Vanya Vorobiov

Basic definitions

What is integrability in elementary functions

Liouville's Theorem (Differential algebra)

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- (ab)' = a'b + ab'

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Let F be the differential field. Then

- **b** is called the logarithm of a if $b' = \frac{a'}{a}$
- ▶ b is called the exponent of a if $a' = \frac{b'}{b}$

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