# **Chapter 1: Building Abstractions with Procedures**

```
Exercise 1.1
```

```
• 10
• (+ 5 3 4) \rightarrow 12
• (- 9 1) \rightarrow 8
• (/ 6 2) \rightarrow 3
• (+ (* 2 4) (- 4 6)) \rightarrow 6
• (define a 3) \rightarrow Stores 3 into var a
• (define b (+ a 1)) \rightarrow Stores 4 (+ 3 1) into var b
• (+ a b (* a b)) \rightarrow 19
• (= a b) \rightarrow NIL
• (if (and (> b a) (< b (* a b)))
       a)
        \hookrightarrow 4
• (cond ((= a 4) 6)
          ((= b 4) (+ 6 7 a)
          (else 25)))
          \hookrightarrow 16
• (+ 2 (if (> b a) b a)) \rightarrow 6
• (* (cond ((> a b) a)
             ((< a b) b)
             (else -1))
       (+ a 1))
        \hookrightarrow 16
Exercise 1.2
(/ (+ 5 4 (- 2
                    (+ 6
                        (/ 4 5)))))
    (* 3
       (-62)
        (- 2 7)))
Exercise 1.3
(define ex1.3 (x y z)
        (cond ((> x y))
                 (if (> y z)
                       (+ (* x x) (* y y))
                       (+ (* x x) (* z z)))
               (t
                  (if (> x z)
                       (+ (* y y) (* x x))
```

## Exercise 1.4

The function a-plus-abs-b utilizes the if condition to change the operation to a sum if b is positive or a substraction otherwise, acting as |b|.

(+ (\* y y) (\* z z))))))

Mathematically:

a-plus-abs-b
$$(a,b)=\left\{egin{aligned} a+b & \text{if } b>0 \\ a-b & \text{if } b<0 \end{aligned}\right.\equiv a+|b|$$

## Exercise 1.5

With an applicative oreder evaluation, the test function will not run properly because (p) will loop on itself, continiously running (test 0 (p)). Using normal order evaluation, because y is not utilized on the test function, the if clause will be executed and resolve to 0.

#### Exercise 1.6

The new if does not work in the sqrt-iter function, it throws a *stack overflow* type error.

This is because the special form if runs in applicative order, thus evaluating the predicate and only running then or else when needed. In the case of new-if, because of the recursive call, it will be stuck evaluating that.

## Exercise 1.7

Trying out the newton method, on very low numbers (0.0001) returns not very accurate results, compared to an actual square root method, comparing it with the common lisp sqrt:

- (sqrt 0.0001)  $\rightarrow 0.01$
- (newton-sqrt 0.0001)  $\rightarrow 0.032308448$

Now, with large numbers, what happens is that the number of operations exponentially increases and gets stuck evaluating. So, if we were to try and fix the first issue with smaller numbers, making our good-enough? function use a lower boundary, we would eventually reach the second problem, getting stuck in recursion.