





VisRec: A Hands-on Tutorial on Deep Learning for Visual Recommender Systems Session 5: ACF

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Attentive Collaborative Filtering: Multimedia Recommendation with Item- and Component-Level Attention

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or ACF

Context

Multimedia recommendation.

Explicit feedback is not always available.

Rely on implicit users interactions.

Key Insights

- Two levels of implicit feedback:
 - Item level
 - Component Level

• Leverage (hierarchical) attention mechanism to weight the importance of an item/component in each level.

Approach

BPR [4] based training.

• Latent factor model + neighbourhood model.

Originally tested in Pinterest and Vine datasets.

In this tutorial we test it on the Wikimedia dataset.

Model

User *i*, parametrized as \mathbf{u}_i Item *l,j*, parametrized as \mathbf{v}_j Component *m* of item *l* \mathbf{v}_j \mathbf{p}_l

Implementation Detail: $v_j = p_l$ was used for efficiency and better performance.

Model

User representation

item level attention

$$\mathbf{u}_i + \sum_{l \in \mathcal{R}(i)} \alpha(i, l) \mathbf{p}_l.$$
consumed item / by user i

Estimated score

$$\hat{R}_{ij} = \left(\mathbf{u}_i + \sum_{l \in \mathcal{R}(i)} \alpha(i, l) \mathbf{p}_l\right)^T \mathbf{v}_j.$$

Implementation Detail: Limited the profile to a maximum of 9 items per user.

models/acf.py

@ class ACF



Model logic

```
class ACF(nn.Module):
    def init (self,
                 users,
                 items,
                 feature_path,
                 model dim=128,
                 input_feature_dim=0,
                 tied_item_embedding=True,
                 device=None):
        super().__init__()
        self.pad token = 0
        self.device = device
       # Should be moved to an ACFRecommender
        self.users = users
        self.items = items
       self.feature_path = feature_path
        self.model_dim = model_dim
        self.input_feature_dim = input_feature_dim
        self.all items = torch.tensor(items)
        self.all_items = self.all_items + 1 if self.all_items.min() == 0 else self.all_items
        self.feature_data = self.load_feature_data(feature_path)
       num_items = max(self.all_items) + 1
        input feature dim = self.feature data.shape[-1]
        self.item_model = nn.Embedding(num_items, self.model_dim, padding_idx=self.pad_token)
        self.user_model = ACFUserNet(users,
                                     items,
                                     emb dim=self.model dim,
                                     input feature dim-input feature dim,
                                    profile_embedding=self.item_model,
                                     device=self.device)
```

models/acf.py

@ class ACF



Model logic

```
def forward(self, user_id, profile_ids, pos, neg, profile_mask):
    profile_features = self.get_features(profile_ids).to(self.device)

    user_output = self.user_model(user_id, profile_ids, profile_features, profile_mask)
    user = user_output['user']

    pos_pred = self.get_predictions(user, pos)
    neg_pred = self.get_predictions(user, neg)

    return pos_pred, neg_pred
```

```
def get_predictions(self, user, items):
    item_embeddings = self.item_model(items)
    prediction = self.score(user, item_embeddings)
    return prediction
```

```
def score(self, user, items):
    return (user * items).sum(1) / self.model_dim
```

user's
$$i$$
 factors item's $/$ weighted components
$$a(i,l) = \mathbf{w}_1^T \phi(\mathbf{W}_{1u}\mathbf{u}_i + \mathbf{W}_{1v}\mathbf{v}_l + \mathbf{W}_{1p}\mathbf{p}_l + \mathbf{W}_{1x}\mathbf{x}_l + \mathbf{b}_1) + \mathbf{c}_1.$$
 item's $/$ factors bias terms

$$\alpha(i,l) = \frac{exp(a(i,l))}{\sum_{n \in \mathcal{R}(i)} exp(a(i,n))}.$$

user's
$$i$$
 factors item's $/$ weighted components
$$a(i,l) = \mathbf{w}_1^T \phi(\mathbf{W}_{1u}\mathbf{u}_i) + \mathbf{W}_{1v}\mathbf{v}_l + \mathbf{W}_{1p}\mathbf{p}_l + \mathbf{W}_{1x}\mathbf{\bar{x}}_l + \mathbf{b}_1) + \mathbf{c}_1.$$
 item's $/$ factors bias terms

$$\alpha(i,l) = \frac{exp(a(i,l))}{\sum_{n \in \mathcal{R}(i)} exp(a(i,n))}.$$

user's
$$i$$
 factors
$$a(i,l) = \mathbf{w}_1^T \phi(\mathbf{W}_{1u}\mathbf{u}_i + \mathbf{W}_{1v}\mathbf{v}_l + \mathbf{W}_{1p}\mathbf{p}_l) + \mathbf{W}_{1x}\mathbf{x}_l + \mathbf{b}_1) + \mathbf{c}_1.$$
 item's l factors bias terms

$$\alpha(i,l) = \frac{exp(a(i,l))}{\sum_{n \in \mathcal{R}(i)} exp(a(i,n))}.$$

user's
$$i$$
 factors
$$a(i,l) = \mathbf{w}_1^T \phi(\mathbf{W}_{1u}\mathbf{u}_i + \mathbf{W}_{1v}\mathbf{v}_l + \mathbf{W}_{1p}\mathbf{p}_l + \mathbf{W}_{1x}\mathbf{x}_l + \mathbf{b}_1) + \mathbf{c}_1.$$
item's l weighted components bias terms

$$\alpha(i,l) = \frac{exp(a(i,l))}{\sum_{n \in \mathcal{R}(i)} exp(a(i,n))}.$$

user's
$$i$$
 factors
$$a(i,l) = \mathbf{w}_1^T \phi(\mathbf{W}_{1u}\mathbf{u}_i + \mathbf{W}_{1v}\mathbf{v}_l + \mathbf{W}_{1p}\mathbf{p}_l + \mathbf{W}_{1x}\mathbf{x}_l + \mathbf{b}_1) + \mathbf{c}_1.$$
item's l weighted components bias terms

$$\alpha(i,l) = \frac{exp(a(i,l))}{\sum_{n \in \mathcal{R}(i)} exp(a(i,n))}.$$

models/acf.py

@ class ACFUserNet



User level logic

```
class ACFUserNet(nn.Module):
    Get user embedding accounting to surpassed items
    def init (self, users, items, emb dim=128, input feature dim=0, profile embedding=None, device=None):
        super(). init ()
        self.pad_token = 0
        self.emb dim = emb dim
        num users = max(users) + 1
        num_items = max(items) + 1
        reduced_feature_dim = emb_dim
        self.feats = ACFFeatureNet(emb_dim, input_feature_dim, reduced_feature_dim) if input_feature_dim > 0 else None
        self.user_embedding = nn.Embedding(num_users, emb_dim)
        if not profile_embedding:
            self.profile embedding = nn.Embedding(num_items, emb_dim, padding_idx=self.pad_token)
            self.profile embedding = profile embedding
        f = 1 if self.feats is not None else 0
        self.w u = nn.Linear(emb dim, emb dim)
        self.w_v = nn.Linear(emb_dim, emb_dim)
        self.w_p = nn.Linear(emb_dim, emb_dim)
        self.w_x = nn.Linear(emb_dim, emb_dim)
        self.w = nn.Linear(emb_dim, 1)
        self._kaiming_(self.w_u)
        self._kaiming_(self.w_v)
        self._kaiming_(self.w_p)
        self. kaiming (self.w_x)
        self._kaiming_(self.w)
```

models/acf.py

@ class ACFUserNet



User level logic

```
def forward(self, user ids, profile ids, features, profile mask, return component attentions=False,
            return profile attentions=False, return attentions=False):
   user = self.user embedding(user ids)
    profile = self.profile_embedding(profile_ids)
   features = features.flatten(start_dim=2, end_dim=3) # Add
    feat_output = self.feats(user, features, profile_mask, return_attentions=return_component_attentions)
    components = feat_output['pooled_features']
    user = self.w u(user)
    profile_query = self.w_p(profile)
    components = self.w_x(components)
    profile query = profile query.permute((1,0,2))
    components = components.permute((1,0,2))
    alpha = F.relu(user + profile_query + components) # TODO: + item, Add curent_item emb (?)
   alpha = self.w(alpha)
    profile_mask = profile_mask.permute((1,0))
    profile_mask = profile_mask.unsqueeze(-1)
    alpha = alpha.masked_fill(torch.logical_not(profile_mask), float('-inf'))
    alpha = F.softmax(alpha, dim=0)
    alpha = alpha.permute((1,0,2))
   user_profile = (alpha * profile).sum(dim=1)
   user = user + user_profile
   output = {'user': user}
   if return component attentions:
        output['component_attentions'] = feat_output['attentions']
   if return_profile_attentions:
        output['profile attentions'] = alpha.squeeze(-1)
    return output
```

models/acf.py

@ class ACFUserNet

User & profile latent factors

```
def forward(self, user ids, profile ids, features, profile mask, return component attentions=False,
            return profile attentions=False, return attentions=False):
    user = self.user embedding(user ids)
    profile = self.profile_embedding(profile_ids)
   features = features.flatten(start_dim=2, end_dim=3) # Add
    feat_output = self.feats(user, features, profile_mask, return_attentions=return_component_attentions)
    components = feat_output['pooled_features']
    user = self.w u(user)
    profile_query = self.w_p(profile)
    components = self.w_x(components)
    profile query = profile query.permute((1,0,2))
    components = components.permute((1,0,2))
    alpha = F.relu(user + profile_query + components) # TODO: + item, Add curent_item emb (?)
    alpha = self.w(alpha)
    profile_mask = profile_mask.permute((1,0))
    profile_mask = profile_mask.unsqueeze(-1)
   alpha = alpha.masked_fill(torch.logical_not(profile_mask), float('-inf'))
    alpha = F.softmax(alpha, dim=0)
    alpha = alpha.permute((1,0,2))
    user profile = (alpha * profile).sum(dim=1)
   user = user + user_profile
   output = {'user': user}
   if return component attentions:
        output['component_attentions'] = feat_output['attentions']
   if return_profile_attentions:
        output['profile attentions'] = alpha.squeeze(-1)
    return output
```

models/acf.py

@ class ACFUserNet

Item represented as weighted components

```
def forward(self, user ids, profile ids, features, profile mask, return component attentions=False,
            return profile attentions=False, return attentions=False):
    user = self.user embedding(user ids)
   profile = self.profile_embedding(profile_ids)
   features = features.flatten(start_dim=2, end_dim=3) # Add
    feat_output = self.feats(user, features, profile_mask, return_attentions=return_component_attentions)
    components = feat_output['pooled_features']
    user = self.w u(user)
    profile_query = self.w_p(profile)
    components = self.w_x(components)
    profile query = profile query.permute((1,0,2))
    components = components.permute((1,0,2))
    alpha = F.relu(user + profile_query + components) # TODO: + item, Add curent_item emb (?)
    alpha = self.w(alpha)
    profile_mask = profile_mask.permute((1,0))
    profile_mask = profile_mask.unsqueeze(-1)
    alpha = alpha.masked_fill(torch.logical_not(profile_mask), float('-inf'))
    alpha = F.softmax(alpha, dim=0)
    alpha = alpha.permute((1,0,2))
    user profile = (alpha * profile).sum(dim=1)
   user = user + user_profile
   output = {'user': user}
   if return component attentions:
        output['component_attentions'] = feat_output['attentions']
   if return_profile_attentions:
        output['profile attentions'] = alpha.squeeze(-1)
    return output
```

models/acf.py

@ class ACFUserNet

```
def forward(self, user ids, profile ids, features, profile mask, return component attentions=False,
            return profile attentions=False, return attentions=False):
    user = self.user embedding(user ids)
    profile = self.profile_embedding(profile_ids)
    features = features.flatten(start dim=2, end dim=3) # Add
    feat_output = self.feats(user, features, profile_mask, return_attentions=return_component_attentions)
    components = feat_output['pooled_features']
    user = self.w u(user)
   profile_query = self.w_p(profile)
    components = self.w_x(components)
   profile query = profile query.permute((1,0,2))
    components = components.permute((1,0,2))
   alpha = F.relu(user + profile_query + components) # TODO: + item, Add curent_item emb (?)
   alpha = self.w(alpha)
   profile_mask = profile_mask.permute((1,0))
   profile_mask = profile_mask.unsqueeze(-1)
   alpha = alpha.masked_fill(torch.logical_not(profile_mask), float('-inf'))
   alpha = F.softmax(alpha, dim=0)
   alpha = alpha.permute((1,0,2))
    user_profile = (alpha * profile).sum(dim=1)
   user = user + user_profile
   output = {'user': user}
   if return component attentions:
       output['component_attentions'] = feat_output['attentions']
   if return_profile_attentions:
       output['profile attentions'] = alpha.squeeze(-1)
    return output
```

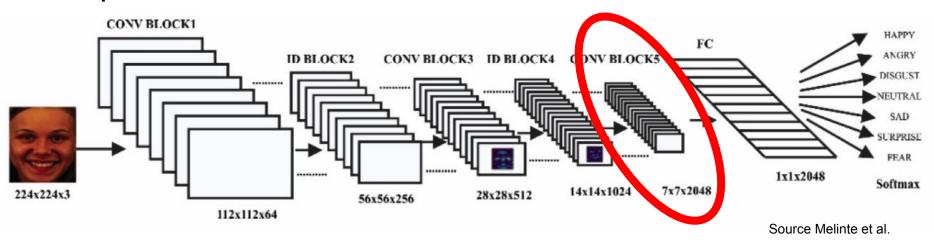
models/acf.py

@ class ACFUserNet

User representation formation

```
def forward(self, user ids, profile ids, features, profile mask, return component attentions=False,
            return profile attentions=False, return attentions=False):
    user = self.user embedding(user ids)
    profile = self.profile_embedding(profile_ids)
   features = features.flatten(start_dim=2, end_dim=3) # Add
    feat_output = self.feats(user, features, profile_mask, return_attentions=return_component_attentions)
    components = feat_output['pooled_features']
    user = self.w u(user)
    profile_query = self.w_p(profile)
    components = self.w_x(components)
    profile query = profile query.permute((1,0,2))
    components = components.permute((1,0,2))
    alpha = F.relu(user + profile_query + components) # TODO: + item, Add curent_item emb (?)
    alpha = self.w(alpha)
    profile_mask = profile_mask.permute((1,0))
    profile_mask = profile_mask.unsqueeze(-1)
   alpha = alpha.masked_fill(torch.logical_not(profile_mask), float('-inf'))
    alpha = F.softmax(alpha, dim=0)
   alpha = alpha.permute((1,0,2))
   user_profile = (alpha * profile).sum(dim=1)
    user = user + user profile
    vulput - 1 user : users
    if return component attentions:
       output['component_attentions'] = feat_output['attentions']
   if return_profile_attentions:
       output['profile attentions'] = alpha.squeeze(-1)
    return output
```

Components



Implementation detail:

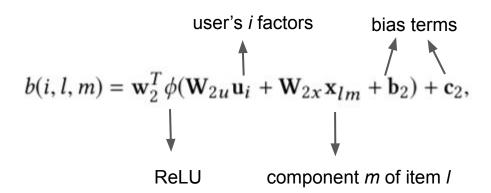
Used the output of the *layer4* of a ResNet50 [2] for this tutorial.

Add layer to reduce dimension of each feature vector.

Component Level Attention

Weighted components for item / component level attention

$$\overline{\mathbf{x}}_{l} = \sum_{m=1}^{|\{\mathbf{x}_{l*}\}|} \beta(i, l, m) \cdot \mathbf{x}_{lm},$$



Component Level Attention

It's an attention after all

$$\beta(i, l, m) = \frac{exp(b(i, l, m))}{\sum_{n=1}^{|\{\mathbf{x}_{l*}\}|} exp(b(i, l, n))}.$$

```
models/acf.py
```

@ class ACFFeatureNet



Component level logic

```
class ACFFeatureNet(nn.Module):
   Process auxiliary item features into latent space.
   All items for user can be processed in batch.
    def __init__(self, emb_dim, input_feature_dim, feature_dim, hidden_dim=None, output_dim=None):
        super(). init ()
        ...
        self.dim_reductor = nn.Linear(input_feature_dim, feature_dim)
        self.w_x = nn.Linear(feature_dim, hidden_dim)
        self.w_u = nn.Linear(emb_dim, hidden_dim)
        self.w = nn.Linear(hidden_dim, 1)
        self._kaiming_(self.w_x)
        self._kaiming_(self.w_u)
        self. kaiming (self.w)
```

models/acf.py

@ class ACFFeatureNet



Component level logic

```
def forward(self, user, components, profile_mask, return_attentions=False):
    x = self.dim_reductor(components) # Add
    x = x.movedim(0, -2) # BxPxHxD => PxHxBxD
    x_{tilde} = self.w_x(x)
   user = self.w_u(user)
    beta = F.relu(x_tilde + user)
    beta = self.w(beta)
    beta = F.softmax(beta, dim=1)
    x = (beta * x).sum(dim=1)
    x = x.movedim(-2, 0) # PxBxD => BxPxD
    feature dim = x.shape[-1]
    profile_mask = profile_mask.float()
    profile_mask = profile_mask.unsqueeze(-1).expand((*profile_mask.shape, feature_dim))
    x = profile_mask * x
    output = {'pooled_features': x}
    if return_attentions:
        output['attentions'] = beta.squeeze(-1).squeeze(-1)
    return output
```

models/acf.py

@ class ACFFeatureNet

Dimensionality reduction

```
def forward(self, user, components, profile mask, return attentions=False):
   x = self.dim_reductor(components) # Add
    X = X:IIIOVEUIII(V, -Z) # DXFXNXV -> FXNXDXV
   x_{tilde} = self.w_x(x)
   user = self.w_u(user)
   beta = F.relu(x_tilde + user)
   beta = self.w(beta)
   beta = F.softmax(beta, dim=1)
   x = (beta * x).sum(dim=1)
   x = x.movedim(-2, 0) # PxBxD => BxPxD
   feature_dim = x.shape[-1]
   profile_mask = profile_mask.float()
   profile_mask = profile_mask.unsqueeze(-1).expand((*profile_mask.shape, feature_dim))
   x = profile_mask * x
   output = {'pooled_features': x}
   if return_attentions:
       output['attentions'] = beta.squeeze(-1).squeeze(-1)
   return output
```

models/acf.py

@ class ACFFeatureNet

Component-Level Attention

```
def forward(self, user, components, profile_mask, return_attentions=False):
    x = self.dim_reductor(components) # Add
   x = x.movedim(0, -2) # BxPxHxD => PxHxBxD
    x_{tilde} = self.w_x(x)
    user = self.w_u(user)
    beta = F.relu(x_tilde + user)
    beta = self.w(beta)
    beta = F.softmax(beta, dim=1)
    x = (beta * x).sum(dim=1)
    x = x.movedim(-2, 0) \# PxBxD => BxPxD
    feature dim = x.shape[-1]
    profile_mask = profile_mask.float()
    profile_mask = profile_mask.unsqueeze(-1).expand((*profile_mask.shape, feature_dim))
   x = profile_mask * x
    output = {'pooled_features': x}
    if return_attentions:
        output['attentions'] = beta.squeeze(-1).squeeze(-1)
    return output
```

Training

BPR [4] Optimization Objective

$$\arg\min_{\mathbf{U},\mathbf{V}} \sum_{(i,j,k)\in\mathcal{R}_B} -\ln\sigma(\hat{R}_{ij} - \hat{R}_{ik}) + \lambda(||\mathbf{U}||^2 + ||\mathbf{V}||^2),$$

Trained using Adam

Implementation detail:

Regularization was key to increase performance as well as to avoid flat attentions.

 $0 < \lambda < 1e$ -4 worked, with 1e-5 achieving the best results.

trainers/acf_trainer.py

@ class ACFTrainer



Training logic

```
class ACFTrainer():
   Handles training process
   def __init__(self, model, datasets, loss, optimizer, version, batch_size=100, device=None,
                max_profile_size=9, checkpoint_dir=None):
       Parameters
       model: initialized UserNet
       dataset: initialized MovieLens
       loss: one of the warp functions
       optimizer: torch.optim
       run_name: directory to save results
       batch_size: number of samples to process for one update
       device: gpu or cpu
       self.pad token = 0
       self.version = version
       self.epoch = 0
       self.best loss = np.inf
       self.loss = loss
       self.optimizer = optimizer
       self.batch_size = batch_size
       self.device = get device(device)
       self.model = model
       self.model = self.model.to(self.device)
       self.train, self.test = datasets
       self.all items = self.preprocess inputs(self.train.items, to tensor=True)
       self.train_loader = DataLoader(self.train, batch_size=batch_size, shuffle=True,
                                      collate_fn=generate_collate_fn(max_profile_size), num_workers=8)
       self.test loader = DataLoader(self.test, batch size=batch size, shuffle=True,
                                     collate_fn=generate_collate_fn(max_profile_size), num_workers=1)
```

```
trainers/acf_trainer.py
```

@ class ACFTrainer



Training logic

```
def fit(self, num_epochs, k=10):
   num train_batches = len(self.train) / self.batch_size
   num_test_batches = len(self.test) / self.batch_size
   for epoch in tqdm(range(num_epochs)):
       self.epoch = epoch
       for phase in ['train', 'val']:
           self.logger.epoch(epoch, phase)
           self.model.train(phase == 'train')
           loss = 0
           cur step = 0
           if phase == 'train':
               t = tqdm(self.train_loader)
               for batch in t:
                    self.optimizer.zero_grad()
                   cur loss = self.training step(batch)
                   self.optimizer.step()
                   loss += cur_loss
                   cur step += 1
                   avg_loss = loss / cur_step
                   t.set_description(f"Average Loss {avg_loss:.4f}")
                    t.refresh()
               loss /= num_train_batches
               self.logger.metrics(loss, 0, epoch, phase)
               with torch.no_grad():
                    for batch in tqdm(self.test_loader):
                        cur_loss = self.validation_step(batch)
                       loss += cur loss
                    loss /= num test batches
                    # self.logger.metrics(loss, self.score(k=k), epoch, phase)
                    self.logger.metrics(loss, 0.0, epoch, phase)
                    if loss < self.best loss:
                       self.best_loss = loss
                        self.logger.save(self.state, epoch)
```

trainers/acf_trainer.py

@ class ACFTrainer

trainers/loss.py

Weston, J., Bengio, S., & Usunier, N. (2011). Wsabie: Scaling up to large vocabulary image annotation.

```
def training_step(self, batch):
    user_id, profile_ids, pos, neg = self.preprocess_inputs(*batch)
    profile_mask = self.get_profile_mask(profile_ids)
    pos_pred, neg_pred = self.model(user_id, profile_ids, pos, neg, profile_mask)

loss = self.loss(pos_pred, neg_pred)
    loss.backward()
    return loss.item()
```

```
def bpr_loss(pos, neg, b=0.0, collapse=True):
    res = torch.sigmoid(neg - pos + b)
    if collapse:
        res = res.mean()
    return res

def warp_loss(pos, neg, b=1, collapse=True):
    loss = bpr_loss(pos, neg, b, collapse=False)
    m = (loss > 0.5).float()
    m *= torch.log(m.sum() + 1) + 1
    res = m * loss
    if collapse:
        res = res.mean()
    return res
```

Main Results

AUC	RR	R@20	P@20	nDCG@20	R@100	P@100	nDCG@100
0.80409	0.01594	0.05473	0.00273	0.02127	0.14935	0.00149	0.03781

Let's go to colab!









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References

- [1] Chen, J., Zhang, H., He, X., Nie, L., Liu, W., & Chua, T. S. (2017, August). Attentive collaborative filtering: Multimedia recommendation with item-and component-level attention. In *Proceedings of the 40th International ACM SIGIR conference on Research and Development in Information Retrieval* (pp. 335-344).
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Supporting Material

General Implementation Details

Implemented using python 3.7.5 and pytorch 1.7.

Ran in research group cluster with 8-cpu and 2 GeForce GTX 1080 Ti (only one used per model training).

Each epoch took around 3 hours.

```
Input: User-item interaction matrix \mathbf{R}. Each item l is
     represented by a set of component features \{x_{l*}\}.
Output: Latent feature matrix U, V, P and parameters in
     attention model O

    Initialize U, V and P with Gaussian distribution. Initialize Θ

     with xavier [17].
 2: repeat
        draw (i, j, k) from \mathcal{R}_B
        For each item l in \mathcal{R}(i):
            For each component m in \{x_{I_+}\}:
 5:
                Compute \beta(i, l, m) according to Eqns. (10) and (11)
            Compute \bar{\mathbf{x}}_l according to Eqn. (12)
        Compute \alpha(i, l) according to Eqns. (8) and (9)
      \mathbf{u}_{i}' \leftarrow \mathbf{u}_{i} + \sum_{l \in \mathcal{R}(i)} \alpha(i, l) \mathbf{p}_{l}
10: \hat{R}_{ijk} \leftarrow \mathbf{u}_i' \mathbf{v}_j - \mathbf{u}_i' \mathbf{v}_k
       For each parameter \theta in \{U, V, P, \Theta\}:
11:
           Update \theta \leftarrow \theta + \eta \cdot (\frac{\exp^{-\hat{R}_{ijk}}}{1 + \exp^{-\hat{R}_{ijk}}} \cdot \frac{\partial \hat{R}_{ijk}}{\partial \theta} + \lambda \cdot \theta).
13: until convergence
14: return U, V, P and Θ.
```

```
Input: User-item interaction matrix \mathbf{R}. Each item l is
     represented by a set of component features \{x_{l*}\}.
Output: Latent feature matrix U, V, P and parameters in
     attention model \Theta
     Initialize U, V and P with Gaussian distribution. Initialize Θ
                                                                                                                 Kaiming was
     with xavier [17].
                                                                                                                 used
 2: repeat
        draw (i, j, k) from \mathcal{R}_B
        For each item l in \mathcal{R}(i):
            For each component m in \{x_{I_{+}}\}:
 5:
                Compute \beta(i, l, m) according to Eqns. (10) and (11)
            Compute \bar{\mathbf{x}}_I according to Eqn. (12)
        Compute \alpha(i, l) according to Eqns. (8) and (9)
       \mathbf{u}_{i}' \leftarrow \mathbf{u}_{i} + \sum_{l \in \mathcal{R}(i)} \alpha(i, l) \mathbf{p}_{l}
      \hat{R}_{ijk} \leftarrow \mathbf{u}_i' \mathbf{v}_j - \mathbf{u}_i' \mathbf{v}_k
        For each parameter \theta in \{U, V, P, \Theta\}:
11:
           Update \theta \leftarrow \theta + \eta \cdot (\frac{\exp^{-\hat{R}_{ijk}}}{1 + \exp^{-\hat{R}_{ijk}}} \cdot \frac{\partial \hat{R}_{ijk}}{\partial \theta} + \lambda \cdot \theta).
13: until convergence
14: return U, V, P and Θ.
```

```
Input: User-item interaction matrix \mathbf{R}. Each item l is
     represented by a set of component features \{x_{l*}\}.
Output: Latent feature matrix U, V, P and parameters in
     attention model O

    Initialize U, V and P with Gaussian distribution. Initialize Θ

     with xavier [17].
   repeat
                                                                                                                  Triplet sampling
        draw (i, j, k) from \mathcal{R}_B
                                                                                                                 originally bootstrap
                                                                                                                 sampling, we did it
        For each item l in \mathcal{R}(i):
                                                                                                                 without replacement
            For each component m in \{x_{I_{+}}\}:
                                                                                                                 for consistency.
                Compute \beta(i, l, m) according to Eqns. (10) and (11)
            Compute \bar{\mathbf{x}}_I according to Eqn. (12)
        Compute \alpha(i, l) according to Eqns. (8) and (9)
       \mathbf{u}_{i}' \leftarrow \mathbf{u}_{i} + \sum_{l \in \mathcal{R}(i)} \alpha(i, l) \mathbf{p}_{l}
       \hat{R}_{ijk} \leftarrow \mathbf{u}_i' \mathbf{v}_j - \mathbf{u}_i' \mathbf{v}_k
        For each parameter \theta in \{U, V, P, \Theta\}:
11:
           Update \theta \leftarrow \theta + \eta \cdot (\frac{\exp^{-\hat{R}_{ijk}}}{1 + \exp^{-\hat{R}_{ijk}}} \cdot \frac{\partial \hat{R}_{ijk}}{\partial \theta} + \lambda \cdot \theta).
```

13: until convergence14: return U, V, P and Θ.

```
Input: User-item interaction matrix \mathbf{R}. Each item l is
     represented by a set of component features \{x_{l*}\}.
Output: Latent feature matrix U, V, P and parameters in
     attention model O

    Initialize U, V and P with Gaussian distribution. Initialize Θ

     with xavier [17].
 2: repeat
        draw (i, j, k) from \mathcal{R}_B
        For each item l in \mathcal{R}(i):
            For each component m in \{x_{I_{+}}\}:
                                                                                                                  Component
                Compute \beta(i, l, m) according to Eqns. (10) and (11)
                                                                                                                  attention
            Compute \bar{\mathbf{x}}_I according to Eqn. (12)
        Compute \alpha(i, l) according to Eqns. (8) and (9)
        \mathbf{u}_{i}' \leftarrow \mathbf{u}_{i} + \sum_{l \in \mathcal{R}(i)} \alpha(i, l) \mathbf{p}_{l}
        \hat{R}_{ijk} \leftarrow \mathbf{u}_i' \mathbf{v}_j - \mathbf{u}_i' \mathbf{v}_k
        For each parameter \theta in \{U, V, P, \Theta\}:
11:
           Update \theta \leftarrow \theta + \eta \cdot (\frac{\exp^{-\hat{R}_{ijk}}}{1 + \exp^{-\hat{R}_{ijk}}} \cdot \frac{\partial \hat{R}_{ijk}}{\partial \theta} + \lambda \cdot \theta).
13: until convergence
14: return U, V, P and Θ.
```

```
Input: User-item interaction matrix \mathbf{R}. Each item l is
     represented by a set of component features \{x_{l*}\}.
Output: Latent feature matrix U, V, P and parameters in
     attention model O

    Initialize U, V and P with Gaussian distribution. Initialize Θ

     with xavier [17].
 2: repeat
        draw (i, j, k) from \mathcal{R}_B
        For each item l in \mathcal{R}(i):
            For each component m in \{x_{I*}\}:
                Compute \beta(i, l, m) according to Eqns. (10) and (11)
            Compute \bar{\mathbf{x}}_{l} according to Eqn. (12)
        Compute \alpha(i, l) according to Eqns. (8) and (9)
                                                                                                                  Item Attention
        \mathbf{u}_{i}' \leftarrow \mathbf{u}_{i} + \sum_{l \in \mathcal{R}(i)} \alpha(i, l) \mathbf{p}_{l}
        \hat{R}_{ijk} \leftarrow \mathbf{u}_i' \mathbf{v}_j - \mathbf{u}_i' \mathbf{v}_k
        For each parameter \theta in \{U, V, P, \Theta\}:
11:
            Update \theta \leftarrow \theta + \eta \cdot (\frac{\exp^{-\hat{R}_{ijk}}}{1 + \exp^{-\hat{R}_{ijk}}} \cdot \frac{\partial \hat{R}_{ijk}}{\partial \theta} + \lambda \cdot \theta).
13: until convergence
14: return U, V, P and Θ.
```

```
Input: User-item interaction matrix \mathbf{R}. Each item l is
    represented by a set of component features \{x_{l*}\}.
Output: Latent feature matrix U, V, P and parameters in
    attention model O

    Initialize U, V and P with Gaussian distribution. Initialize Θ

    with xavier [17].
 2: repeat
       draw (i, j, k) from \mathcal{R}_B
       For each item l in \mathcal{R}(i):
           For each component m in \{x_{I_{+}}\}:
              Compute \beta(i, l, m) according to Eqns. (10) and (11)
           Compute \bar{\mathbf{x}}_l according to Eqn. (12)
       Compute \alpha(i, l) according to Eqns. (8) and (9)
        \mathbf{u}_{i}' \leftarrow \mathbf{u}_{i} + \sum_{l \in \mathcal{R}(i)} \alpha(i, l) \mathbf{p}_{l}
        \hat{R}_{ijk} \leftarrow \mathbf{u}_i' \mathbf{v}_j - \mathbf{u}_i' \mathbf{v}_k
                                                                                                          Compute
       For each parameter \theta in \{U, V, P, \Theta\}:
                                                                                                          scores and
           Update \theta \leftarrow \theta + \eta \cdot (\frac{\exp^{-\hat{R}_{ijk}}}{1 + \exp^{-\hat{R}_{ijk}}})
                                                                                                          update model
                                                                                                          parameters
    until convergence
14: return U, V, P and Θ.
```