

Sample Statistics	Discrete RV	Properties
$Mean = \bar{X} = \frac{\sum_{i=1}^n x_i}{n}$ $Var = s^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1}$ $Std = s = \sqrt{\frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1}}$ $Cov = s_{xy} = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{n - 1}$ $Corr = r_{xy} = \frac{s_{xy}}{s_x s_y}$	$E[X] = \sum_i x_i P(X = x_i)$ $Var(X) = E[(X - E[X])^2]$ $= E[X^2] - E[X]^2$ $Cov(X, Y) =$ $= E[XY] - E[X]E[Y]$	$E[aX + bY + c] = aE[X] + bE[Y] + c$ $E[X \cdot Y] = E[X] \cdot E[Y] + Cov(X, Y)$ $Var(aX + c) = a^2 Var(X)$ $Var(X + Y) = Var(X) + Var(Y) + 2Cov(X, Y)$

Variable: k			
↓ Fixed ↓	# Successes	# Trials/Time until success	↓ Fixed ↓
1 trial	<b>Ber(p)</b> $P(X = 1) = p$	<b>Geo(p)</b> $P(X = k) = (1 - p)^{k-1} p$	1 success
n trials	<b>Bin(n, p)</b> $P(X = k) = \binom{n}{k} p^k (1 - p)^{n-k}$	<b>NegBin(r, p)</b> $P(X = k) = \binom{k-1}{r-1} p^r (1 - p)^{k-r}$	r successes
Interval of Time λ: expected # occurrences	<b>Poi(λ)</b> $P(X = k) = e^{-\lambda} \frac{\lambda^k}{k!}$	<b>Exp(λ)</b> $P(k_1 < X < k_2) = \int_{k_1}^{k_2} \lambda e^{-\lambda x} dx$	Interval of time to 1 <sup>st</sup> success λ: rate of occurrence

Example: Randomly filling a quiz with 4 options for each question. On average we answer 6 questions per minute.

Variable: k			
↓ Fixed ↓	# Successes	# Trials/Time until success	↓ Fixed ↓
1 trial	<b>Ber(p)</b> : Prob of correct answer to next question	<b>Geo(p)</b> : # of questions until we get the first correct answer	1 success
n trials	<b>Bin(n, p)</b> : Prob of correctly answering any 3 out of 4 questions	<b>NegBin(r, p)</b> : # of questions until we get 3 correct answers	r successes
Interval of Time λ: expected # occurrences	<b>Poi(λ)</b> : Prob of answering four questions in 20 seconds. (λ = 2, because 6 in 60 secs -> 2 in 20 secs)	<b>Exp(λ)</b> : Prob of spending from 5 to 8 seconds to answer next question. (λ = 6 / 60 = 0.1)	Interval of time to 1 <sup>st</sup> success λ: events/time