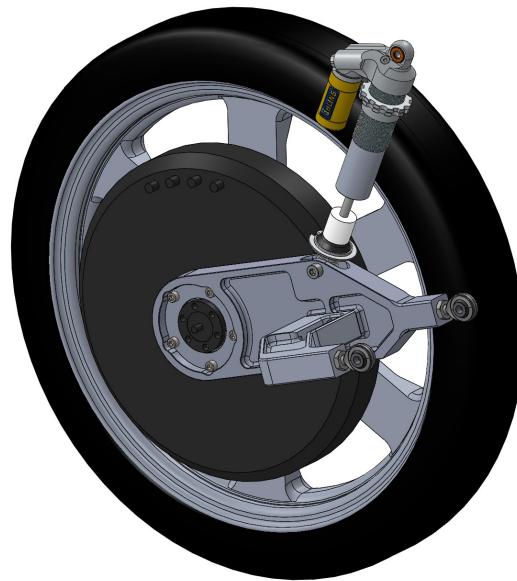
### 8.2 Rear suspension

The rear suspension uses independent trailing arms mounted outwards from the rear of the chassis. The trailing arm itself is custom-machined and mounts the same Öhlins TTX25 shock absorber as the front suspension. Figure 16 shows the rear suspension assembly.

## 9 Finite element analysis

Finite element analysis was performed using ANSYS on the chassis and all suspension and steering components (downstream from the rack and pinion). FEA of the chassis followed the specifications provided by the ASC regulations. A general methodology was to fix a solid beam or wall in space, and apply a 5G acceleration to the chassis against it. Images for FEA simulations of each requested scenario are shown in Appendix B.

Worst-case loading forces on each wheel were used to derive appropriate constraints and forces for FEA simulation of the suspension and steering system. A complete derivation and summary of loading forces on each wheel is given in Appendix A. Images of all FEA simulations for suspension and steering are available in Appendix C.



SOLIDWORKS Educational Product. For Instructional Use Only.

Figure 16: View of rear suspension assembly

## 9.1 Front suspension

### 9.1.1 Clevises

Hand calculations were used to resolve the forces from the road as loading onto the clevises. The back face of the clevis was constrained with compression only support. Cylindrical supports were used for the bolt holes and fastener pretension was added. Frictional contacts were added between the fasteners and the clevis.

### 9.1.2 Upper control arms

Contacts were modeled between the control arm tubes and the bearing plate. Forces were applied to the bearing plate based on hand calculations.

### 9.1.3 Lower control arms

Contacts were modeled between the control arm tubes and the mounting tabs on the coilover clevis. Forces were applied to the profile that the bearing sits in, based off of hand calculations.

### 9.1.4 Uprights

A dummy wheel was modeled to which forces were applied. The dummy wheel contacted the spindle with a frictional contact which then applied a load to the upright. The brake forces were applied to the caliper mounting holes, assuming only one caliper was providing all braking force.

### 9.1.5 Spindles

A dummy wheel was modeled to which forces were applied. The dummy wheel contacted the spindle with a frictional contact which then applied a load to the upright.

### 9.1.6 Upper bearing plates

Contacts were modeled between the control arm tubes and the bearing plate. Forces were applied to the bearing plate based on hand calculations.

### 9.1.7 Coilover control arm tabs

The maximum force on the front wheel was resolved as a compressive load in the coilover and applied to this tab.

### 9.1.8 Coilover mounting plates

Hand calculations were used to resolve the forces from the road as loading onto the clevises. For this simulation a frictional contact was added between the clevis and the mounting plate. Dummy chassis tubes were modeled behind the mounting plate and welded edges were fixed.

## 9.2 Rear suspension

### 9.2.1 Clevises

The worst case of four loading scenarios was taken (2 clevis positions, each with either the inside or outside wheel when rounding a corner). It was assumed that all lateral force was applied to a single clevis because otherwise this is a statically indeterminate problem on paper.

### 9.2.2 Coilover tabs

The maximum normal force and acceleration force on the rear wheel was resolved as a compressive load in the coilover and applied to this tab.

## 9.3 Steering

### 9.3.1 Steering arms

A compression support was added on the face datuming off of the upright. The maximum lateral force on the tire during 1G cornering was resolved as a torque on the upright. This torque was applied by a bearing load acting at the end of the steering arm.

### 9.3.2 Tie rods

A similar analysis to that for the steering arm was used. Force was applied to one end of the tie rod while the other remained fixed. Both sides of the tie rod were tested with an applied force and fixed support.

## 9.4 Results

All FEA results for suspension and steering components are summarized in Table 2. Note that FEA for the rear suspension trailing arm and brace. Simulations of the rear trailing arm are experiencing convergence and stress concentration issues.

Part Number	Part Name	Material	Max Stress (MPa)	Safety Factor
MS00015	Coilover Clevis	Aluminum, 7075	147	3.4
MS00029	Upper Control Arm Clevis	Aluminum, 7075	191	2.6
MS00102	Lower Control Arm Clevis	Aluminum, 7075	198	2.5
MS00017	Upper Control Arm	Chromoly Steel, 4130	199	2.3
MS00018	Lower Control Arm	Chromoly Steel, 4130	226	2.0
MS00019	Upright	Aluminum, 7075	210	2.4
MS00020	Spindle	Chromoly Steel, 4140	177	2.3
MS00030	Upper Bearing Plate	Chromoly Steel, 4130	141	3.3
MS00036	Coilover Control Arm Tab	Chromoly Steel, 4130	159	2.9
MS00038	Coilover Mounting Plate	Chromoly Steel, 4130	147	3.1
MS00086	Rear Suspension Clevis Mount	Chromoly Steel, 4130	231	2.0
MS00047	Rear Suspension Coilover Tab	Chromoly Steel, 4130	147	3.1
MS00065	Trailing Arm	Aluminum, 7075	X	X
MS00074	Steering Arm	Aluminum, 6061-T6	77	3.5
MS00101	Tie Rod	Aluminum, 6061-T6	41	6.6

Table 2: Summary of FEA results for suspension and steering components

Mass ( $M$ )	550	kg
Wheelbase	2.60	m
Track	1.60	m
Tire Diameter	0.53	m
Wheel Assembly Moment of Inertia ( $J_w$ )	0.25	$\text{kg m}^2$
Distance from Front Wheel to CoG ( $a$ )	1.32	m
Distance from Front Wheel to CoG ( $b$ )	1.28	m
Distance from Road to CoG ( $h$ )	0.52	m
Full Wheel Travel in Compression	45	mm
Front Coilover Angle from Vertical	40	°
Rear Coilover Angle from Vertical	30	°

Table 3: Important vehicle parameters

## A Loading conditions

FEA of the chassis, suspension, and steering system was done using ANSYS software. Loading conditions were derived from both ASC requirements and real-world scenarios. Assuming a smooth driving surface, the largest normal force acting on the front tire will occur while braking in a turn. Similarly, the largest normal force acting on the rear tire will occur while accelerating in a turn. To approximate these loading condition, the a superposition of two static half car models is used; one for cornering and one for hard braking.

Table 3 lists vehicle parameters that are relevant in determining the loading conditions in the suspension. The mass and moment of inertia were computed using CAD software.

### A.1 Braking

Figure 17 shows a free body diagram of a half car model undergoing braking. The required braking force can be approximated as follows:

$$F_{\text{braking}} = F_{\text{Nf}} + F_{\text{Nr}} = Mg = (550 \text{ kg})(9.81 \text{ m s}^{-2}) = 5.40 \text{ kN} \quad (1)$$

From Figure 17, summing the moments about the centre of gravity and the vertical forces results in the following equations:

$$aF_{\text{Nf}} = hF_{\text{braking}} + bF_{\text{Nr}} \quad (2)$$

$$F_{\text{Nf}} + F_{\text{Nr}} = Mg \quad (3)$$

Solving for the front normal force:

$$\begin{aligned} aF_{\text{Nf}} &= hF_{\text{braking}} + b(Mg - F_{\text{Nf}}) \\ F_{\text{Nf}} &= \frac{hF_{\text{braking}} + bMg}{a + b} = \frac{(0.52 \text{ m})(5.40 \text{ kN}) + (1.28 \text{ m})(550 \text{ kg})(9.81 \text{ m s}^{-2})}{(1.32 \text{ m}) + (1.28 \text{ m})} = 3.74 \text{ kN} \end{aligned} \quad (4)$$

Note that 3.74 kN is for both front wheels. Therefore there is approximately 1.87 kN of normal force on each front tire during hard braking.

### A.2 Acceleration

MSXII uses NGM SCM-150 motors which have a peak torque of 135 N m. From this torque value and a number of other vehicle parameters the vehicle's maximum acceleration can be calculated as follows:

$$a = \frac{F_w}{\frac{1}{2}M} \quad (5)$$

$$\alpha_w = \frac{T_m - F_w r}{J_w} \quad (6)$$

$$\alpha_w = ar \quad (7)$$

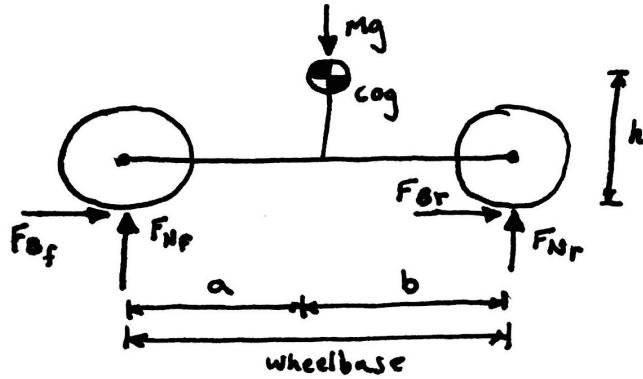


Figure 17: Free body diagram of vehicle braking

where  $a$  is the acceleration of the vehicle,  $F_w$  is the friction force acting on a single tire while accelerating,  $J_w$  is the moment of inertia of the wheel assembly,  $r$  is the radius of the tire,  $T_m$  is the torque from the motor and  $\alpha_w$  is the angular acceleration of the wheel.

Rearranging the above three equations, the acceleration of the vehicle can be expressed as a function of motor torque as follows:

$$a = \frac{T_m r}{\frac{1}{2} M r^2 + J_w}$$

$$a = \frac{(135 \text{ N m})(0.27 \text{ m})}{\frac{1}{2}(550 \text{ kg})(0.27 \text{ m}^2)^2 + 0.25 \text{ kg m}^2} = 1.80 \text{ m s}^{-2} \quad (8)$$

Solving for friction force on a single rear tire:

$$F_w = Ma = (550 \text{ kg})(1.80 \text{ m s}^{-2}) = 990 \text{ N} \quad (9)$$

The resulting normal force on the rear wheels can be calculated as follows:

$$bF_{Nr} = hF_w + a(Mg - F_{Nr})$$

$$F_{Nr} = \frac{hF_w + aMg}{a + b} = \frac{(0.52 \text{ m})(990 \text{ N}) + (1.32 \text{ m})(550 \text{ kg})(9.81 \text{ m s}^{-2})}{(1.32 \text{ m}) + (1.28 \text{ m})} = 2.94 \text{ kN} \quad (10)$$

Note that 2.94 kN is for both rear wheels. Therefore there is approximately 1.47 kN of normal force on each rear tire during maximum acceleration.

### A.3 Cornering

ASC regulations require simulations of a 1G turn, at minimum. This corresponds to the following lateral force:

$$F_{steer} = Mg = (550 \text{ kg})(9.81 \text{ m s}^{-2}) = 5.40 \text{ kN} \quad (11)$$

Additionally, the diameter of several highway exit ramps around the University of Waterloo were measured on satellite maps. The recommended speed limit on these exits is  $50 \text{ km h}^{-1}$ . Assuming a worst case scenario where the vehicle takes an exit with a 100 m diameter at  $80 \text{ km h}^{-1}$  ( $22.22 \text{ m s}^{-1}$ ), the required lateral force required to navigate this corner can be found as follows:

$$F_{steer} = \frac{Mv^2}{r} = \frac{(550 \text{ kg})(22.22 \text{ m s}^{-1})^2}{50 \text{ m}} = 5.43 \text{ kN} \quad (12)$$

This corresponds nearly identically to a 1G turn. Since the lateral force required in the second scenario is slightly higher, 5.34 kN will be used as the worst case cornering force.

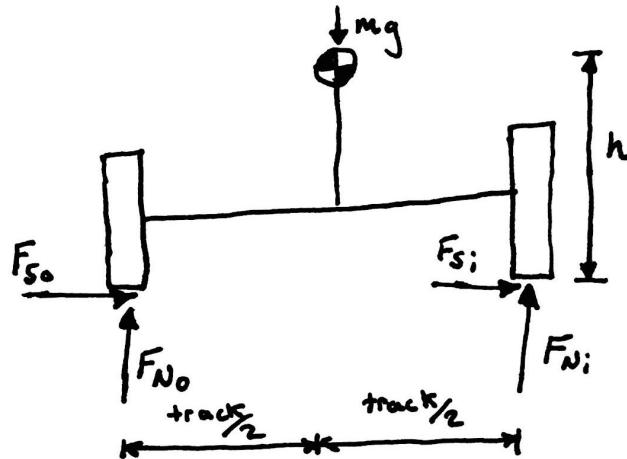


Figure 18: Free body diagram of vehicle cornering

Using the half car model shown in Figure 18, summing the moments about the centre of gravity and the vertical forces results in the following equations:

$$\frac{1}{2}L_{\text{track}}F_{\text{No}} = hF_{\text{steer}} + \frac{1}{2}L_{\text{track}}F_{\text{Ni}} \quad (13)$$

$$F_{\text{No}} + F_{\text{Ni}} = Mg \quad (14)$$

Solving for the outside wheel normal force:

$$\begin{aligned} \frac{1}{2}L_{\text{track}}F_{\text{No}} &= hF_{\text{steer}} + \frac{1}{2}L_{\text{track}}(Mg - F_{\text{Ni}}) \\ F_{\text{No}} &= \frac{hF_{\text{steer}} + \frac{1}{2}L_{\text{track}}Mg}{L_{\text{track}}} = \frac{(0.52 \text{ m})(5.43 \text{ kN}) + (0.80 \text{ m})(550 \text{ kg})(9.81 \text{ m s}^{-2})}{1.60 \text{ m}} = 4.46 \text{ kN} \end{aligned} \quad (15)$$

Solving for the inside wheel normal force:

$$F_{\text{Ni}} = Mg - F_{\text{No}} = (550 \text{ kg})(9.81 \text{ m s}^{-2}) - 4.46 \text{ kN} = 0.93 \text{ kN} \quad (16)$$

Note that the forces above are for both front and rear outside wheels. Assuming the force is evenly split between the front and rear, there is approximately 2.23 kN of normal force on each outside tire and 0.47 kN for each inside tire during maximum cornering.

#### A.4 Bump

As stipulated in the ASC 2018 regulations, the analysis for suspension and steering must include loading considerations for a 2G bump. We interpret this requirement as the body of the vehicle accelerating upwards at 2G, in which case the additional normal force subjected to a single tire can be expressed as follows:

$$F_{\text{N,bump}} = \frac{2Mg}{4} = \frac{2(9.81 \text{ m s}^{-2})(550 \text{ kg})}{4} = 2.70 \text{ kN} \quad (17)$$

#### A.5 Superposition

The braking, accelerating, and cornering conditions subject the wheels to normal forces that differ from those experienced when the car is at rest. The change in normal force for each loading condition can be expressed

as follows:

$$\Delta F_{Nf,\text{braking}} = F_{Nf,\text{braking}} - \frac{Mg}{4} = 1.87 \text{ kN} - 1.35 \text{ kN} = 0.52 \text{ kN} \quad (18)$$

$$\Delta F_{Nr,\text{accelerating}} = F_{Nr,\text{accelerating}} - \frac{Mg}{4} = 1.47 \text{ kN} - 1.35 \text{ kN} = 0.12 \text{ kN} \quad (19)$$

$$\Delta F_{No,\text{cornering}} = F_{No,\text{cornering}} - \frac{Mg}{4} = 2.23 \text{ kN} - 1.35 \text{ kN} = 0.88 \text{ kN} \quad (20)$$

$$\Delta F_{Ni,\text{cornering}} = F_{Ni,\text{cornering}} - \frac{Mg}{4} = 0.47 \text{ kN} - 1.35 \text{ kN} = -0.88 \text{ kN} \quad (21)$$

$$\Delta F_{N,\text{bump}} = F_{N,\text{bump}} - \frac{Mg}{4} = 2.70 \text{ kN} - 1.35 \text{ kN} = 1.35 \text{ kN} \quad (22)$$

To approximate the worst case loading condition, a superposition of the changes in normal force and the nominal normal force is applied. Note that the nominal force used is the same for each wheel, which assumes a centre of gravity approximately centred along the wheelbase.

$$F_{Nfi,\text{max}} = \Delta F_{Nf,\text{braking}} + \Delta F_{Ni,\text{cornering}} + 2F_{N,\text{nominal}} = 0.52 \text{ kN} - 0.88 \text{ kN} + 2.70 \text{ kN} = 2.34 \text{ kN} \quad (23)$$

$$F_{Nfo,\text{max}} = \Delta F_{Nr,\text{braking}} + \Delta F_{No,\text{cornering}} + 2F_{N,\text{nominal}} = 0.12 \text{ kN} - 0.88 \text{ kN} + 2.70 \text{ kN} = 4.10 \text{ kN} \quad (24)$$

$$F_{Nri,\text{max}} = \Delta F_{Nf,\text{braking}} + \Delta F_{Ni,\text{cornering}} + 2F_{N,\text{nominal}} = 0.52 \text{ kN} + 0.88 \text{ kN} + 2.70 \text{ kN} = 1.94 \text{ kN} \quad (25)$$

$$F_{Nro,\text{max}} = \Delta F_{Nr,\text{braking}} + \Delta F_{No,\text{cornering}} + 2F_{N,\text{nominal}} = 0.12 \text{ kN} + 0.88 \text{ kN} + 2.70 \text{ kN} = 3.70 \text{ kN} \quad (26)$$

## A.6 Summary

Table 4 summarizes the loading conditions used for static structural FEA simulations on the suspension and steering components. Note that the direction of the force corresponds with the global coordinate system of the MSXII and the vectors shown in Figure 19. The assemblies shown are for the driver's side of the vehicle

Table 4: Summary of worst case loading conditions

Worst Case Loading	$F_x$ (kN)	$F_y$ (kN)	$F_z$ (kN)
Braking & Cornering (Inside Front Wheel)	2.72	2.34	2.70
Braking & Cornering (Outside Front Wheel)	-2.72	4.10	2.70
Accelerating & Cornering (Inside Rear Wheel)	2.72	1.94	0.99
Accelerating & Cornering (Outside Rear Wheel)	-2.72	3.70	0.99

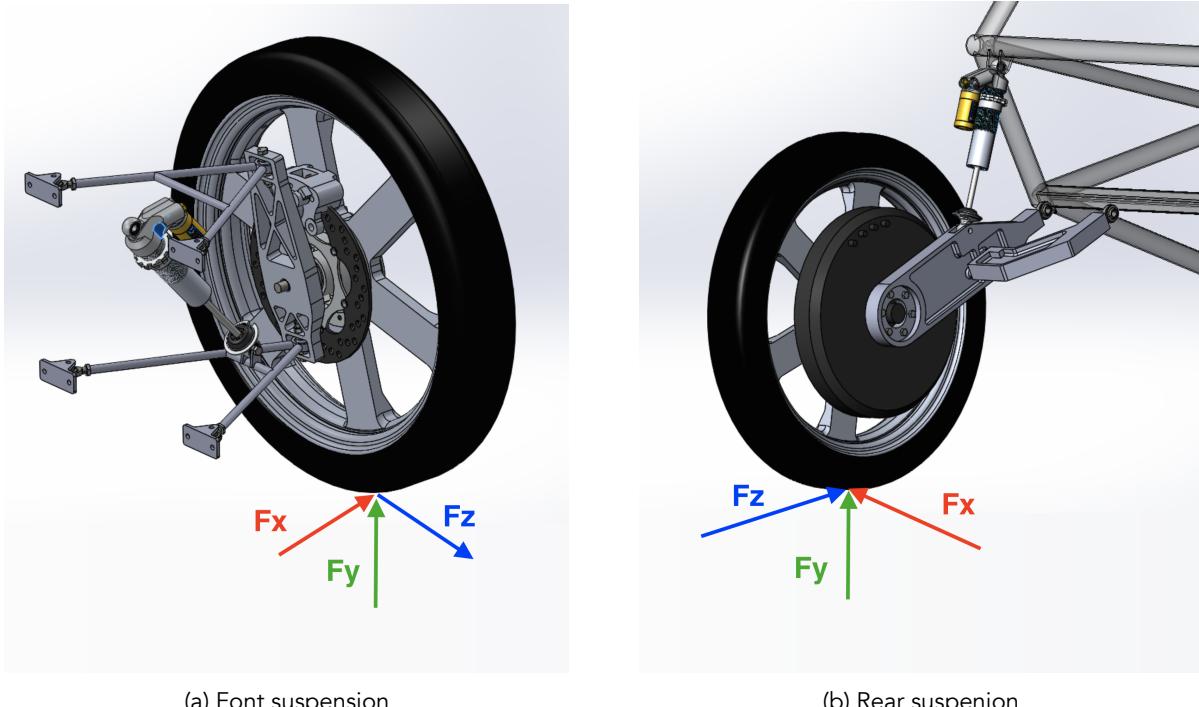


Figure 19: Suspension coordinate system

## B FEA images for chassis

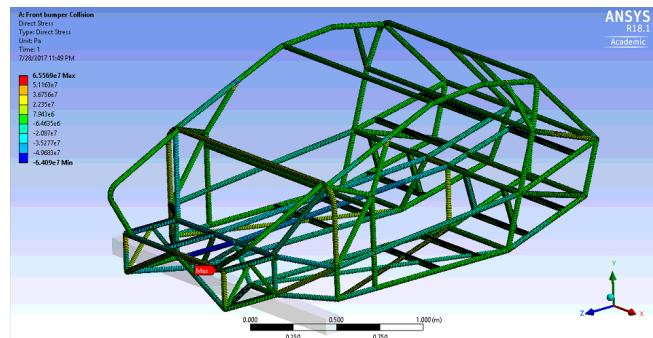


Figure 20: Front bumper collision

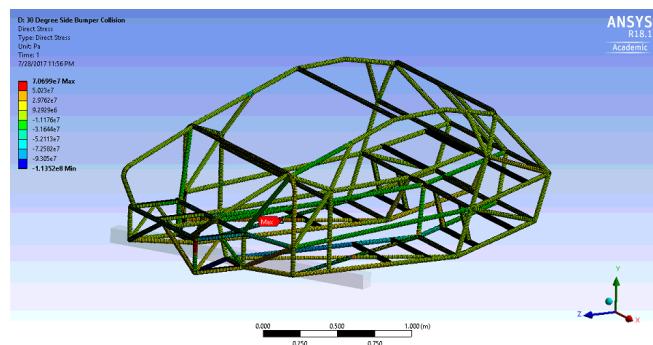


Figure 21: Front bumper 30 degree collision

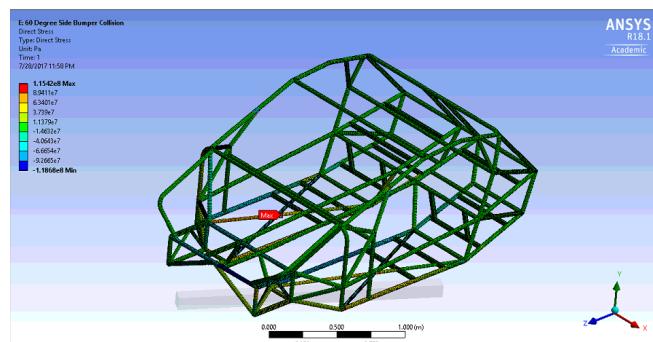


Figure 22: Front bumper 60 degree collision

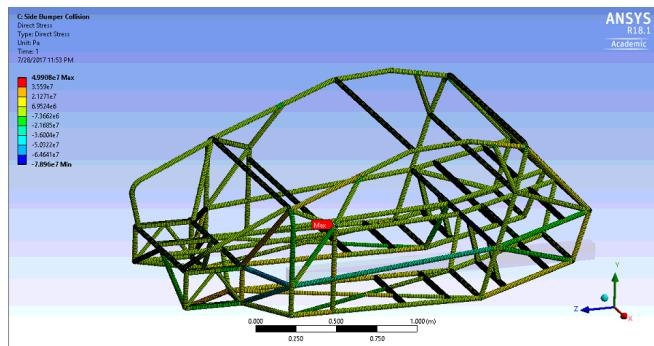


Figure 23: Side bumper collision

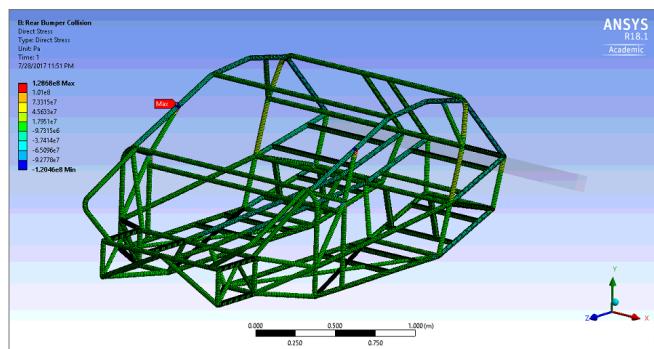


Figure 24: Rear bumper collision

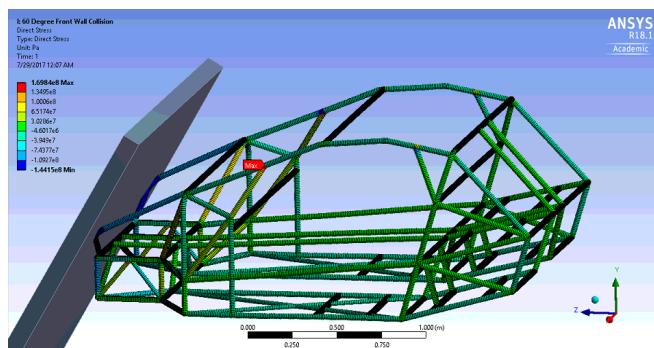


Figure 25: Hood 60 degree collision

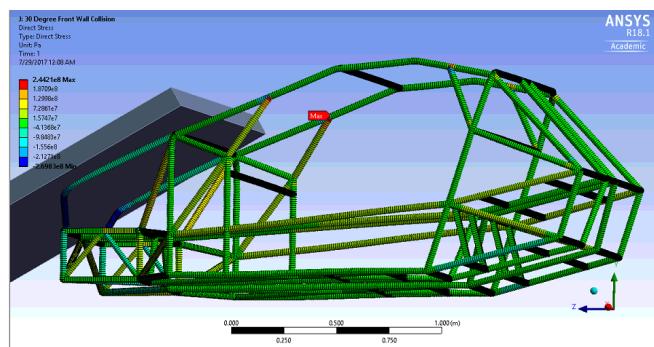


Figure 26: Hood 30 degree collision

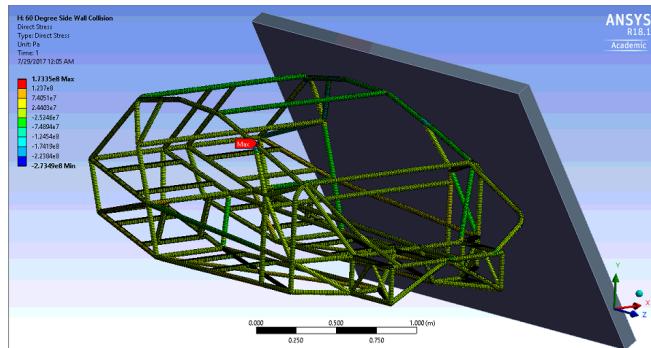


Figure 27: Side 60 degree collision

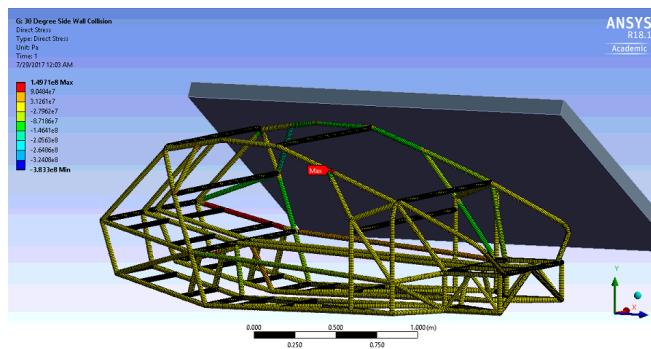


Figure 28: Side 30 degree collision

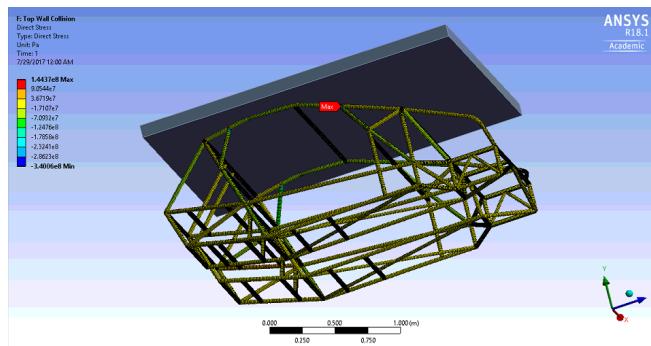


Figure 29: Roof top collision

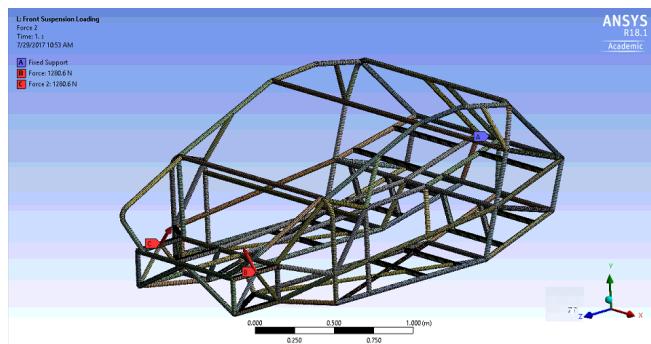


Figure 30: Vehicle rest front subframe loading

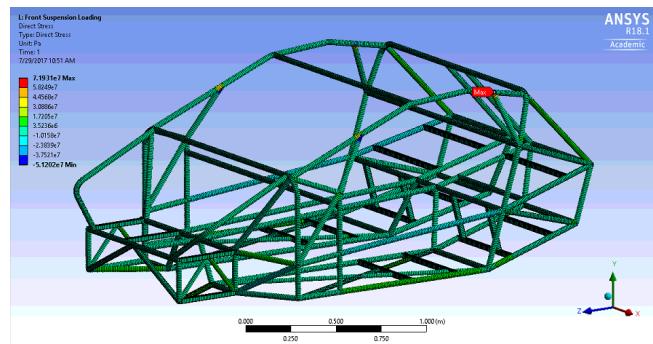


Figure 31: Vehicle rest front subframe stress

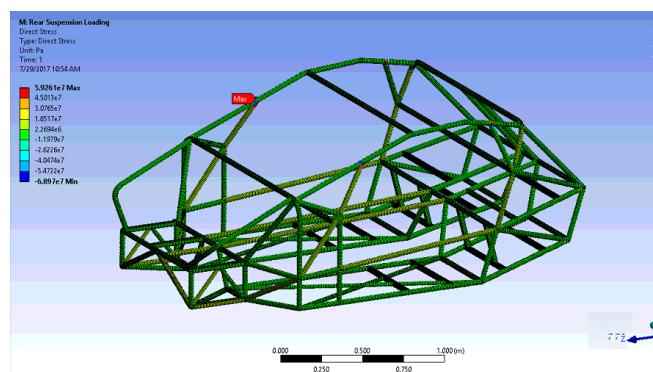


Figure 32: Vehicle rest rear subframe stress

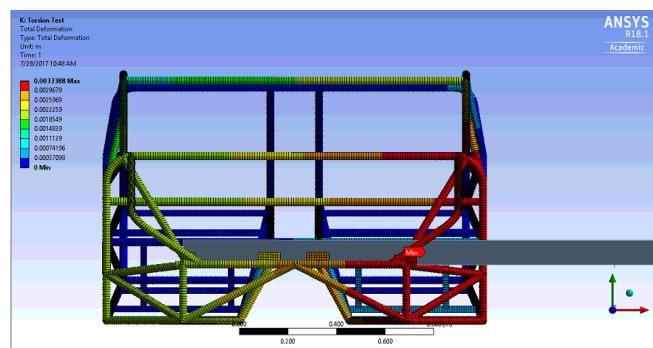


Figure 33: Torsion test, deformation

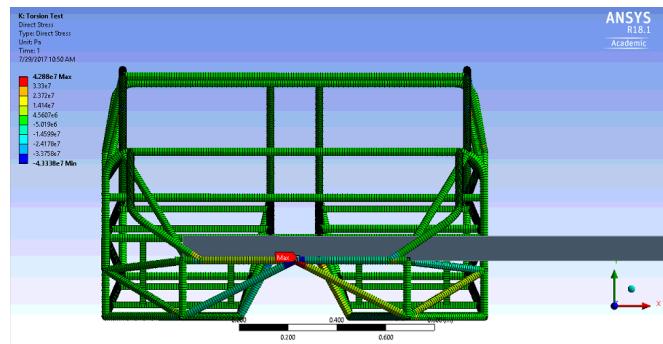


Figure 34: Torsion test, stress

## C FEA images for suspension and steering

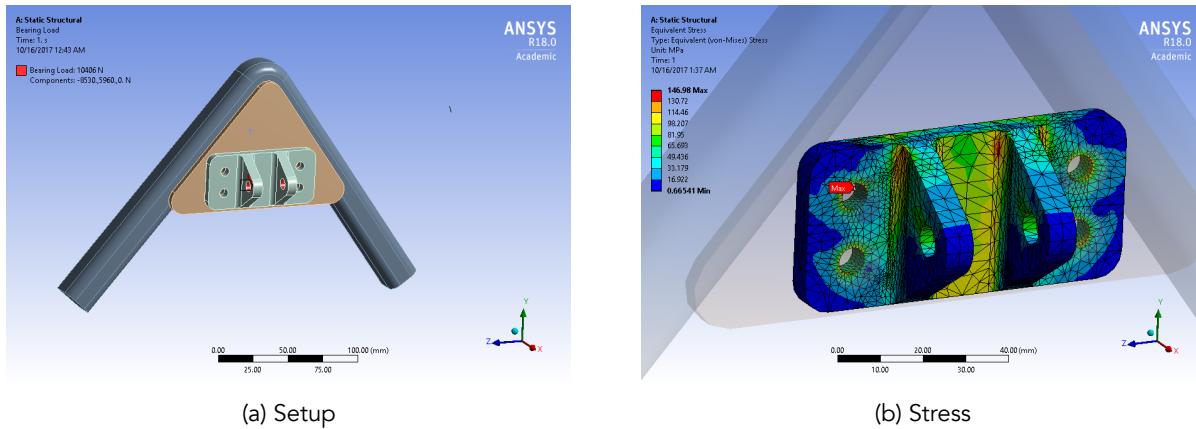


Figure 35: Coilover clevis

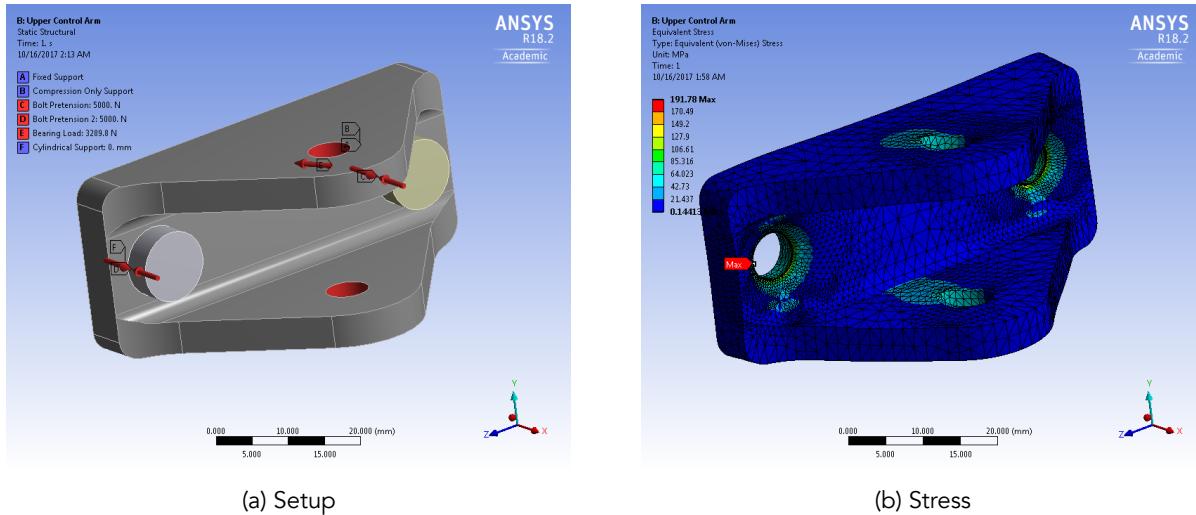


Figure 36: Upper control arm clevis

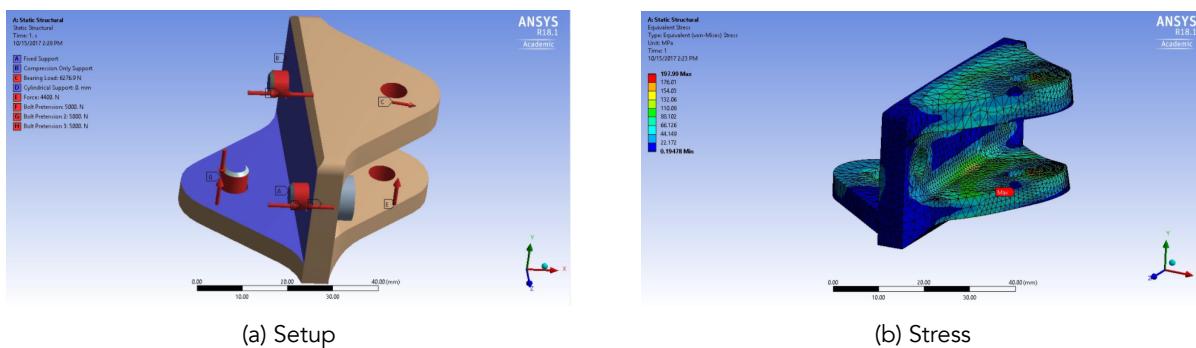


Figure 37: Lower control arm clevis

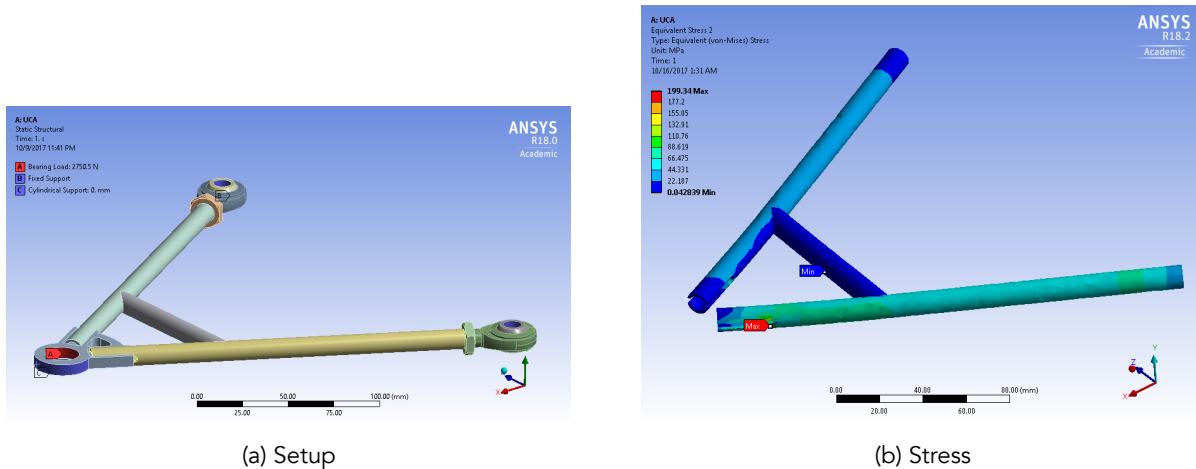


Figure 38: Upper control arm

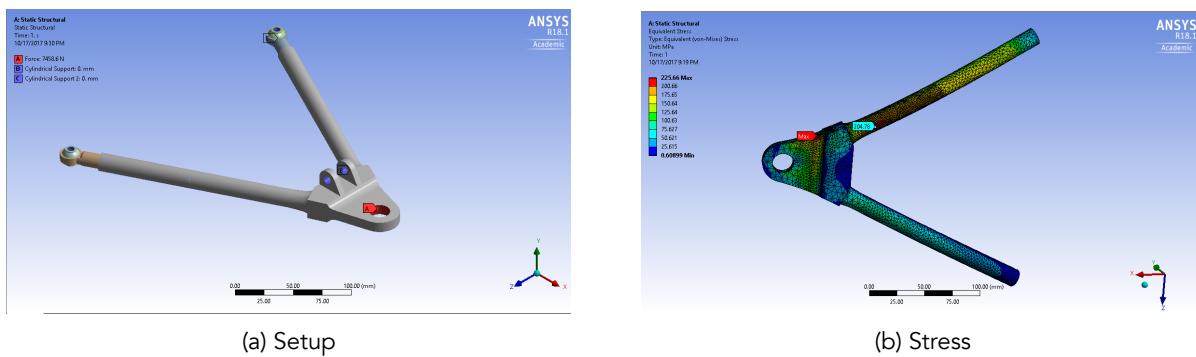


Figure 39: Lower control arm

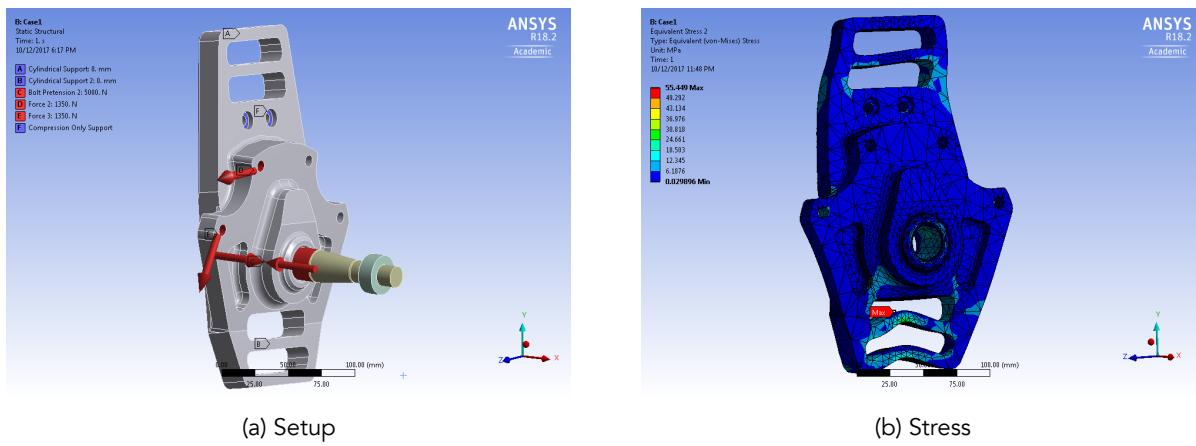


Figure 40: Upright

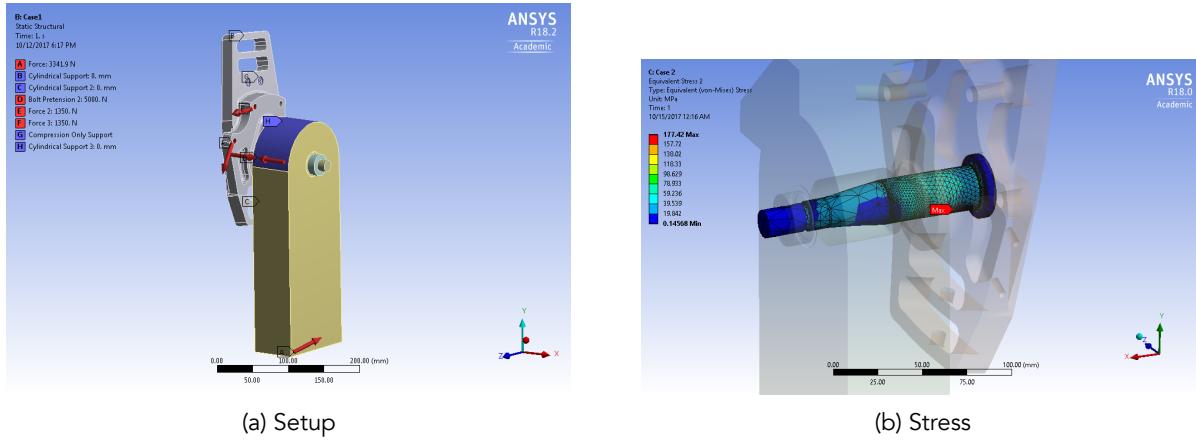


Figure 41: Spindle

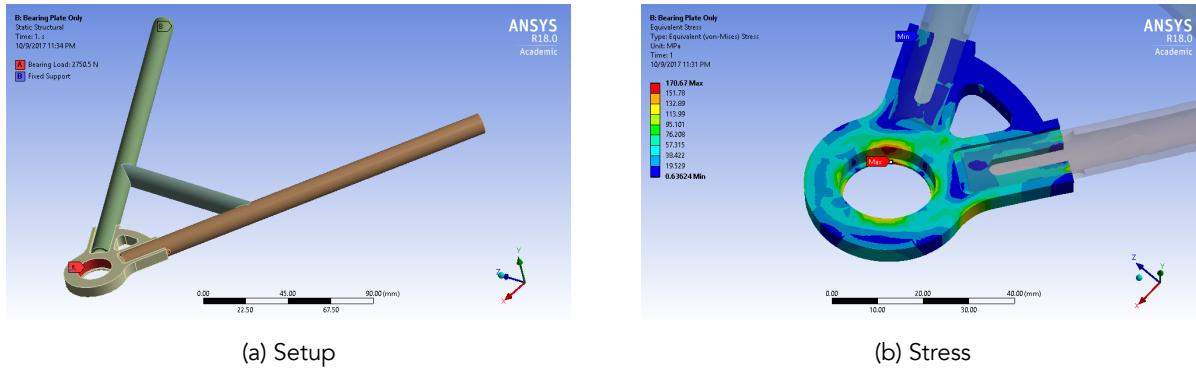


Figure 42: Upper bearing plate

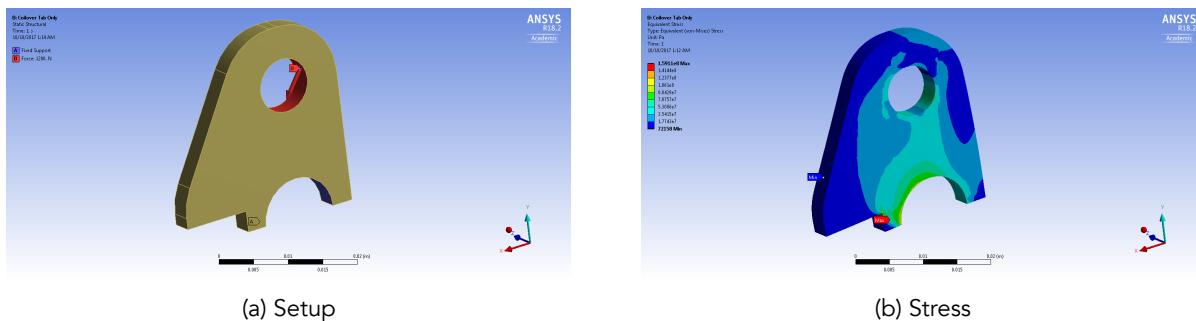


Figure 43: Coilover control arm tab

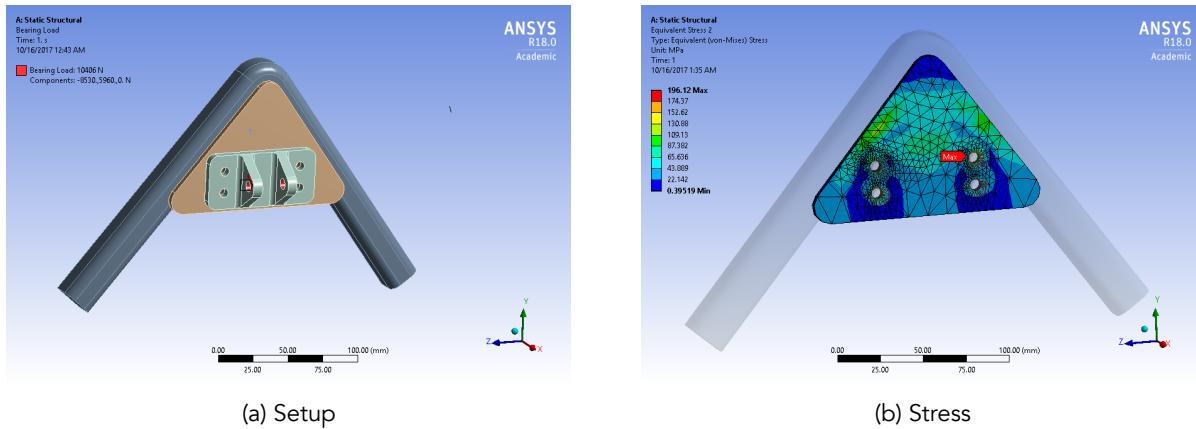


Figure 44: Coilover mounting plate

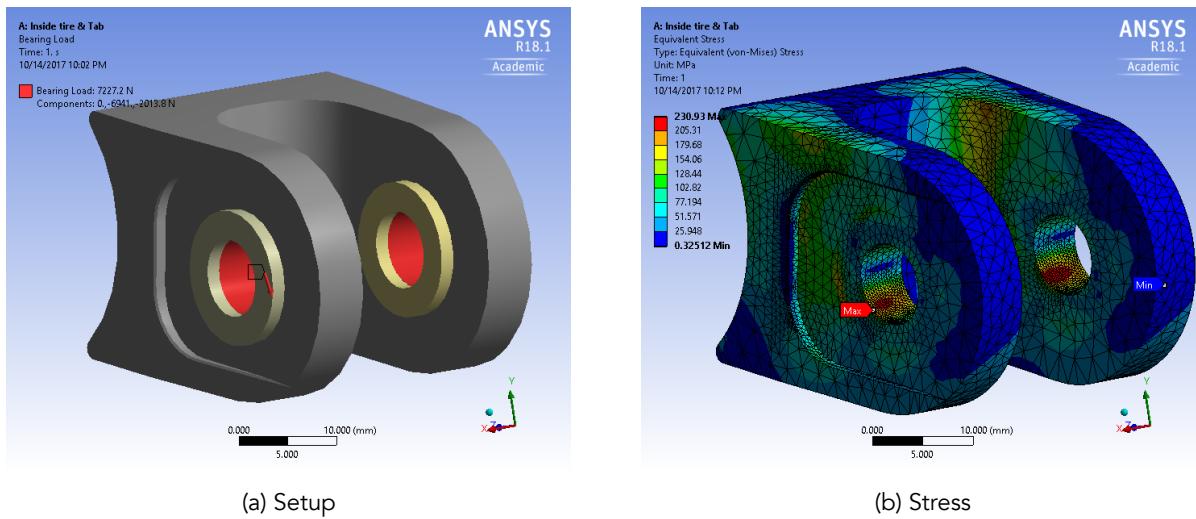


Figure 45: Rear suspension clevis

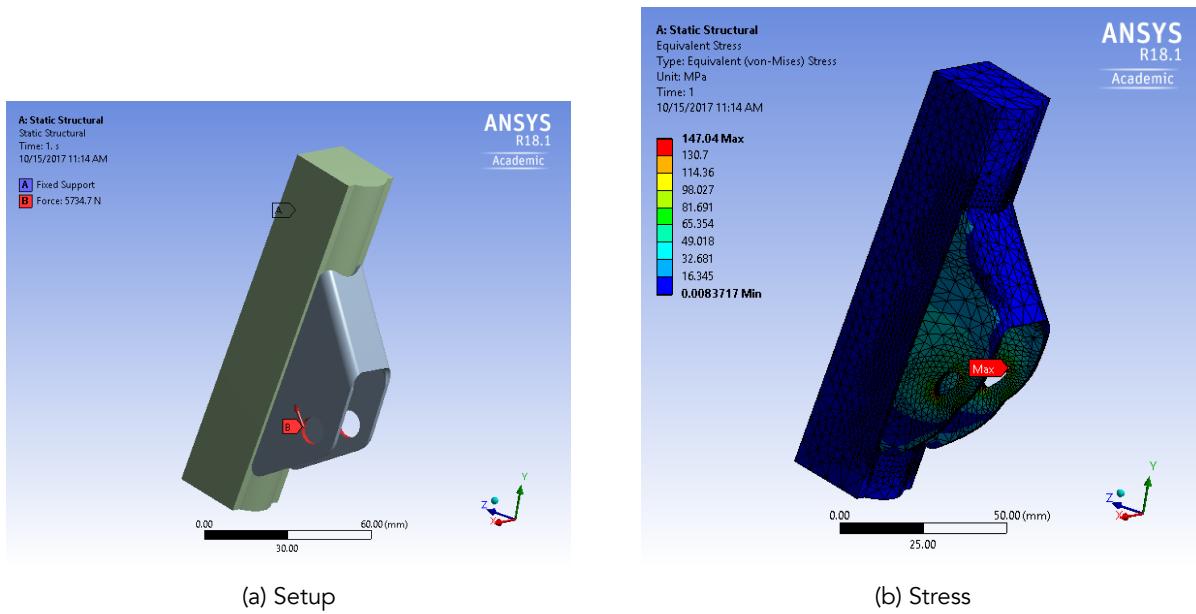


Figure 46: Rear suspension coilover tab

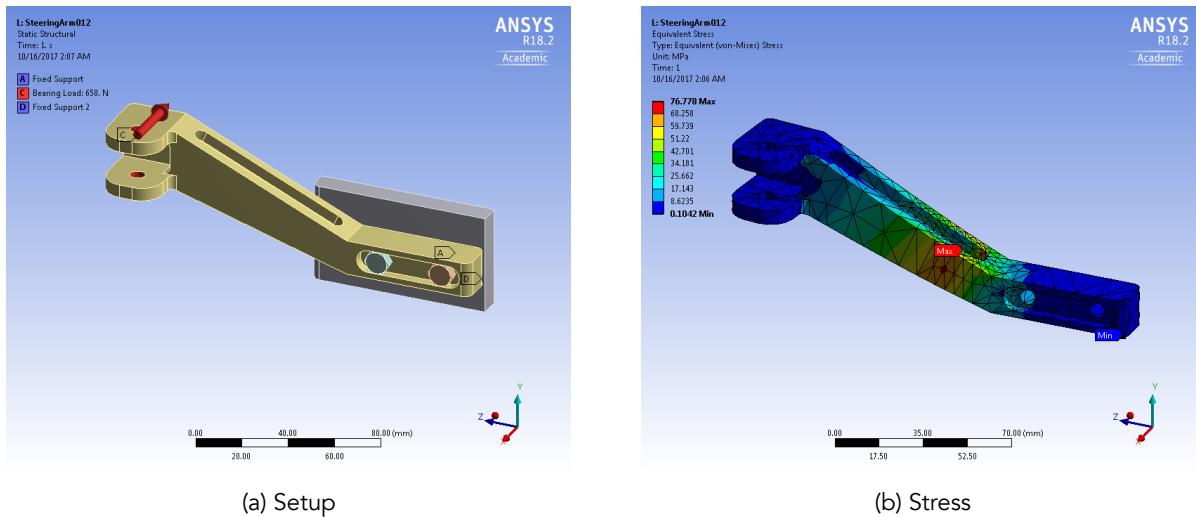


Figure 47: Steering arm

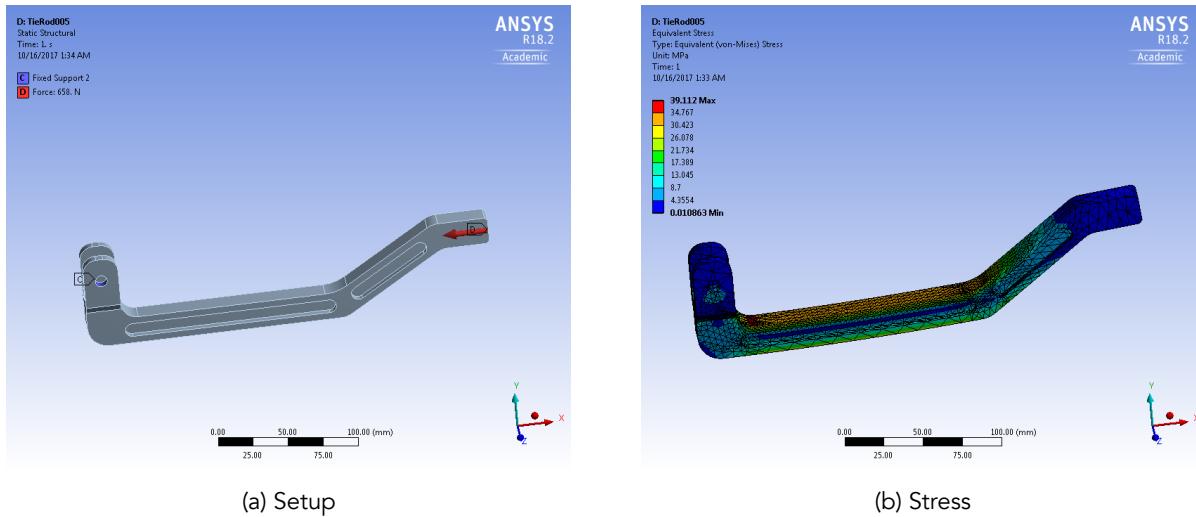


Figure 48: Tie rod