### B. Tech Project

Final Presentation

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Word Representable Graphs



#### Introduction

The problem of determining if a graph is a word representable is NP-complete. But we wanted to develop a tool that can do so for smaller graphs.

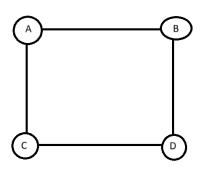


# Word Representable Graphs

Word-representable graphs can be represented by a word (or sequence) whose entries alternate in a prescribed way. In essence, each pair of vertices connected by an edge in the graph corresponds to an alternating pair of letters in the word.



### Word Representable Graphs



 $\bullet W = abcadcbd$ 



# Word Representable Graphs

#### Importance of WRG

Contains these important classes of graph

- circle graphs
- 3-colorable graphs
- comparability graph

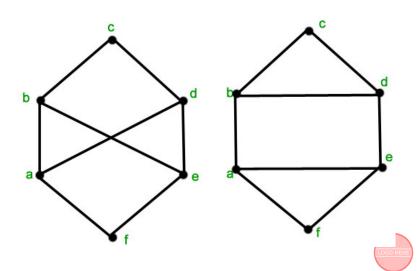


### Graph Isomorphism

Graph isomorphism refers to determining whether two graphs are structurally identical, meaning they have the same arrangement of vertices and edges, even with different labels.



# Graph Isomorphism



#### Problem Statement

Designing an algorithm to determine whether a given graph is word-representable or not.

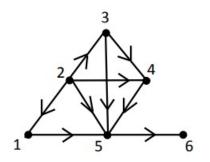


# Methodology

#### Semi Transitive Orientation

Semi-transitive orientation refers to a directed arrangement of edges in a graph where certain directed paths exhibit a partial transitivity property, forming transitive cliques. It's a way of directing the edges such that paths either maintain transitivity or follow a specific pattern, aiding in graph analysis and characterization.

### Semi Transitive Orientation



 Example of semi-transitive orientation



### Results

### Time Complexity - $O(2^{n^2})$

Number of non-isomorphic non-word representable graphs

- 6  $W_5$  out of 112 1 s
- 7 25 out of 853 10 s
- 8 929 out of 11117 1000 s



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