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Statitics

Statitics is a branch of mathematics that deals with the collection, analysis, interpretation, presentation, and organization of data. In applying statistics to a scientific, industrial, or social problem, it is conventional to begin with a statistical population or a statistical model to be studied.

- 1. Collection
 - Sampling of data
- 2. Analysis
 - Data Analysis techniques
- 3. Interpretation
 - Graphs or Plotting
- 4. Presentation

5. Organization

Stats Helps in

- Decision Making
 - Data Driven Decision Making
- Clarity and Precision

Stats used in many fields such as business, economics, engineering, and social sciences to make informed decisions and predictions.

Types of Statistics

1. Descriptive Statistics

It involves summarizing and describing data using measures such as mean, median, mode, range, standard deviation, and graphical representations like histograms and box plots. Descriptive statistics helps in identifying patterns, relationships, and trends in data, making it an essential tool in various fields, including business, medicine, and social science.

Exploring the Data (EDA).

2. Inferential Statistics

Inferential statistics is a branch of statistical science that involves drawing conclusions or making predictions about a larger population from a sample of data. This is done by using probability and hypothesis testing to determine the likelihood that observed results are due to chance or if there is a significant relationship between variables.

Genrating inference from population on the basis of sample.

Why Stats is Important for Data Science

Statistics is important because it helps to describe, understand, and interpret data. It is used to identify patterns and make predictions based on the information available. Statistics provides a framework for decision-making and problem-solving, and helps to make sense of complex data sets.

Question / Problem

How many Pakistani female and male are in IT industry? If there are 10 vacancies, then how we will know that how many seats we have to give to Male or Female?

Solution

Conduct a surveys of different cities, districts and gather the data. Let's suppose we took survey of 500 people.

- 250 Male IT
- 100 Female IT
- 150 Non IT

Maybe we didn't use a good technique to gather sample. Stats also helps in how to collect the data.

Scales or Levels of Measurement

1. Nominal Scale

- Names, Labels and Qualities. No Number and also No Order/Ranking.
- **Example**: Male, Female, Dot, Cat, Bird, Ahsan, Shakoor, Jawad, Ahmad.
- Stats: Can apply Mode, Frequency and Chi-Square.

2. Ordinal Scale

- Nominal Scale + Rank or Order.
- **Example**: Is it hot in Pakistan?
- o Options: I agree, I Strongly agree, I don't agree
- o Class Position of students first, second, third etc.
- Stats: Can check Median, Mode.

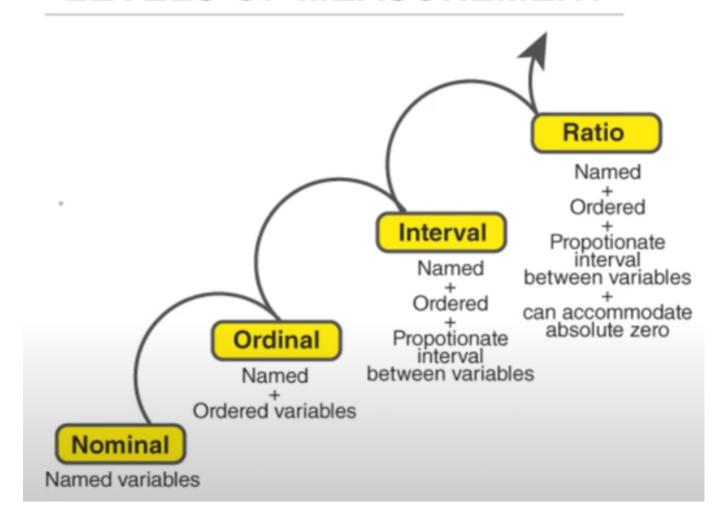
3. Interval Scale

- Numbers, Equal difference between numbers, Not True Zero, Absolute Zero.
- **Example**: Temperature in Celsius, Dates in Calender year.
- **Stats**: Can check Mean, Median, Mode, Variance, Standard Deviation, ANOVA Test, Regression Analysis.

4. Ratio Scale

- Numbers, True Zero, Meaningful Arithmetic Operations.
- **Example**: Height, Weight, Income, distance, decimal.
- Stats: Can apply Mean, Median, Mode, SD, Geomteric Mean, Harmonic Mean.

LEVELS OF MEASUREMENT



Qualitative vs Quantitive Data

Qualitative Data	Quantitive Data
Quality Measure	Quantity Measure
Categorical Data	Numerical Data
No Number Involved	Only Numbers
Nominal Scale	Interval Scale
Ordinal Scale	Ratio Scale
	Can Apply Arithmetic Operations

Example

Male, Female is a qualitative data, but what if we represent it using 0 and 1 then it will be also a **Qualitative Data**. Because 0 and 1 is the method to collect the data and at the end of day it represents Female or Male data.

It is called **Data Encoding**. We do it to increase the performance of computer and less time required to process.

Discrete Data

Discrete data is a type of data that can only take on a specific set of distinct values, such as integers, and is used to represent counts, frequencies, or categories. Such as 1, 2, 3, Car parking in parking lot, Number of children in family.

Coninuous Data

Continuous data is a type of data that can take on any value within a continuous range, such as decimal numbers, and is used to represent measurements or quantities. Such as all the decimal numbers between 1-2, Measurable data - height, weight, temperature, time series.

Binary Data

Binary data is a type of data that can only take on two values, typically represented as 0 and 1, and is used to represent categorical data or to encode other types of data. Such as True or False, Yes or No.

Time Series Data

Time series data is a type of data that is collected at regular intervals over time, and is used to analyze trends, cycles, and patterns in the data. Such as, calculating weight after every 10 days, stock market, weather, temperature.

Spatial Data

Spatial data is a type of data that is used to represent geographic features, locations, and phenomena, and is used in many fields such as geography, urban planning, and environmental science. Such as, location of a city, location of a building, location of a person.

Categorical Data

Categorical data is a type of data that is used to represent categories or groups, and is typically represented using text or labels. For example, the gender of a person can be represented as "male" or "female", which are categories. Blood Groups (A,AB,O,AB+).

No order included.

Ordinal Categorical Data

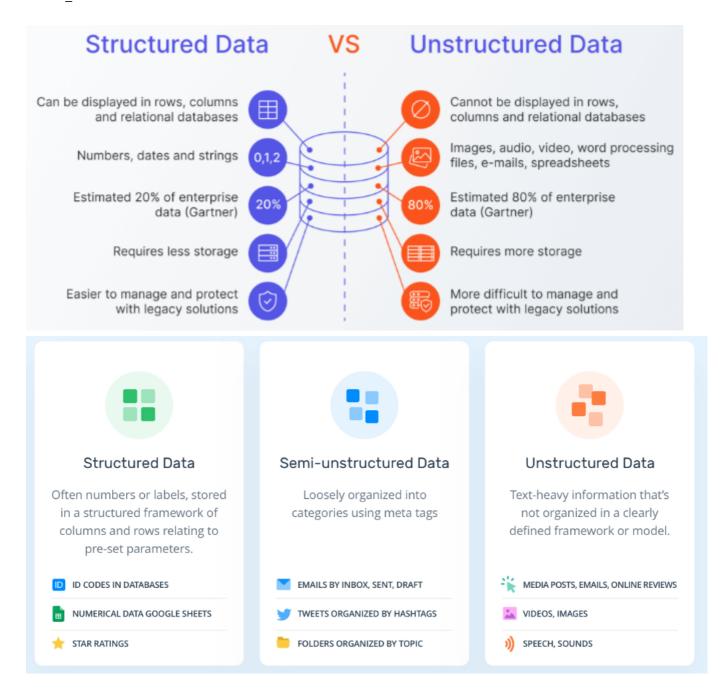
Same like categorical data but data is ordered. For example, Ratings, Educational level etc.

Multivariate Data

Multivariate data is a type of data that consists of multiple variables/columns/attributes that are measured on the same set of observations, and is used to analyze the relationships and patterns between the variables.

Univariate - one variable. Bivariate - two variables.

Structured vs Unstructured Data



Boolean Data

Boolean data is a type of data that can only take on two values, typically represented as 0 and 1, and is used to represent categorical data or to encode other types of data. It is also known as binary data.

Operationalization and Proxy Measurements

We measures something in order to give labels. Sometimes, we get the data which have no standard measurements and we make strategy to measure that concept which is called **Operationalization**Measurement.

For Example, measuring stress, we will measure the factors which give stress that is hearbeat, colestrol level, self reported feelings.

Using a related but indirect measure to estimate a variable of interest is called **Proxy Measurement**.

For Example, finding tree age, we can't ask the tree to tell us its age, so we can count the rings of stem to estimate the age.

Surrogate Endpoints

A surrogate endpoint is a measure that is used as a substitute for a more meaningful or direct measure of a phenomenon, and is used when the direct measure is difficult or impossible to obtain. Final aim can't be easily measured.

For Example, Heart Attack, we make different end-points to save a person rather than to give him a heart attack controller tablet. We measure the blood pressure and other factor and try to save the person.

Benefits

- 1. Short Research
- 2. Ethics
- 3. Help to save money

True and Error Score

True and error score is a measure of the accuracy of a measurement or prediction, where the true score is the actual value and the error score is the difference between the predicted and actual values.

True and error score is used in many fields, including engineering, physics, and statistics, to evaluate the accuracy of measurements and predictions. **Errors wh? questions** helps you to understand the error. Adjustments in algorithms are actually minimizing the errors.

For example, if a person's true weight is 70 kilograms and a scale measures it as 72 kilograms, then the error score is 2 kilograms. Maybe you make mistake (Human) or Weighing Balance error. Mostly this error occurs in **continuous data**.

```
X = T + E
where X = Observed Value, T = True Value and E = Error Value
```

Types of Errors

Systematic errors are errors that occur consistently and can be corrected for, while random errors are errors that occur randomly and cannot be completely eliminated.

1. Random Errors

Random errors are unpredictable and occur randomly in the measurement or evaluation process. These errors are typically due to factors outside the control of the person measuring or evaluating, such as outside influences or human error.

For example, random error is an error that if we do it twice then the values will change. Such as Dice, each time you will get random number.

2. Systematic Errors

Systematic errors, also known as measurement errors or assessment errors, are consistent and predictable mistakes made in the measurement or evaluation process. These errors can arise from flaws in the measurement instrument or from the way the measurement is conducted.

For example, an electronic scale that, if loaded with a standard weight, provides readings that are systematically lower than the true weight by 0.5 grams – that is, the arithmetic mean of the errors is -0.5 gram.

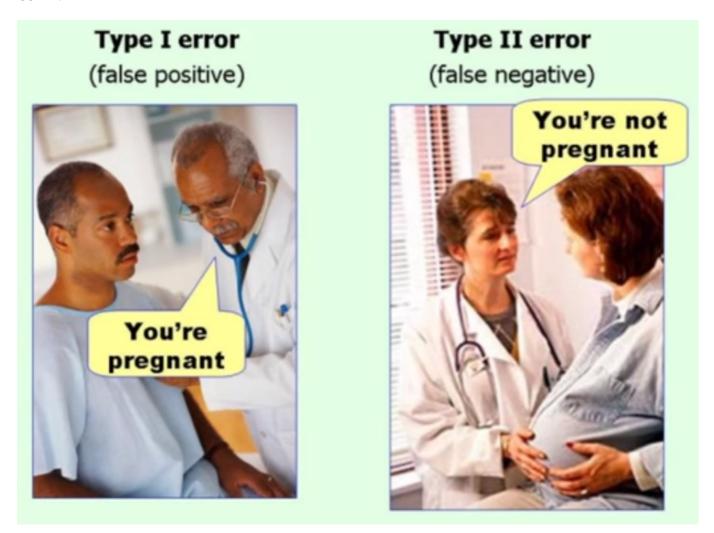
Type-I Error

False Positive Error. For example, let's suppose you don't have COVID but test kit is showing that you have COVID.

Work on 0 and 1 or ON and OFF.

Type-II Error

False Negative Error. For example, let's suppose you have COVID but test kit is showing that you don't have COVID.



Data Scientists should care alot about errors due to following factors:

- 1. Better Decision Making.
- 2. ML and Al Models will work better.
- 3. Better understanding of risk management.
- 4. Ethical implementation.

Reliability and Validity

Reliability and validity are both about how well a method measures something.

Reliability

Reliability refers to the consistency of a measure (whether the results can be reproduced under the same conditions). Claim is True. If we collect the data and that is reliable. A reliable is tool or method, when it yield the same results under consistent condition.

For example, we collected height and weight of different students in class and then ask them to verify the data. If they say yes then it is reliable.

For example, if you scored 95% on a test the first time and the next you score, 96%, your results are reliable. So, even if there is a minor difference in the outcomes, as long as it is within the error margin, your results are reliable.

Validity

Validity refers to the accuracy of a measure (whether the results really do represent what they are supposed to measure). Valid something which means accurate.

For example, all 12-inch rulers are one foot, I must repeat the experiment several times and obtain very similar results, indicating that 12-inch rulers are indeed one foot.

Why Important

Data is measure which are level of Measurements.

NOTE, DATA IS NEW OIL

If your data is Reliable and Valid then:

- 1. Your data is trust worthy.
- 2. You can take sound decision based on data.
- 3. Ethical Research.
- 4. Effective Solution

Triangulation

Triangulation in statistics refers to the use of multiple methods or sources of data to verify or corroborate a particular measurement or estimation. This technique is often used to reduce measurement error and increase the accuracy of results.

For example, Health records, air quality metrices, sattelite images all three leads to that Lahore is polluted city to live then it is triangulization.

Why Important Triangulation

- 1. Credibility
- 2. Reduces Bias
- 3. Increase Confidence on findings
- 4. Comprehensice View

Demerits

- 1. Resouce Intensive
- 2. Complex Integration
- 3. Skill Requirements

Measurement and Data Bias

Bias in research or data collection refers to systematic errors that skew results or inferences away from reality. Bias can occur in various aspects of research, including data collection, analysis, interpretation, and publication.

These biases can arise from various sources:

- 1. **Sampling Bias**: When the sample used in a study does not accurately represent the population.
 - For example, if a study is conducted only on men, the results may not be representative of the general population.
- 2. **Selection Bias**: When the participants included in the study do not accurately represent the general population. Its like listening to opinions of those people who agree with you.
 - For example, if a health survey is conducted only in urban hospitals, trends in rural areas may be missed.
- 3. **Confirmation Bias**: When researchers or data collectors consciously or unconsciously favor data or interpret results that confirm their pre-existing beliefs or hypotheses.
 - Pre Assumptions, Pre Existing beliefs.
 - For example, a detective only see to those clues which support his theory.
- Publication/Survivorship Bias: Selectively publishing only positive or significant results while neglecting negative or non-significant findings.
- 5. **Reporting Bias**: When only certain outcomes or aspects of a study are reported, leaving out others that may be equally important.
 - Media Channels.

These all lead you to **Information Bias**.

Measurement Bias

Measurement bias is a particular type of bias that is associated with systematic errors in collecting, recording, or interpreting measurements. It can significantly impact the reliability and validity of study outcomes. It mislead to draw conclusion.

Types of measurement bias include:

1. **Instrument Bias**: When there are flaws in the measurement instruments themselves. For example, a scale consistently showing lower weight than actual.

- 2. **Observer Bias**: When the person measuring (observer) unintentionally influences the results, perhaps due to their expectations or preconceived notions.
- 3. **Response Bias**: When study participants provide answers they believe are expected or socially acceptable, rather than their true thoughts or feelings.
- 4. **Sampling Bias**: A type of measurement bias related to how the sample is selected. If the sample does not accurately represent the population, measurement bias can occur.

Reducing Bias and Measurement Bias

- 1. Improve Sampling Methods (Randomized Sampling)
- 2. Use Refined Research Designs
- 3. Data Collection Vigillances (Use standardized protocol or use multiple resources)
- 4. Analytical Awareness (Statistical test & Peer Review)
- 5. Ongoing Education and Awareness

Data Analysis

A process of transforming raw data (collected data) into meaningful insights.

Types of Data Analysis

- 1. Descriptive Data Analysis
 - Focuses on summarizing the main features of a dataset.
- 2. Diagnostic Data Analysis
 - Digs deeper to find the cause behind the observed patterns.
- 3. Predictive Data Analysis
 - Uses historical data to predict future outcomes.
- 4. Prescriptive Data Analysis
 - Recommends actions and predicts their outcomes.
- 5. EDA
 - Explores data for patterns, anomalies, and hypotheses.
- 6. Inferential Analysis
 - Makes inferences about populations using sample data.
- 7. Causal Analysis
 - o Determines causality between variables.
- 8. Mechanistic Analysis
 - 1. Examines the exact mechanisms of changes in variables.

More Details

Population vs Sample

What is a Population?

In statistics, a population refers to the entire group that you want to draw conclusions about. For example, the population could be "all the people living in Lahore City" or "every oak tree in a forest."

What is a Sample?

A sample is a subset of the population, selected for study. For instance, surveying 1,000 residents of Lahore City as a sample of the entire city's population.

Ensuring Accurate Sampling

- 1. Random Sampling: Ensures every member of the population has an equal chance of being selected.
- 2. Stratified Sampling: Divides the population into strata and samples from each stratum.
- 3. Sample Size: Larger samples generally provide more accurate reflections of the population.

Central Tendency

Central Tendency is a way to describe the center of a data set. In data terms, it's the point around which the data clusters. Think of it as a way to summarize a whole lot of numbers with just one value that represents them best.

The Big Three of Central Tendency

1. Mean (The Average)

- Arithmetic Mean
- Geomteric Mean is calculated by multiplying all the valus together and then taking the nth root.
- Harmonic Mean is the reciprocal of the arithmetic mean of the reciprocals of the values.
 Suitable for rates and ratios.
- Weighted Mean is the weight or importance of each value in dataset.

2. Median (The Middle Value)

- Always sort the data then find the middle value.
- Outliers can be handle.
- Use on Real estates data, Income data.

3. Mode (The Most Common)

- Frequency of the most common value.
- Use on categorical data.

NOTE

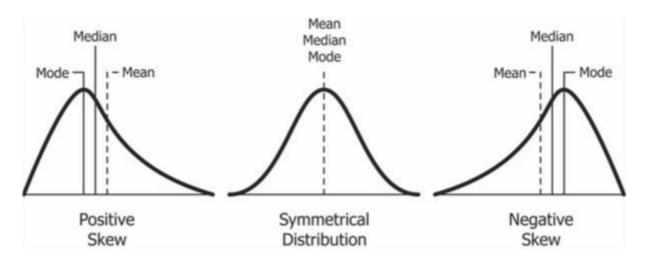
Mean: Can be skewed by outliers (like a billionaire moving into a neighborhood). **Median:** Great for skewed distributions (think wealth distribution). **Mode:** Perfect for categorical data (like survey responses).

Sample Mean: The mean of a sample of data. **Population Mean:** The mean of the entire population.

Population Mean	Sample Mean
$\mu = \frac{\sum_{i=1}^{N} x_i}{N}$	$\overline{X} = \frac{\sum_{i=1}^{n} x_i}{n}$
N = number of items in	n = number of items in
the population	the sample

Limitations of Mean

- 1. Sensitive to Outliers.
- 2. Sensitive to extreme values.
- 3. Sensitive to the number of values.
- 4. Doesn't tell the full story.



Variability | Dispersion | Spread of Data

Variability often referred to as dispersion, is the hearbeat of a dataset. It measures how much individual data points differ from each other and from the central tendency (like mean or median).

- 1. Range of Spread
 - o Max Min
- 2. IQR
 - Shows middle 50% of data.
 - o Q1, Q2, Q3, Q4
 - Helps to remove outliers
- 3. Variance
 - Checks spread around the mean
- 4. Standard Deviation
- 5. Standard Error

1. Range of Data

Sensitive to outliers.

- Minimum Value
- Maximum Value

Range = Maximum - Minimum

2. IQR (Interquartile Range)

Any data divided into 4 parts.

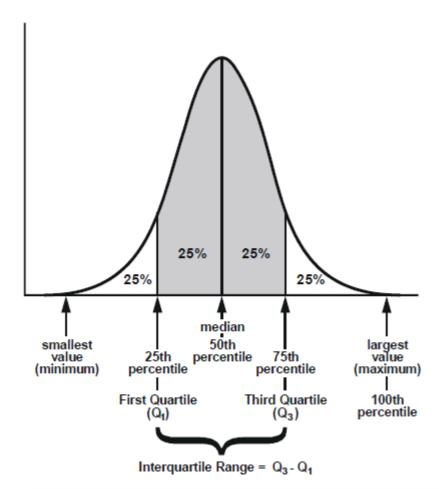
- Q1 (25th Percentile)
- Q2 (50th Percentile)
- Q3 (75th Percentile)
- Q4 (100th Percentile)

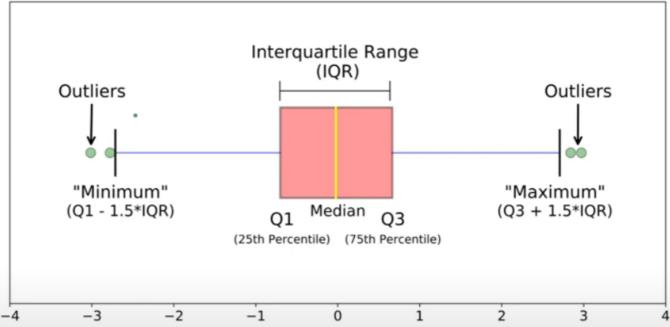
The middle 50% of data is IQR. Helps to identify outliers.

IQR = Q3 - Q1

Steps

- 1. Sort the data in ascending the order.
- 2. Find the quartiles.
- 3. Subtract Q1 from Q3.





3. Variance

Variance is a statistical measure that quantifies the extent to which data points in a set deviate from the mean.

Variance is a statistical measure of the spread of a dataset, calculated as the average of the squared differences between each data point and the mean, and is used to quantify the dispersion of data around an average value. For example, if the mean of a dataset is 10 and the variance is 4, it means that the data points in the dataset are on average 4 units away from the mean.

Variance is a measure of how spread out a set of data points is from the mean.

More About Variance

Variance is calculated by taking the average of the squared differences from the Mean. For a population (denoted as σ^2) and a sample (denoted as s^2), the formulas are slightly different:

• Population Variance:

$$\sigma^2 = rac{\sum (x_i - \mu)^2}{N}$$

• Sample Variance:

$$s^2=rac{\sum(x_i-ar{x})^2}{n-1}$$

Where x_i are the individual data points, μ is the population mean, \bar{x} is the sample mean, N is the size of the population, and n is the size of the sample.

4. Standard Deviation

Standard deviation is a measure of the dispersion of data around the mean.

A low standard deviation means that the data points are close to the mean, indicating smooth and consistent terrain. In contrast, a high standard deviation indicates that the data points are spread out over a wider range of values, akin to a rough, uneven landscape.

Mean +- SD/std/st.dev = 3 +- 0.05

Standard deviation is the square root of the variance. For a set of data, it's calculated using the following formulas:

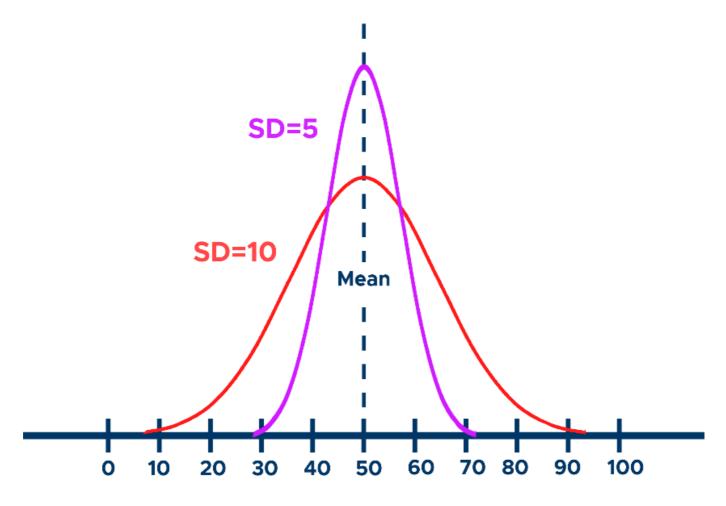
Population Standard Deviation

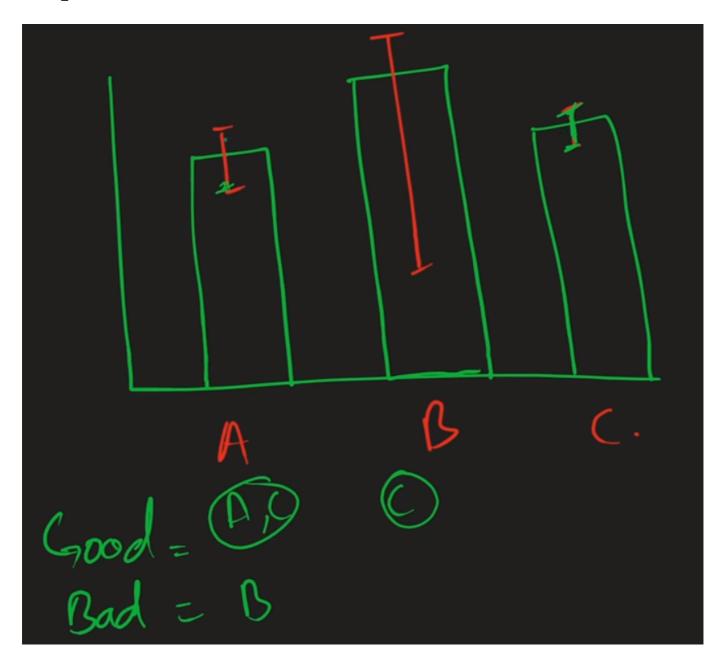
$$\sigma = \sqrt{rac{\sum (x_i - \mu)^2}{N}}$$

• Sample Standard Deviation

$$s=\sqrt{rac{\sum (x_i-ar{x})^2}{n-1}}$$

Where x_i represents each data point, μ is the population mean, \bar{x} is the sample mean, and N and n are the number of data points in the population and sample, respectively.





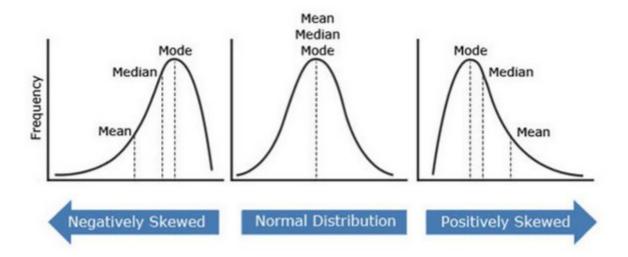
Standard Error

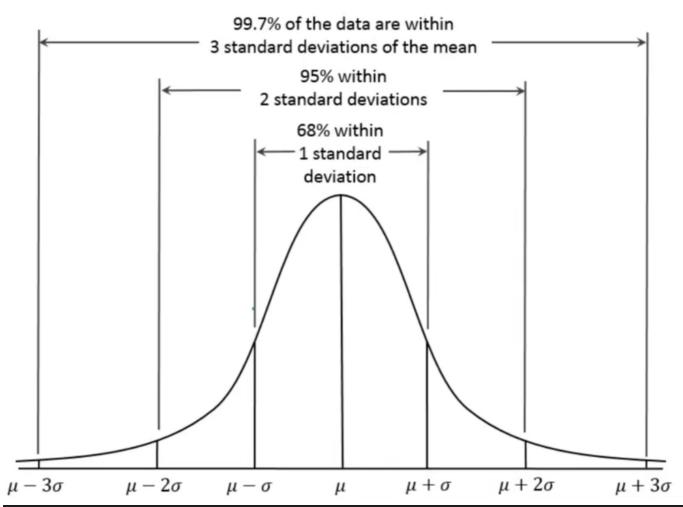
The standard error is used when we want to estimate the precision of the sample mean as an estimate of the population mean. It is calculated as the standard deviation divided by the square root of the sample size. The larger the sample size, the smaller the standard error, which means that the sample mean is more likely to be close to the true population mean. On the other hand, the standard deviation is used to describe the variability of the data set itself. It is calculated as the square root of the variance, which is the average of the squared differences from the mean. The standard deviation is useful for understanding how much the values in a data set vary from the mean.

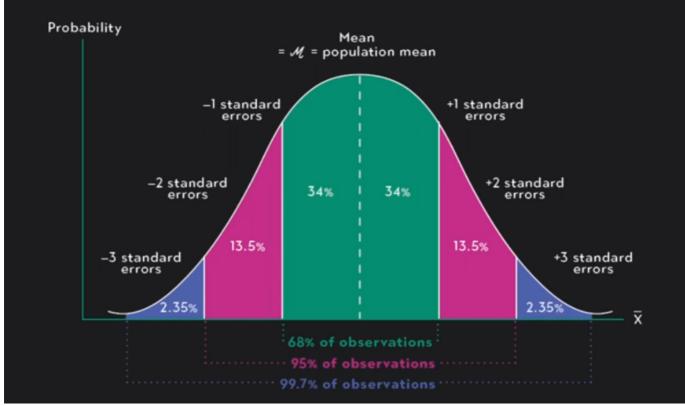
se = SD / square_root(n)

Normal Distribution / Gaussian Distribution

If we calculate STD;







Data Distributions

Data distribution refers to how data points in a dataset are spread out or clustered across a range of values. It is the blueprint that describes the shape or spread of data in a graphical format. Understanding the

distribution of data is fundamental in choosing the correct statistical methods and models for analysis.

Graphical representations such as histograms, box plots, and probability density plots are invaluable in visualizing data distributions. We apply distributions on **numerical data** only.

Understanding the distribution of data is pivotal in data science for several reasons:

- 1. Model Selection
- 2. Predictive Analysis
- 3. Outlier Detection

Why is normal distribution important in data science and data analysis?

The normal distribution is important in data science and data analysis because it provides a framework for statistical inference, simplifies analysis, and allows for the application of a wide range of statistical techniques.

How to Normalize the Data?

- 1. Min-Max Normalization
- 2. Z-Score Normalization

1. Normal/Gaussian Distribution: The Bell Curve

Symmetrical, bell-shaped curve centered around the mean. Example: Human heights within a specific gender and age group.

2. Uniform Distribution: Even Spread

All values have the same frequency, creating a flat distribution. Example: A fair roll of a dice, where each outcome from 1 to 6 is equally likely.

3. Binomial Distribution: Success or Failure

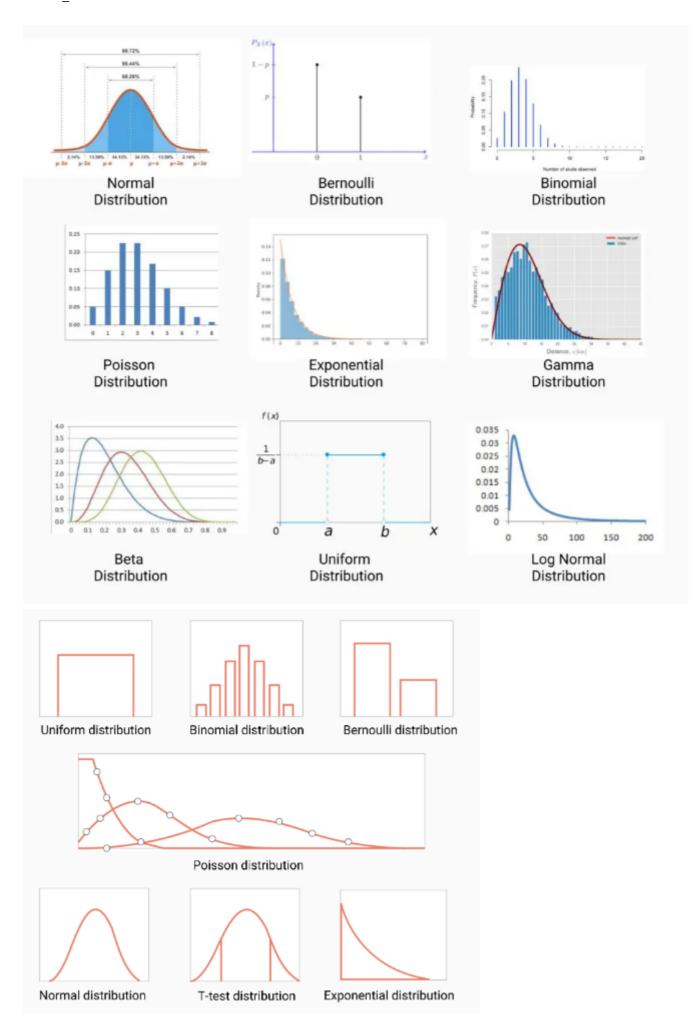
Represents the probability of a fixed number of successes in a series of independent experiments. Example: The number of heads observed when flipping a coin multiple times.

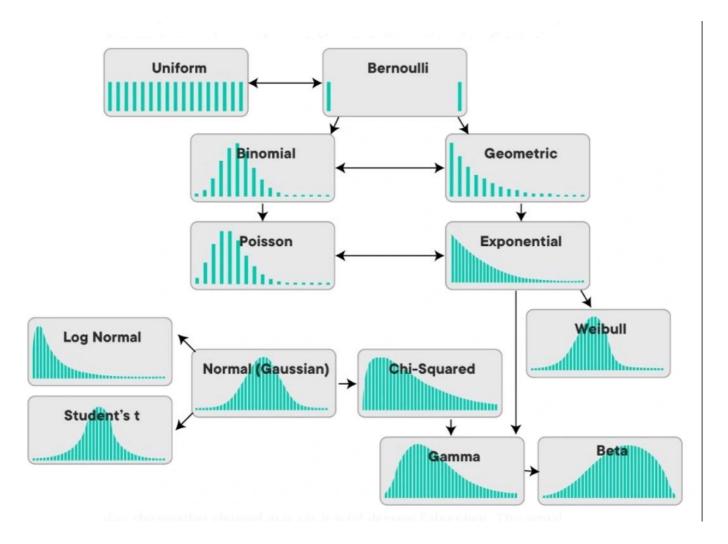
4. Poisson Distribution: Counting Events

Models the number of times an event occurs within a fixed interval. Example: The number of emails a person receives per day.

5. Exponential and Gamma Distributions: Modeling Time

Often used to model waiting times or lifetimes. Example: The amount of time until the next bus arrives.





Skewness vs Kurtosis

Skewness and kurtosis are measures that describe the shape of a data distribution. While they may sound complex, they are essentially tools to understand how data behaves around the mean.

Symmetrical Data Distribution

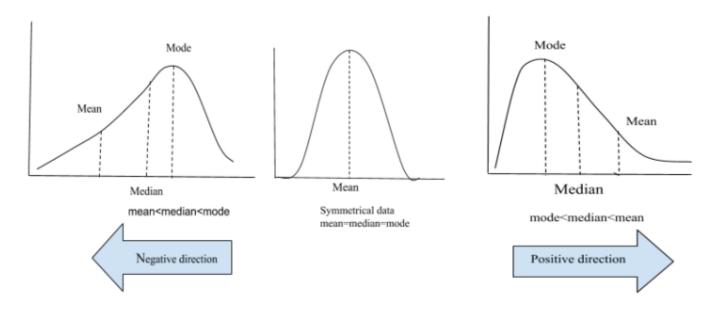
A distribution in which Mean, Media, and Mode are same on center data i.e Normally distributed.

Skewness: The Asymmetry Measure

Skewness measures the degree of asymmetry of a distribution around its mean. It indicates whether the data points are skewed to the left (negative skew) or to the right (positive skew) of the mean.

- Positive Skew: A distribution with a longer tail on the right side.
- Negative Skew: A distribution with a longer tail on the left side.

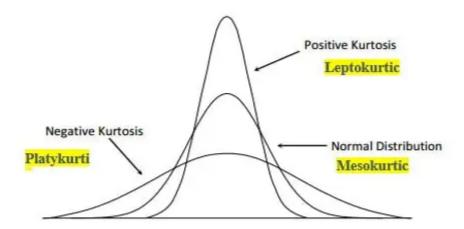
Example: Income distribution is often positively skewed, as a majority of people earn below the average, with a few high earners creating a long right tail.



Kurtosis: The Tailedness Measure

Kurtosis measures the 'tailedness' of a distribution. It describes the height and sharpness of the central peak and the heaviness of the distribution's tails.

- High Kurtosis (Leptokurtic): A distribution with heavy tails and a sharper peak than a normal distribution.
- Low Kurtosis (Platykurtic): A distribution with lighter tails and a flatter peak.



Skewness vs Kurtosis: The Key Differences

- Focus on Symmetry: Skewness primarily focuses on the symmetry, or lack thereof, of a distribution, whereas kurtosis is more about the extremity of data points.
- Implication on Data Analysis: Skewness affects the direction of data deviation, while kurtosis influences the probability of extreme values.

Data Collection

Data collection is the process of gathering and measuring information on variables of interest in a systematic manner, enabling one to answer stated research questions, test hypotheses, and evaluate outcomes. The quality of your data collection determines the quality of your data analysis.

Primary Data

Primary data is data that is collected directly from the source, such as through surveys, interviews, or observations, and is used to gather original information about a particular topic. For example, a researcher conducting a survey to gather data about people's opinions on a political issue is collecting primary data.

- 1. Research/Experiment Data Collection
- 2. Interview Data Collection
- 3. Primary Reagent Data Collection
 - Lab/University/Institute Data
- 4. Questionaire Data Collection
- 5. Survey Data Collection
- 6. Audio Data Podcast

Secondary Data

Secondary data is data that has been previously collected by someone else and is used to analyze or interpret information about a particular topic. For example, a researcher using census data to analyze population trends is using secondary data.

Best Practices in Data Collection

- 1. Clearly Define Your Objectives
- 2. Choose the Right Data Collection Method
- 3. Ensure Data Accuracy and Reliability
 - Implement checks and balances to validate the accuracy of your data.
 - This might include cross-checking with multiple sources or using validated instruments.
- 4. Be Mindful of Data Privacy and Ethics
- 5. Plan for Data Storage and Management
 - Have a system for organizing, storing, and managing your data.
 - This could involve databases, cloud storage, and data management software.
- 6. Train Your Data Collection Team
- 7. Pilot Test Your Data Collection Tools
- 8. Document the Process

Resources

ABC of Statistics