

Python Programming

Modulus Operator

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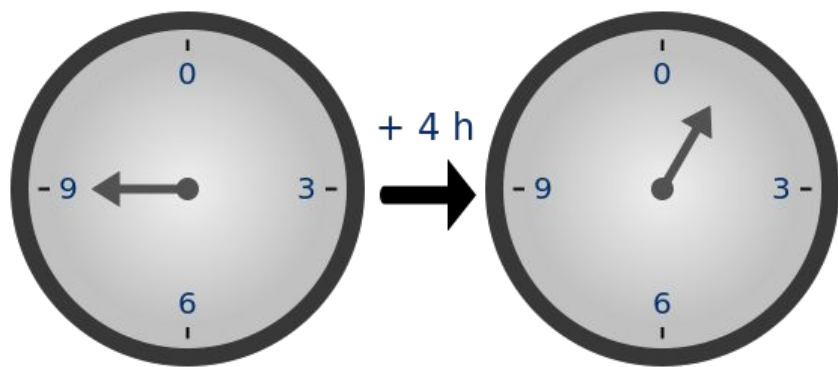
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Modulus operation



- Let's use **12-hour Clock Cycle**
- If it is 9 now, what time:
- after 12 h? Still 9
- after 4 h? 1
- after 16 ($4 + 12$) h? 1
- after 17 ($5 + 12$) h? 2
- after 29 ($5 + 2 \cdot 12$) h? 2
- before 24 ($2 \cdot 12$) h? 9
- before 25 ($1 + 2 \cdot 12$) h? 8
- **Every multiple of 12 is useless**

Modulus operation

- $a \bmod n = a \% n$ finds the remainder after division by n :
- let $a = 27$, $n = 12$, then $r = a \% n$?
- $27 / 12 = (2 \cdot 12 + 3) / 12 = 2 + 3 / 12 = 2.25$
 - 2 = Integer division part = called the quotient
 - Means we have maximum 2 multiples of 12 ($2 \cdot 12 = 24 \leq 27$)
 - 0.25 = fractional part
 - 3 (remainder) of division = $27 - 24$
- $27 \% 12 = 3 \Rightarrow$ Remainder of division (must be < 12)

Modulus operation

- $25 / 5 = 25/5 + 0/5 = 5$
 - $26 / 5 = 25/5 + \frac{1}{5} = 5.2$
 - $27 / 5 = 25/5 + \frac{2}{5} = 5.4$
 - $28 / 5 = 25/5 + \frac{3}{5} = 5.6$
 - $29 / 5 = 25/5 + \frac{4}{5} = 5.8$
 - $30 / 5 = 30/5 + 0/5 = 6$
- $25 \% 5 = 0$
 - $26 \% 5 = 1$
 - $27 \% 5 = 2$
 - $28 \% 5 = 3$
 - $29 \% 5 = 4$
 - $30 \% 5 = 0$
 - Answer must be < 5

Modulus operation

- let $a = 27$, $n = 7$, then $r = 27 \% 7$?
- $27 / 7 = (3*7 + 6)/7 = 3 + 6/7 = 3.85714285714$
 - $3 =$ Integer division part
 - Means we have maximum 3 multiples of 7 ($3*7 = 21$)
 - $0.85714285714 =$ fractional part
 - 6 (remainder) of division $= 27 - 21$

Modulus %2 and %10

- $100 \% 2 = (50*2 + 0) \Rightarrow 0$
- $101 \% 2 = (50*2 + 1) \Rightarrow 1$
- $108 \% 2 = (54*2 + 0) \Rightarrow 0$
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- $1000 \% 10 = (100*10 + 0) \Rightarrow 0$
- $1001 \% 10 = (100*10 + 1) \Rightarrow 1$
- $1008 \% 10 = (100*10 + 8) \Rightarrow 8$
- $1000 \% 100 = (10*100 + 0) \Rightarrow 0$
- $1234 \% 100 = (100*12 + 34) \Rightarrow 34$
- $1234 \% 1000 = (1000*1 + 234) \Rightarrow 234$
- $1234 \% 10000 = (10000*0 + 1234) \Rightarrow 1234$

- **Observations**

- Number % 2
 - 0 if number is even
 - Even number is divisible by 2
 - 1 for odd
- Number % 10 = last 1 digit
- Number % 100 = last 2 digits
- Number % 1000 = last 3 digits
- Number % 10000 = last 4 digits

Summary

- $\text{Num} \% 2 \Rightarrow$ can tell us if number is even or odd
- $\text{Num} \% 10 \Rightarrow$ gives us the last digit of num
- $\text{Num} / 10 \Rightarrow$ removes the last digit of num (integer division)
- $r = n \% k$ [r must be $< k$]

“Acquire knowledge and impart it to the people.”

“Seek knowledge from the Cradle to the Grave.”