

(0)

and  $\alpha_{i,j} \in K$ , a number field. We write this compactly as  $A\xi = \mathbf{0}$ . Let  $a \in \mathbb{Z}$ ,  $a > 0$ , and  $a \geq \|\alpha_{i,j}\|$  for all  $1 \leq i \leq p$  and  $1 \leq j \leq q$ . Then, there is a constant  $c$  depending only on  $K$  and independent of  $p, q$ , and  $\alpha_{i,j}$  such that the system of equations has a nontrivial solution in  $K^n$  for  $\xi$ , such that for all  $\xi_j$ ,

$$\|x_j\| < c + c(cqa)^{\frac{p}{q-p}}.$$