

Data Structures

Heap Homework 1

Mostafa S. Ibrahim

Teaching, Training and Coaching since more than a decade!

Artificial Intelligence & Computer Vision Researcher

PhD from Simon Fraser University - Canada

Bachelor / Msc from Cairo University - Egypt

Ex-(Software Engineer / ICPC World Finalist)



Problem #1: Max-Heap

- In the lectures, we learned the min-heap
- Change the code to act as a MaxHeap
 - E.g. top returns the max
 - And pop() removes the max
- Test your code thoroughly

Problem #2: Max-Heap

- Can we build a simple MaxHeap of **integers** based on our existing MinHeap code?
- Find a way of using the MinHeap code to build a MaxHeap, without copy-pasting any code

```
class MinHeap:...
```

```
class MaxHeap:  
    def __init__(self, lst):  
        self.minHeap = ...
```

```
    def push(self, key):...
```

```
    def top(self):...
```

```
    def empty(self):...
```

```
    def pop(self):...
```

Problem #3: Find smaller values

- Implement `def smallest_than(self, value):`
 - Returns a list of all the values in the minHeap less than this value
 - Order of the returned list doesn't matter

```
lst = [2, 17, 22, 10, 8, 37, 14,  
       19, 7, 6, 5, 12, 25, 30]  
minHeap = MinHeap(lst)  
  
print(minHeap.smallest_than(10))  
# [2, 5, 7, 6, 8]
```

Problem #4: Is Heap

- `def is_heap(self)`
- Extend your MinHeap class with the above function
- It returns a true if the current internal array in the heap is still a min heap

```
lst = [2, 17, 22, 10, 8, 37, 14,  
       19, 7, 6, 5, 12, 25, 30]  
minHeap = MinHeap(lst)
```

```
assert minHeap.is_heap()
```

```
minHeap.array[0], minHeap.array[-1] = minHeap.array[-1], minHeap.array[0]  
assert not minHeap.is_heap()
```

Problem #5: Heap Sort

- `def sort_heap(self)`
- Extend your MinHeap class with the above function
- It sorts the heap's internal array **in-place** from small to large
 - In-place means this array will be used to do the sort without using/creating another array
 - After the call, the heap array is not heap anymore (just sorted array)
- The function should be $O(n \log n)$

```
lst = [2, 17, 22, 10, 8, 37, 14,
       19, 7, 6, 5, 12, 25, 30]
minHeap = MinHeap(lst)

minHeap.sort_heap()
# [2, 5, 6, 7, 8, 10, 12, 14,
#  17, 19, 22, 25, 30, 37]

print(minHeap.array)
```

“Acquire knowledge and impart it to the people.”

“Seek knowledge from the Cradle to the Grave.”