

# CS15210: Data Transmission

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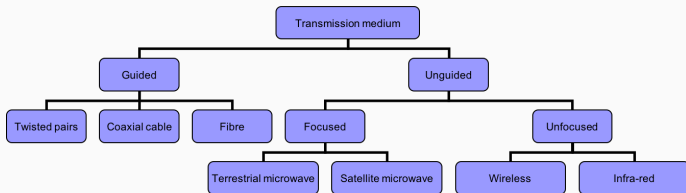
12/02/16

(based on slides by Mike Clarke)

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# Previously, in CS15210...

- Transmission media categories



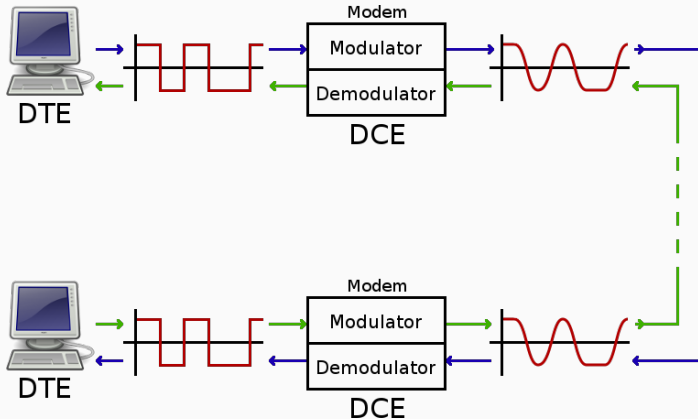
- The overall factors affecting choice of medium:
  - cost, capacity, robustness, security
- The properties of each type of medium

1. DTEs and DCEs
2. Modulation
3. Nyquist's Theorem and Logarithms
4. Wrapping Up

- DTE: Data Terminal Equipment
  - any device that is the source or destination of **digital** data
  - e.g. programs generating data, network cards
- DCE: Data Circuit-Terminating Equipment
  - any device that transmits or receives data in the form of an **analogue** or **digital** signal over a communications channel
  - e.g. modems

- Modem: **mod**ulator-**dem**odulator
- Modems convert signals for transmission across a communication channel:
  - **Modulation**: from digital to analogue
  - **Demodulation**: from analogue to digital
  - Must agree on a method beforehand

# Modems



**Modulation:** from digital to analogue  
**Demodulation:** from analogue to digital

distortion

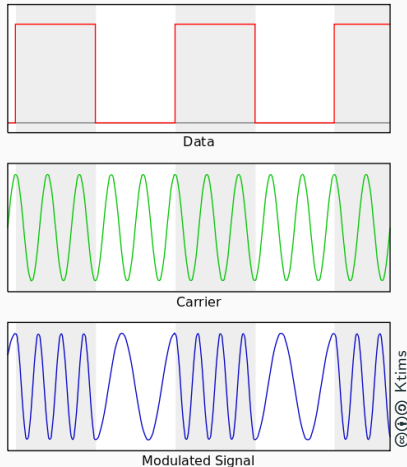


## **Why convert between analogue and digital?**

If a digital signal is sent down a wire just as it is,  
it is very prone to distortion

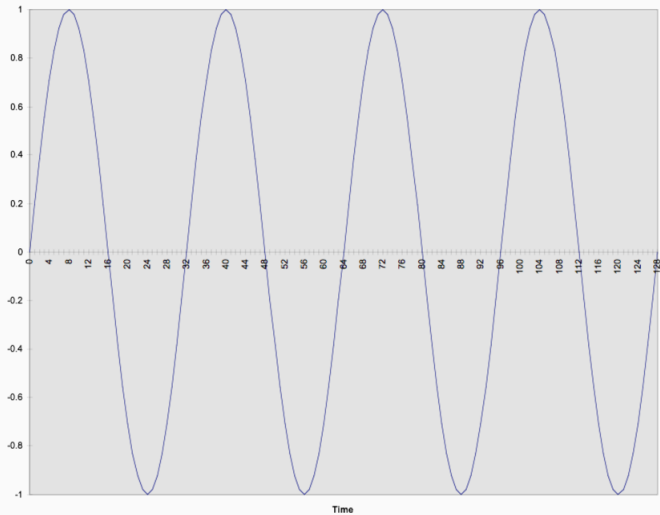
# Modulation and Demodulation

To avoid these problems,  
the **digital signal** is used to change (**modulate**) a **carrier wave**

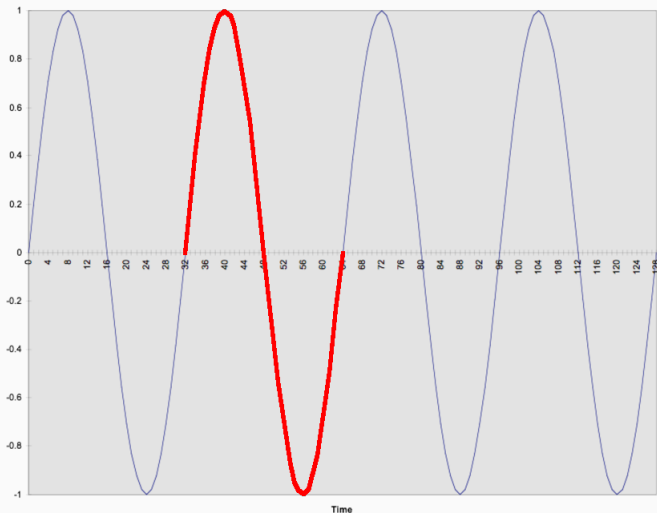




# Waves: A Quick Recap

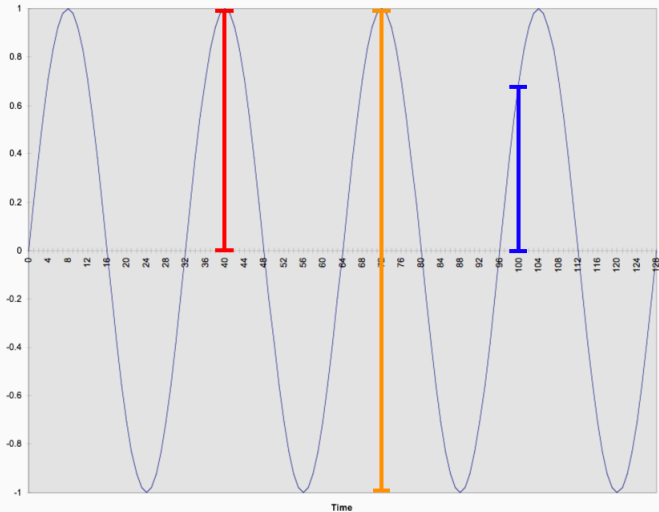


# Waves: Frequency



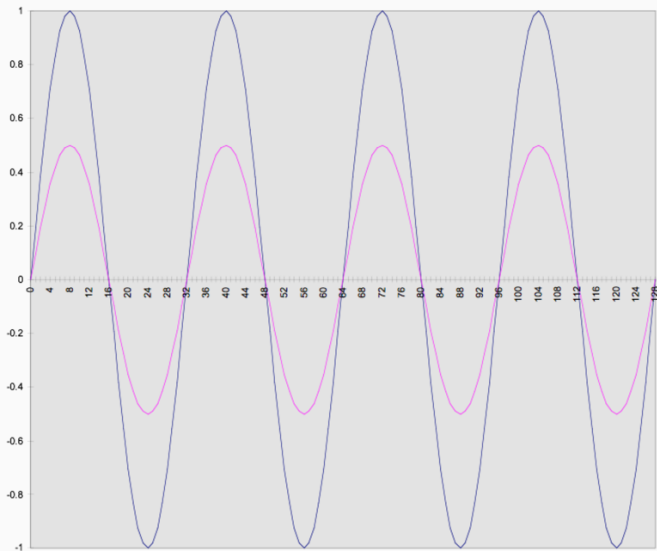
Number of complete cycles per second, measured in Hertz (Hz)  
i.e. if a cycle takes 1 second, frequency = 1 Hz

# Waves: Amplitude



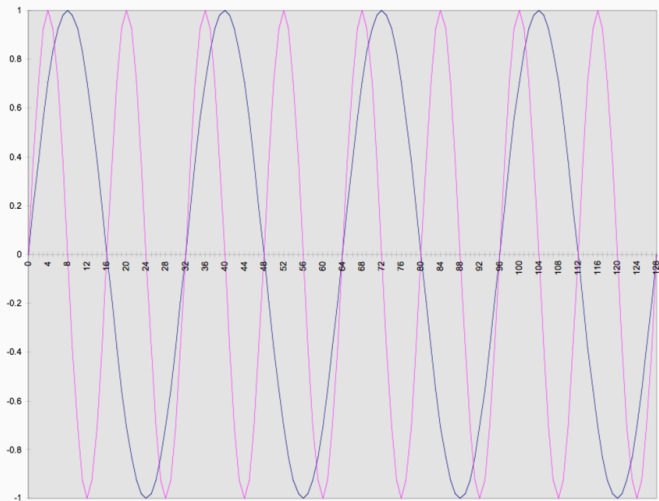
(Peak) amplitude, peak-to-peak amplitude, instantaneous amplitude

# Amplitude Difference



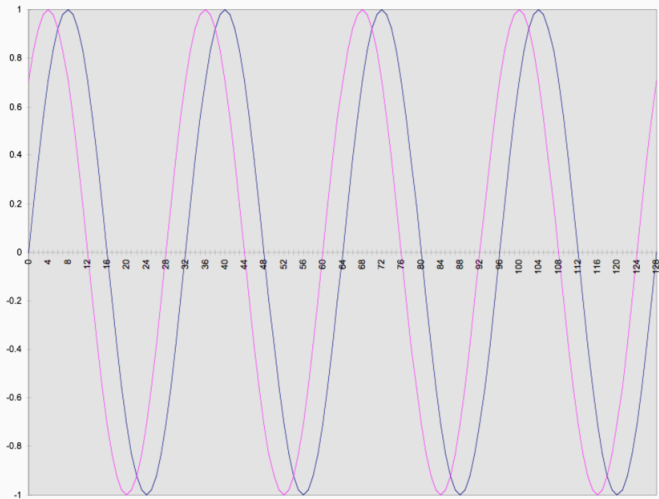
Two waves, the only difference is the amplitude

# Frequency Difference



Two waves, the only difference is the frequency

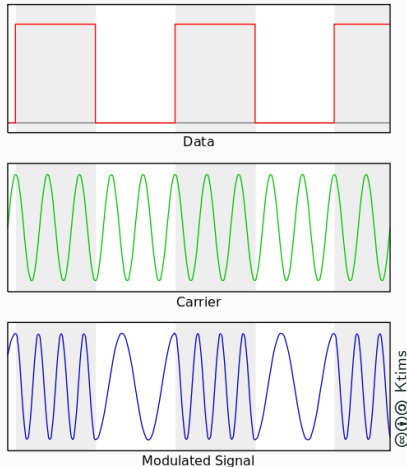
# Phase Difference



Two waves, the only difference is the start time of the cycle

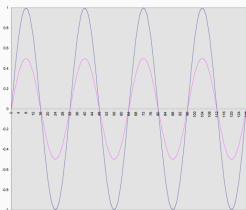
# Modulation and Demodulation

To avoid these problems,  
the **digital signal** is used to change (**modulate**) a **carrier wave**

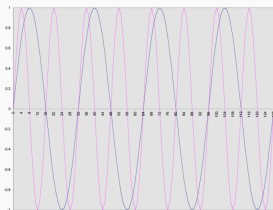


# Types of Modulation

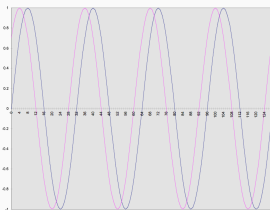
We can adjust the carrier wave to suit the type of data



Amplitude



Frequency

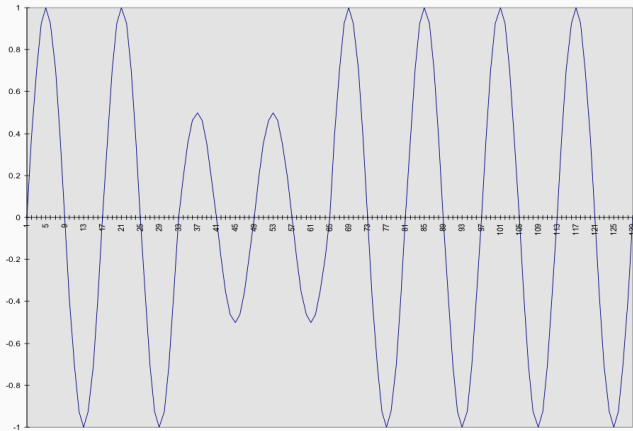


Phase

| Analogue Data             | Digital Data                 |
|---------------------------|------------------------------|
| Amplitude Modulation (AM) | Amplitude-Shift Keying (ASK) |
| Frequency Modulation (FM) | Frequency-Shift Keying (FSK) |
| Phase Modulation (PM)     | Phase-Shift Keying (PSK)     |

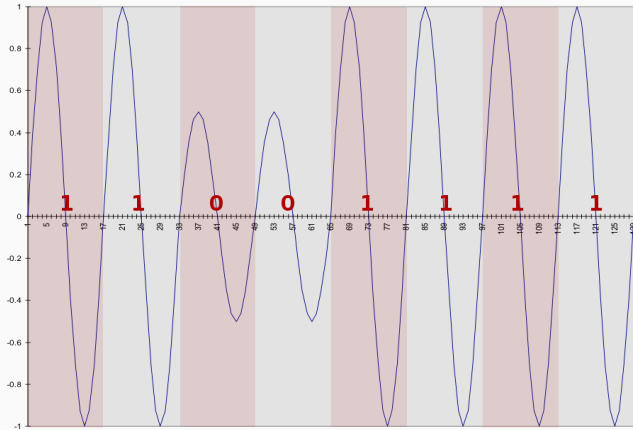


## Amplitude (ASK)



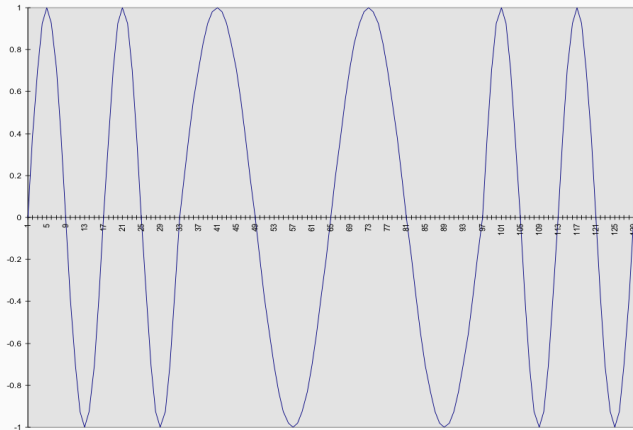
The carrier wave's **amplitude** is changed based on the digital signal

# Amplitude (ASK)



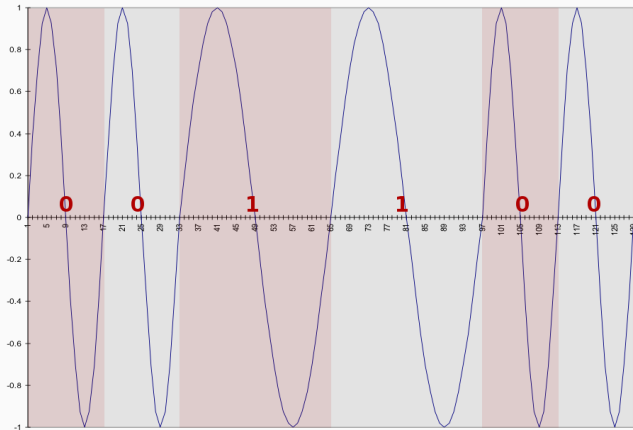
The carrier wave's **amplitude** is changed based on the digital signal

# Frequency (FSK)



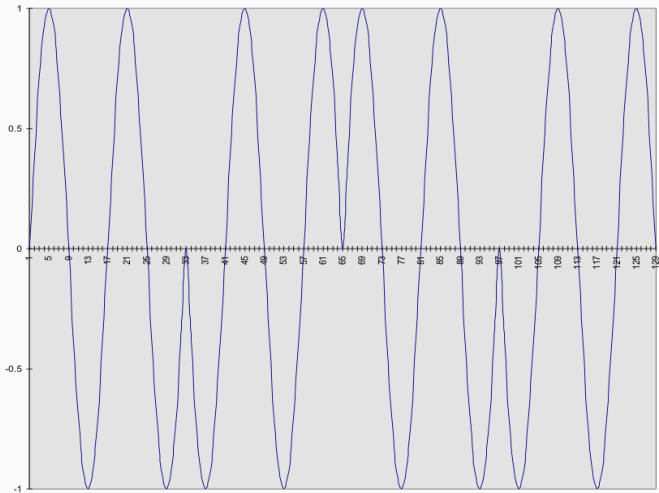
The carrier wave's **frequency** is changed based on the digital signal

# Frequency (FSK)



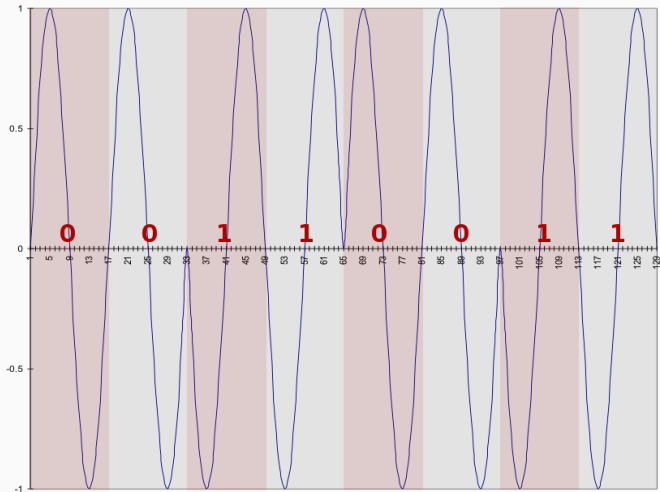
The carrier wave's **frequency** is changed based on the digital signal

# Phase (PSK)



The carrier wave's **phase** is changed based on the digital signal

# Phase (PSK)



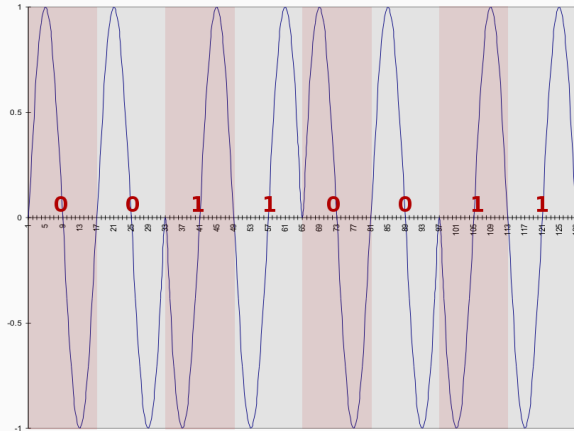
The carrier wave's **phase** is changed based on the digital signal

# Properties: ASK, FSK, and PSK

- Some important things to note...
- ASK is much more susceptible to noise than FSK or PSK
  - noise usually affects amplitude more than frequency or phase
- FSK needs to use two frequencies
  - requires more bandwidth than ASK or PSK for same amount of data
- PSK can carry more information than ASK or FSK...

# Phase (PSK)

PSK can be used to represent data in two ways,

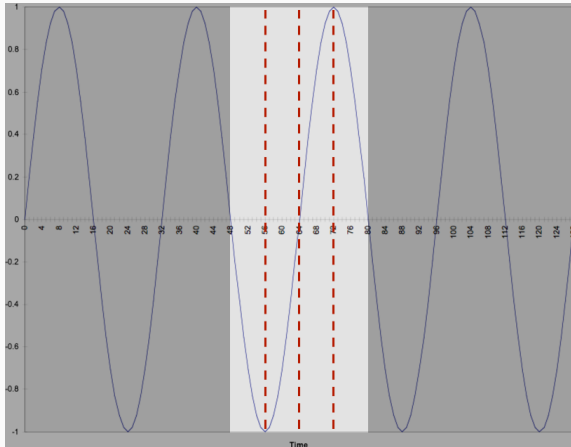


the first is to use the basic phase change  
to signal the change in value



# Phase (PSK)

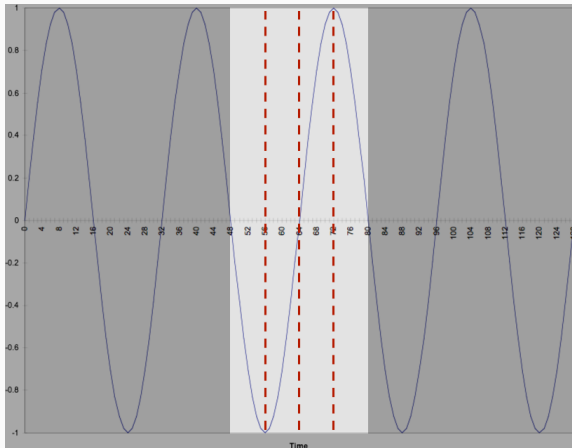
PSK can be used to represent data in two ways,



the second is to use the amount of shift  
to signal the change in value

# Phase (PSK)

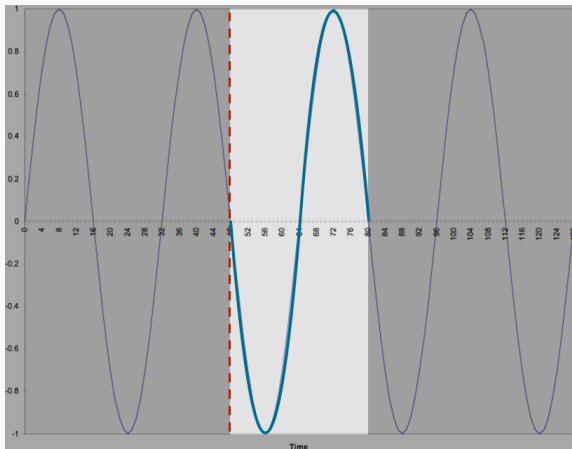
Here, for example, if we split the wave into quarters



we can have four values derived from how much we shifted it

# Phase (PSK)

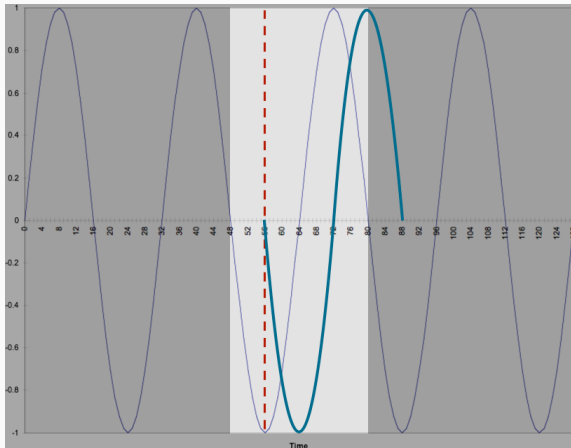
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# Phase (PSK)

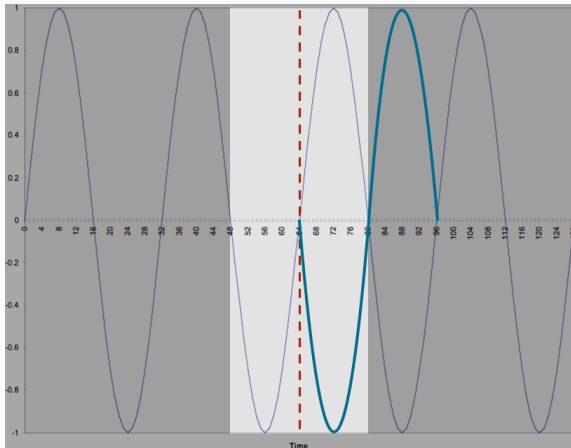
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# Phase (PSK)

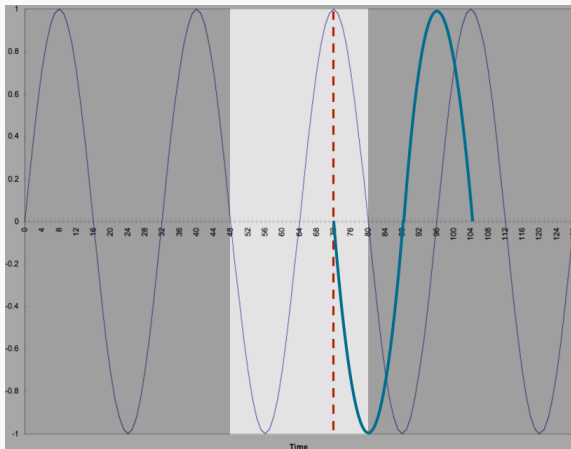
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# Phase (PSK)

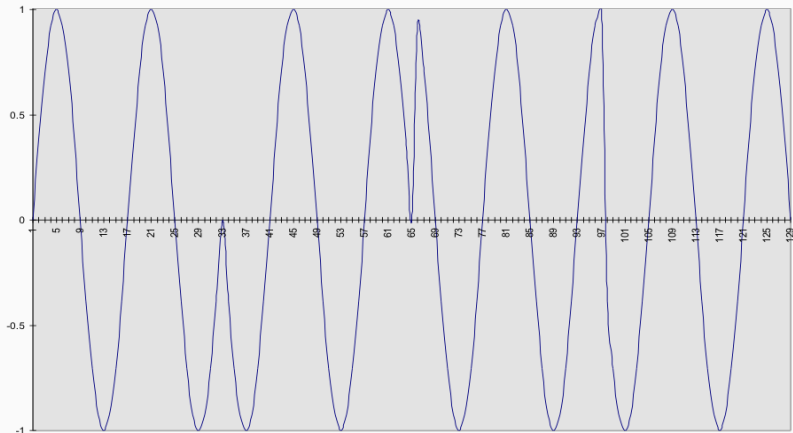
Here, for example, if we split the wave into quarters



we can have four values derived from how much we shifted it

# 4-PSK

This is known as 4-PSK (or Quadrature PSK, QPSK)

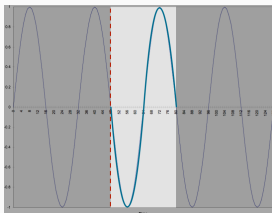


There is also 8-PSK, 16-PSK, etc.

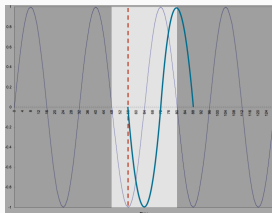
# 4-PSK

There are four possible signal events,  
so they can be used to represent two bits:

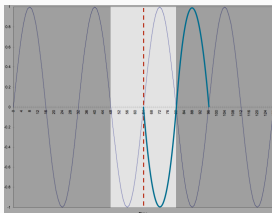
00



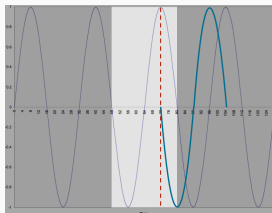
01



10



11



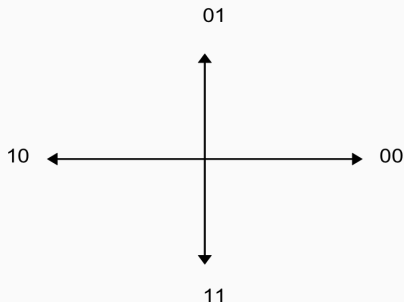


There are four possible signal events,  
so they can be used to represent two bits:

|    |             |             |
|----|-------------|-------------|
| 00 | $0^\circ$   | no change   |
| 01 | $90^\circ$  | $1/4$ shift |
| 10 | $180^\circ$ | $1/2$ shift |
| 11 | $270^\circ$ | $3/4$ shift |

# 4-PSK Constellation Diagram

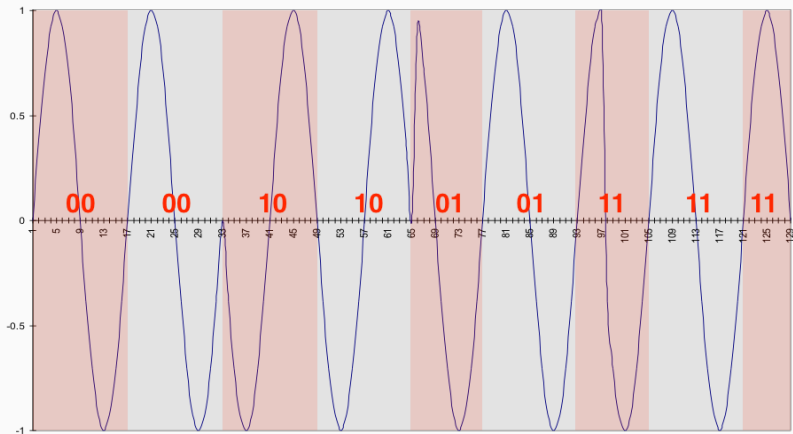
The four signal events can be plotted as a circle,  
a 'Constellation Diagram':



Warning: there are lots of different kinds of constellation diagrams!

# 4-PSK

Adding one more degree of freedom means  
we can transmit twice as much data



# Bit and Baud Rate

- **Bit rate:** the number of bits transmitted per second ( $\text{bit s}^{-1}$ )
- **Baud rate:** the number of signalling events per second (Bd)
- 4-PSK shows the difference between bit rate and baud rate
  - a 1 kHz signal using 4-PSK has:
    - bit rate:  $2000 \text{ bit s}^{-1} \rightarrow 2 \text{ kbit s}^{-1}$
    - baud rate:  $1000 \text{ Bd} \rightarrow 1 \text{ kBd}$
- The bit rate *can* be greater than the baud rate if each signalling event delivers more than one bit

# Nyquist's Theorem

Ignoring the effects of noise, the maximum channel capacity that can be achieved on a channel with bandwidth  $B$  and  $M$  possible signalling levels is:

$$2 \times B \log_2 M \text{ bit s}^{-1}$$

(we will come back to this next lecture...)

$$\log_a x = b$$

If  $a^b = x$ ,  
then  $b$  is the logarithm of  $x$  to the base  $a$ :

$$2^3 = 8 \rightarrow \log_2 8 = 3$$

$$10^2 = 100 \rightarrow \log_{10} 100 = 2$$

# Logarithms

$$a^m \times a^n = a^{(m+n)}$$

$$\left. \begin{array}{l} a^m = x \\ a^n = y \end{array} \right\} \quad x \times y = a^{m+n}$$

$$\left. \begin{array}{l} m = \log_a x \\ n = \log_a y \end{array} \right\} \quad \log_a(x \times y) = m + n$$

$$\log_a x + \log_a y = \log_a(x \times y)$$

# Logarithms and Division

When dealing with division:

$$\log(x/y) = \log x - \log y$$

$$\log(1/x) = -\log x$$

(you can work all of these out in relation to the indices rules)



Some other things to know:

$$\log 1 = 0$$

$$\log_a a = 1$$

(you can work all of these out in relation to the indices rules)

# Logarithms

To convert from one base to another use:

$$\log_a x = \frac{\log_b x}{\log_b a}$$

Divide the multiplier ( $x$ ) by the base ( $a$ ),  
both multiplied by a common log of an alternative base ( $b$ )

# Logarithms

To convert from one base to another use:

$$\log_a x = \log_b x / \log_b a$$

Since calculators usually have logs to the base 10 (and e), we can always find a logarithm to an arbitrary base by using:

$$\log_a x = \log_{10} x / \log_{10} a$$

$$\text{e.g. } \log_2 10000 = \frac{\log_{10} 10000}{\log_{10} 2} = \frac{4}{\log_{10} 2} = \frac{4}{0.30103} = 13.29$$

# The important things to remember:

- DTEs and DCEs
- Modems, modulation, and demodulation:
  - amplitude (ASK), frequency (FSK), phase (PSK, 4-PSK)
  - constellation diagrams
- Understand the difference between bit and baud rate
- Know Nyquist's Theorem and its implications for channel capacity

# Logarithms crib sheet

$$\log_a x = b$$

If  $a^b = x$ ,  
then  $b$  is the logarithm of  $x$  to the base  $a$

Special cases:

$$\log 1 = 0$$

$$\log_a a = 1$$

Useful tricks:

$$\log_a x + \log_a y = \log_a (x \times y)$$

$$\log(x/y) = \log x - \log y$$

$$\log(1/x) = -\log x$$

More on Data Transmission...  
(Back to) Nyquist, bandwidth, and the PSTN