1. Parameters

y0[i]Gross output ys0[j,i]Sectoral supply ty0[j] Output tax rate fs0[i] Household supply id0[i,j]Intermediate demand fd0[i,fd]Final demand va0[va,j] Vaue added ts0[ts,i]Taxes and subsidies m0[i]Imports x0[i]Exports of goods and services mrg0[i] Trade margins trn0[i]Transportation costs duty0[i] Import duties sbd0[i]Subsidies on products tax0[i]Taxes on products ms0[i,m]Margin supply md0[m,i]Margin demand s0[i]Aggregate supply d0[i]Sales in the domestic market a0[i] Armington supply bopdef Balance of payments deficit ta0[i] Tax net subsidy rate on intermediate demand tm0[i]Import tariff ty[j] Output tax rate ta[i] Tax net subsidy rate on intermediate demand Import tariff tm[i]

2. Variables

Y[J]Sectoral production A[I]Armington supply MS[M]Margin supply PA[I] Armington price PY[I]Supply PVA[VA] Value-added PM[M]Margin PFXForeign exchnage RARepresentative agent

3. Macros

$$\begin{split} CVA[j=J] & \prod_{va \in VA} PVA[va]^{\theta_{va}[va,j]} \\ PMD[i=I] & \left(\theta_m[i] \cdot \left(\frac{PFX \cdot (1+tm[i])}{(1+tm0[i])}\right)^{1-2} + (1-\theta_m[i]) \cdot PY[i]^{1-2}\right)^{1/(1-2)} \\ PXD[i=I] & \left(\theta_x[i] \cdot PFX^{1+2} + (1-\theta_x[i]) \cdot \left(\frac{PA[i] \cdot (1-ta[i])}{(1-ta0[i])}\right)^{1+2}\right)^{1/(1+2)} \\ MD[i=I] & A[i] \cdot m0[i] \cdot \left(\frac{PMD[i] \cdot (1+tm0[i])}{PFX \cdot (1+tm[i])}\right)^2 \\ YD[i=I] & A[i] \cdot y0[i] \cdot \left(\frac{PMD[i]}{PY[i]}\right)^2 \\ XS[i=I] & A[i] \cdot x0[i] \cdot \left(\frac{PFX}{PXD[i]}\right)^2 \\ DS[i=I] & A[i] \cdot a0[i] \cdot \left(\frac{PA[i] \cdot (1-ta[i])}{(PXD[i] \cdot (1-ta0[i]))}\right)^2 \end{split}$$

4. Market Clearance

 $mkt_py[i = I]$ – Market clearance for supply price

$$\begin{split} y0_[i] &= \sum_{j \in J} ys0_[j,i] + fs0_[i] - \sum_{m \in M} ms0_[i,m] \\ A[i] \cdot y0[i] \cdot \left(\frac{PMD[i]}{PY[i]}\right)^2 &= \sum_{j \in Y_} Y[j] \cdot ys0[j,i] - \sum_{m \in M} MS[m] \cdot ms0[i,m] \end{split}$$

mkt-pa[i = I] – Market clearance for Armington price

$$\begin{split} a0_[i] &= \sum_{j \in J} id0_[i,j] + \sum_{fd \in FD} (fd0_[i,fd]) \\ A[i] \cdot a0[i] \cdot \left(\frac{PA[i] \cdot (1 - ta[i])}{PXD[i] \cdot (1 - ta0[i])} \right)^2 &= \frac{\theta_c[i] \cdot RA}{PA[i]} + \sum_{j \in Y_} Y[j] \cdot id0[i,j] + \sum_{xfd \in XFD} fd0[i,xfd] \end{split}$$

 $mkt_pm[m_=M]$ – Market clearance for margin

$$\begin{split} \sum_{i \in I} ms0_[i, m_] &= \sum_{i \in I} md0_[m_, i] \\ \sum_{i \in I} MS[m_] \cdot ms0[i, m_] &= \sum_{i \in I | a0[i] \neq 0} A[i] \cdot md0[m_, i] \end{split}$$

 $mkt_pva[va]$ – Market clearance for value-added

$$\sum_{j \in J} va0[va, j] = + \sum_{j \in Y} Y[j] \cdot va0[va, j] \cdot \frac{CVA[j]}{PVA[va]}$$

 $mkt_{-}pfx$ – Market clearance for foreign exchange;

$$\sum_{i \in A_-} XS[i] + bopdef = \sum_{i \in A_-} MD[i]$$

5. Zero Profit

 $prf_{-}y[j=J]$, – Zero profit for sectoral production

$$\begin{split} (1-ty0[j]) \cdot \sum_{i \in I} ys0_[j,i] &= \sum_{i \in I} id0_[i,j] + \sum_{va \in VA} va0_[VA,j] \\ (1-ty[j]) \cdot \sum_{i \in I} PY[i] \cdot ys0[j,i] &= \sum_{i \in I} PA[i] \cdot id0[i,j] + CVA[j] \cdot \sum_{va \in VA} va0[va,j] \end{split}$$

$$\begin{split} prf_a[i = I], - \text{Zero profit for Armington Supply} \\ a0_[i] \cdot (1 - ta0[[i]]) + x0_[i] = y0_[i] + m0_[i] \cdot (1 + tm0[[i]]) + \sum_{m \in M} md0_[m, i] \\ PXD[i] \cdot (a0[i] \cdot (1 - ta0[i]) + x0[i]) = PMD[i] \cdot (y0[i] + (1 + tm0[i]) \cdot m0[i]) + \sum_{m \in M} PM[m] \cdot md0[m, i] \end{split}$$

$$prf_ms[m=M]$$
 – Zero profit for margin supply
$$\sum_{i\in I} PY[i] \cdot ms0[i,m] = PM[m] \cdot \sum_{i\in I} ms0[i,m]$$

6. Income Balance

bal_RA – Income balance for representative agent

$$\begin{split} RA &= \sum_{i \in I} PY[i] \cdot fs0[i] \\ &+ PFX \cdot bopdef \\ &- \sum_{i \in I, xfd \in XFD} PA[i] \cdot fd0[i, xfd] \\ &+ \sum_{va \in VA, j \in J} PVA[va] \cdot va0[va, j] \\ &+ \sum_{i \in I} A[i] \cdot (a0[i] \cdot PA[i] \cdot ta[i] + PFX \cdot MD[i] \cdot tm[i]) \\ &+ \sum_{j \in J} Y[j] \cdot \sum_{i \in I} (ys0[[j], [i]] \cdot PY[i]) \cdot ty[j] \end{split}$$

Hi Siwan!