

## Asymptotische Schranken

### Hausaufgaben

**Aufgabe 1** (2 Points). Prove that  $\sum_{i=1}^n i \in \mathcal{O}(n^2)$ .

**Aufgabe 2** (2 Points). Prove or disprove that  $2^{2n} \in \mathcal{O}(2^n)$ .

**Aufgabe 3** (2 Points). Prove or disprove using the limit criterion:  $\sqrt{n} = \mathcal{O}(\log n)$ .

**Aufgabe 4** (2 Points). Let  $f, f', g, g' : \mathbb{N} \rightarrow \mathbb{R}^+$  such that  $f \in \mathcal{O}(g)$  and  $f' \in \mathcal{O}(g')$ . Show that:

$$ff' \in \mathcal{O}(gg').$$

Does this statement also hold analogously for asymptotically tight bounds?

**Aufgabe 5** (2 Points). Prove or disprove that  $1 + \sum_{k=2}^{\frac{n}{2}} \log(2k) \in \mathcal{O}(n \log n)$ .

**Aufgabe 6** (2 Points). Show that  $\sum_{i=0}^{\log_2(n)-1} 8^i \in \mathcal{O}(n^3)$ .