

# State Assignment Using Decision Trees

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Given a vector  $x$  of gene expressions, state assignment determines which of several states  $s$  in  $S$  is the best label for  $x$ . This is a classification problem.

In state assignment, we are given  $[X^T S]$ , gene expression data paired with its associated state.  $X$  has columns indexed by  $K$  gene (features) and  $N$  rows indexed by data instance. Values in  $X$  are discrete. In our case, values are  $[-1, 0, 1]$ .

We use the notation  $\sigma(x) = s$  to denote that  $s$  is the state assigned to the vector  $x$  in  $X^T$ . The state assigned by algorithm  $A$  is  $\sigma_A(x)$ . Our objective in state assignment is to minimize  $Pr(\sigma_A(x) \neq \sigma(x))$  that probability that the state assigned by  $A$  differs from the true state. We define  $err(A, X) = \sum_{x \in X} 1_{\sigma_A(x) \neq \sigma(x)}$ .

We use  $\nu_k$  to denote  $t$

## Technical Approach

1. Data preparation
  - (a) Eliminate  $T_0$  since all 0's.
  - (b) Combine Normoxia with Resuscitation since insufficient values for Normoxia.
  - (c) Combine perfectly correlated features
2. Analysis 1: All data
  - (a) Construct DT with all data
  - (b) Analyze the effective number of independent features given feature "correlations" (can we use correlation or need a new measure because of nominal values).
  - (c) Assess probability of uniquely identifying states under the null hypothesis of random and independent assignment of expression values
3. Analysis 2: Cross validation
  - (a) Compare misclassification rates with random for 5 classes

4. Analysis 3: Sensitivity to random perturbations of the data
  - (a) Train on data with an error fraction  $f$ . Do repeatedly to see stability of features. Relate to correlation blocks.
  - (b) Evaluate on new data with an error fraction  $f$

## Visualizations

## Vectorized Implementation