## 1 The problem

This is a problem 82 from Project Euler.

#### 2 Definitions

```
import Control.Monad (replicateM)
import Data.List (transpose, minimumBy)
import Data.Ord (comparing)
import Data.Maybe (catMaybes)

type Point = (Int, Int)
type Path = [Point]
```

# 3 Preparations

Program is going to read a matrix of integers from stdin:

```
unrow :: String \to \lceil String \rceil
unrow \ s = \mathbf{let} \ (l, s') = break \ (\in [', ', ', ']) \ s
  in l: case s' of
     \begin{array}{l} [\ ] \rightarrow [\ ] \\ (\_\colon s'') \rightarrow unrow \ s'' \end{array}
parseMatrix :: [String] \rightarrow [[Int]]
parseMatrix\ cont = map\ (map\ read \circ unrow)\ cont
readByLine :: IO [String]
readByLine = \mathbf{do}\ l \leftarrow getLine
  let cnt = length (unrow l)
   ls \leftarrow replicateM (cnt - 1) getLine
   return (l:ls)
main :: IO()
main = \mathbf{do} \ lns \leftarrow readByLine
   let matrix = parseMatrix lns
   print matrix
   print "Let's solve shit"
  print (minimalSum matrix)
```

### 4 Solution

 $\textit{minimalSum } \textit{mt} = \textit{minimumBy } (\textit{comparing } \textit{snd}) \ \$ \ \textit{map } (\lambda i \rightarrow \textit{minimalSumFromPos } (i, 0) \ [] \ \textit{mt}) \ [0 \ .$ 

```
minimalSumFromPos :: Point \rightarrow Path \rightarrow [[Int]] \rightarrow (Path, Int)
minimalSumFromPos(x, y) = mt \mid y \equiv length \ mt - 1 = ([(x, y)], (mt !! x) !! y)
minimalSumFromPos(x, y) were mt = ((x, y) : fst mins, current + snd mins)
  where current = (mt !! x) !! y
     mins = \mathbf{if} \ avaiables \equiv []
       then ([], 0)
       else minimumBy (comparing snd) avaiables
     avaiables = catMaybes [up, down, right]
     up = tryPos(x + 1, y)
     down = tryPos(x-1, y)
     right = tryPos(x, y + 1)
     max_d = length mt
     tryPos(x\theta, y\theta) \mid (x\theta, y\theta) \in were = Nothing
     tryPos(x\theta, y\theta) \mid x\theta < 0 \lor y\theta < 0 = Nothing
     tryPos(x0, y0) \mid x0 \geqslant max\_d \lor y0 \geqslant max\_d = Nothing
     tryPos(x0, y0) = Just $ minimalSumFromPos(x0, y0)((x, y) : were) mt
```

Okay, that's pretty slow. Let's try dynamic programming.

## 5 Dynamic Programming