

**Exercise-1.1:** MSE (Mean Squared Error) function, in this case:  $E(w) = \frac{1}{2} \sum_{n=1}^N \{y(x_n, w) - t_n\}^2$  is a convex function. Meaning there is only one minima point. We want to find its coordinates for a specific value of  $w_i$  we can find that value by  $\frac{\delta}{\delta w_i} E(w) = 0$ .

$$\frac{1}{2} \frac{\delta}{\delta w_i} \sum_{n=1}^N \{y(x_n, w) - t_n\}^2 = \frac{1}{2} * 2 * \sum_{n=1}^N \{(y(x_n, w) - t_n) * \frac{\delta}{\delta w_i} (y(x_n, w) - t_n)\}$$

Then

$$\begin{aligned} \sum_{n=1}^N \{(y(x_n, w) - t_n) * x^i\} &= \sum_{n=1}^N \left\{ \sum_{j=0}^M \{w_j x_n^j\} - t_n \right\} x_n^i \\ &= \sum_{n=1}^N \sum_{j=0}^M \{w_j x_n^{j+i}\} - \sum_{n=1}^N \{t_n x_n^i\} = 0 \end{aligned}$$

Continues as

$$\sum_{n=1}^N \sum_{j=0}^M \{w_j x_n^{j+i}\} = \sum_{n=1}^N \{t_n x_n^i\}$$

Which is

$$\sum_{j=0}^M A_{ij} w_j = T_i \text{ consisten with the equations of } A_{ij} \text{ and } T_i \text{ given at question.}$$