

**Exercise-1.3:** Let X be the random variable denoting the fruit we choose, let Y be the random variable denoting the box we choose.

First part of the question asks  $p(X=a)$ .

$$\begin{aligned} \text{From the sum rule } p(X = a) &= \sum_Y p(X = a, Y) \\ &= 0.2 * 0.3 + 0.2 * 0.5 + 0.6 * 0.3 = 0.34 \end{aligned}$$

Second part of the question asks  $p(Y=g|X=o)$ . We will use Bayes' theorem, since we know  $p(X=o|Y=g)$  we can calculate the first probability.

$$\begin{aligned} p(Y = g|X = o) &= \frac{p(X = o|Y = g)p(Y = g)}{p(X = o)} = \frac{0.3 * 0.6}{0.2 * 0.4 + 0.2 * 0.5 + 0.6 * 0.3} \\ &= \frac{0.18}{0.36} = 0.5 \end{aligned}$$