

I : set of transaction id
 J : set of priority type, 1 2 3 4
 K : set of probability type, 1 2 3 for the probability of transaction, description and customer respectively
 B : set of banks
 a_i : amount of the transaction i
 $date_i$: the date of transaction i
 w_k : weight of probability type k
 $Priority_i$: the priority type of transaction i , 1 2 3 4
 $cost_j$: the cost of employee hired to deal with priority type j t_j : time cost for investigate according to the priority type j $from_i$: the bank from of transaction i
 to_i : the bank to of transaction i
 $p_{k,i}$: the probability type k of transaction i
 M_b : the investigator number in bank b decision variable:
 x_i : 1 if decide to investigate the transaction i , 0 otherwise.
 y_i : 1 if hired employee to investigate transaction i , 0 otherwise
 $E_{m,n}$ for the investigate time cost by bank m for the transaction between bank m and bank n

Objective function:

$$\min. \sum_{i \in I} \left\{ \sum_{k \in K} (w_k * p_{k,i}) * a_i * (1 - x_i) \right\} + \sum_{i \in I} y_i * cost_{Priority_i}$$

Constraints :

we introduce I' that $I' = \{i \in I / y_i = 0\}$

for bank A:

$$\sum_{i \in \{I' / from_i=1\}} t_{Priority_i} * x_i - \sum_{n \in \{2,3,4,5\}} E_{1,n} + \sum_{m \in \{2,3,4,5\}} E_{m,1} \leq M_1$$

for bank B:

$$\sum_{i \in \{I' / from_i=2\}} t_{Priority_i} * x_i - \sum_{n \in \{1,3,4,5\}} E_{2,n} + \sum_{m \in \{1,3,4,5\}} E_{m,2} \leq M_2$$

for bank c:

$$\sum_{i \in \{I' / from_i=3\}} t_{Priority_i} * x_i - \sum_{n \in \{1,2,4,5\}} E_{3,n} + \sum_{m \in \{1,2,4,5\}} E_{m,3} \leq M_3$$

for bank D:

$$\sum_{i \in \{I' / from_i=4\}} t_{Priority_i} * x_i - \sum_{n \in \{1,2,3,5\}} E_{4,n} + \sum_{m \in \{1,2,3,5\}} E_{m,4} \leq M_4$$

for bank E:

$$\sum_{i \in \{I' / from_i=5\}} t_{Priority_i} * x_i - \sum_{n \in \{1,2,3,4\}} E_{5,n} + \sum_{m \in \{1,2,3,4\}} E_{m,5} \leq M_5$$

transactions between bank m and bank n :

$$E_{m,n} + E_{n,m} \leq \sum_{i \in \{I' / from_i = m, to_i = n\}} + \sum_{i \in \{I' / from_i = n, to_i = m\}} t_{Priority y_i} * x_i, \forall m, n \in B$$

Binary Variable Constraints:

$$x_i \in \{0, 1\}$$

$$y_i \in \{0, 1\}$$

Outcome and iterative:

z_i : 1 if the transaction i is scam, 0 otherwise.

α_i : 1 if $x_i = z_i$, 0 otherwise.

1 method 1

Change the objective function into:

$$\min. \sum_{i \in I} (p_{k,i}) * a_i * (1 - x_i) + \sum_{i \in I} y_i * cost_{Priority y_i}$$

run the model for $k=1,2,3$ respectively. And record the x_i as $x_i^{(1)}$, $x_i^{(2)}$ and $x_i^{(3)}$. Then we can have $\alpha_i^{(1)}$, $\alpha_i^{(2)}$ and $\alpha_i^{(3)}$.

$$\text{Let } w_1 = \alpha_i^{(1)} / (\alpha_i^{(1)} + \alpha_i^{(2)} + \alpha_i^{(3)})$$

$$w_2 = \alpha_i^{(2)} / (\alpha_i^{(1)} + \alpha_i^{(2)} + \alpha_i^{(3)})$$

$$w_3 = \alpha_i^{(3)} / (\alpha_i^{(1)} + \alpha_i^{(2)} + \alpha_i^{(3)})$$

with these new w_k , We get our model for the 1st iteration.

$$\text{for the 2nd iteration, } w_1(new) = (w_1(old) + \alpha_i^{(1)} / (\alpha_i^{(1)} + \alpha_i^{(2)} + \alpha_i^{(3)})) / 2$$

...

for the n th iteration,

$$w_1(new) = (w_1(old) * (n - 1) + \alpha_i^{(1)} / (\alpha_i^{(1)} + \alpha_i^{(2)} + \alpha_i^{(3)})) / n$$

...

2 method 2

run the original model and we get optimal solution x'

change $\sum_{k \in K} (w_k * p_{k,i})$ into z_i then we get the real cost c' if we take the optimal solution x' get from our model

$$\sum_{i \in I} z_i * a_i * (1 - x'_i) + \sum_{i \in I} y_i * cost_{Priority y_i} = c'$$

solve this objective function with same constrains:

$$\min. \sum_{i \in I} z_i * a_i * (1 - x_i) + \sum_{i \in I} y_i * cost_{Priority y_i}$$

we have optimal value \tilde{c} and optimal solution $tildex$ which is perfect.

Adjust w_k until we minimize $c' - \tilde{c}$, and we get optimal \tilde{w}_k for the model.