



S. Rinzivillo – rinzivillo@isti.cnr.it

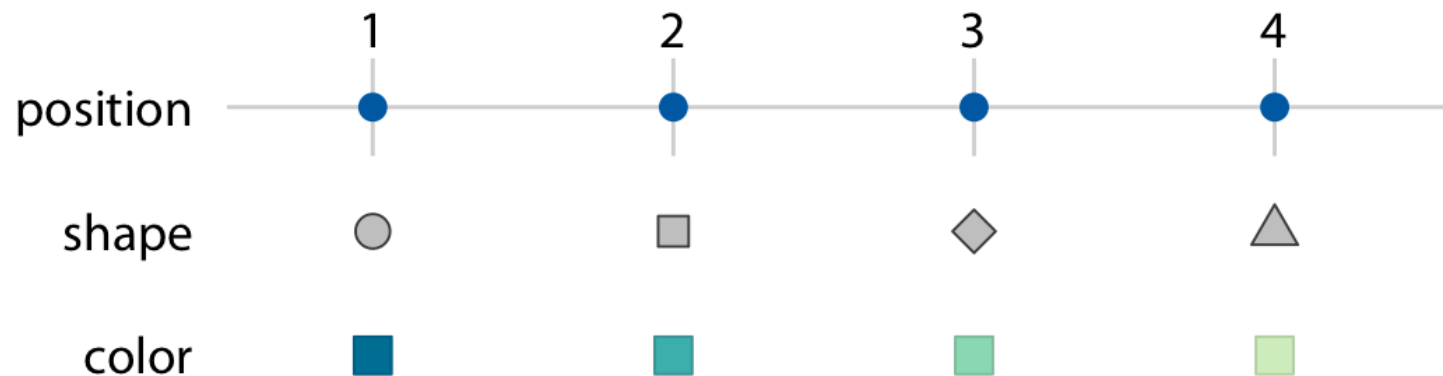
DATA VISUALIZATION AND VISUAL ANALYTICS



SCALES FUNCTION

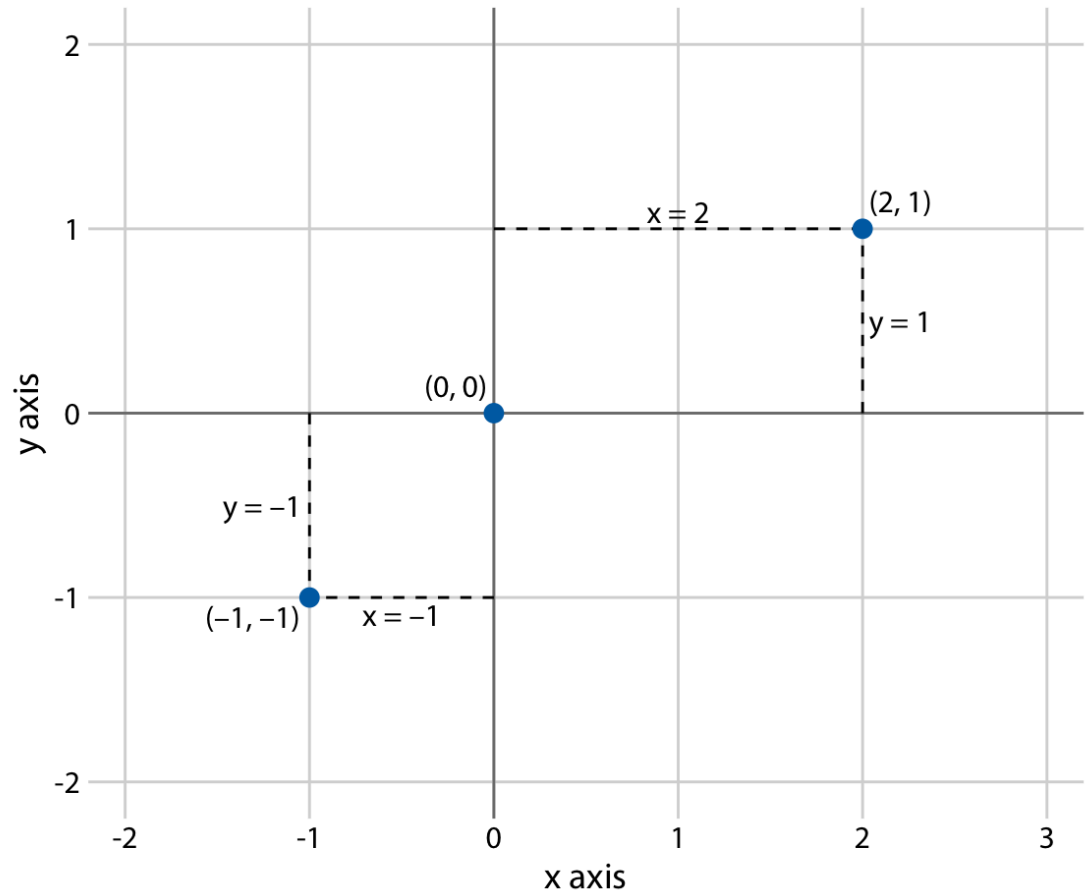
Map data to VV

- We specify a scaling function to map data values to the visual representation
- A **scale** is a unique mapping between data and visual representation
- Scales are **functions** that map from an **input domain** to an **output range**

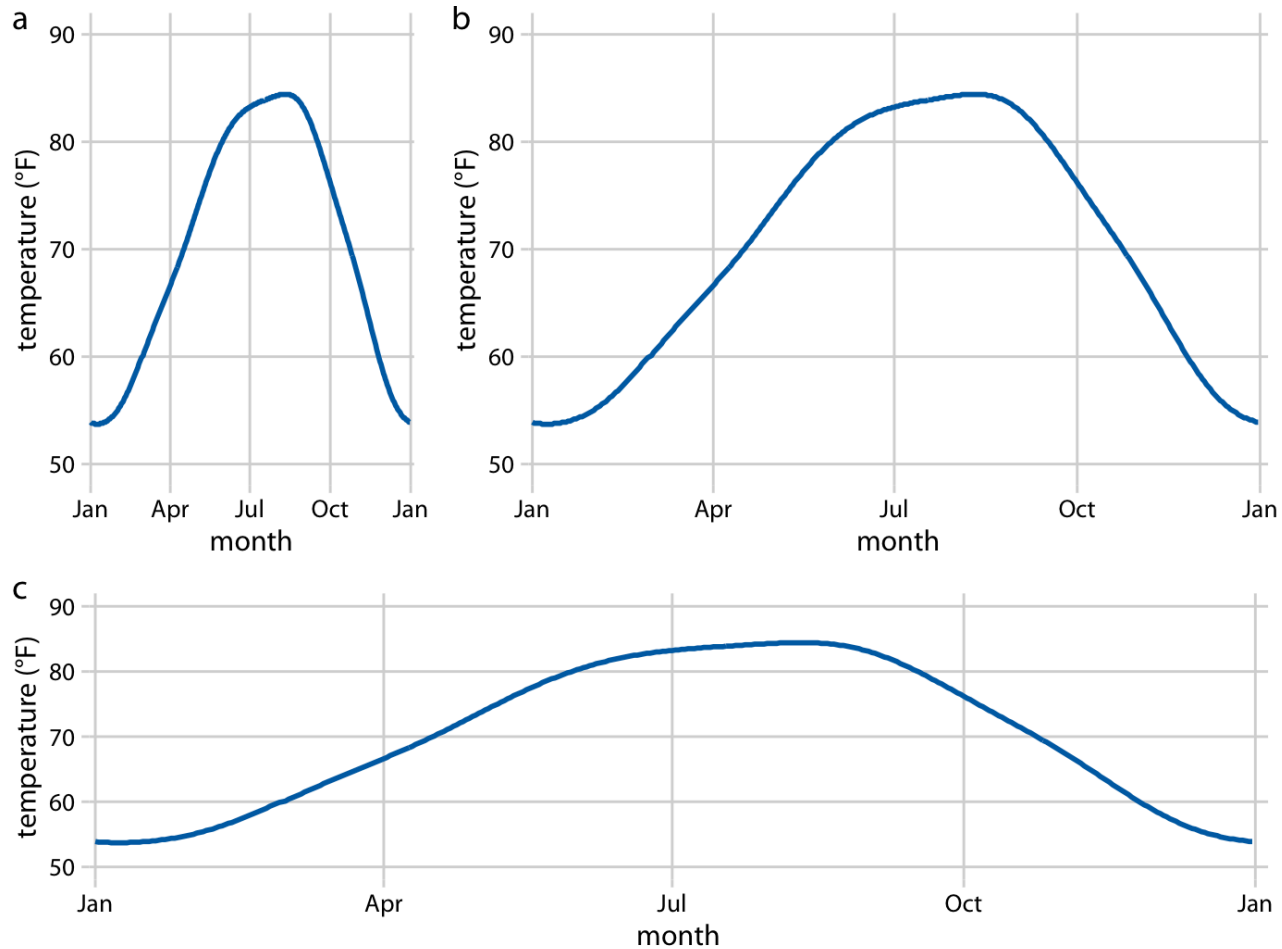


Positional scales: axis

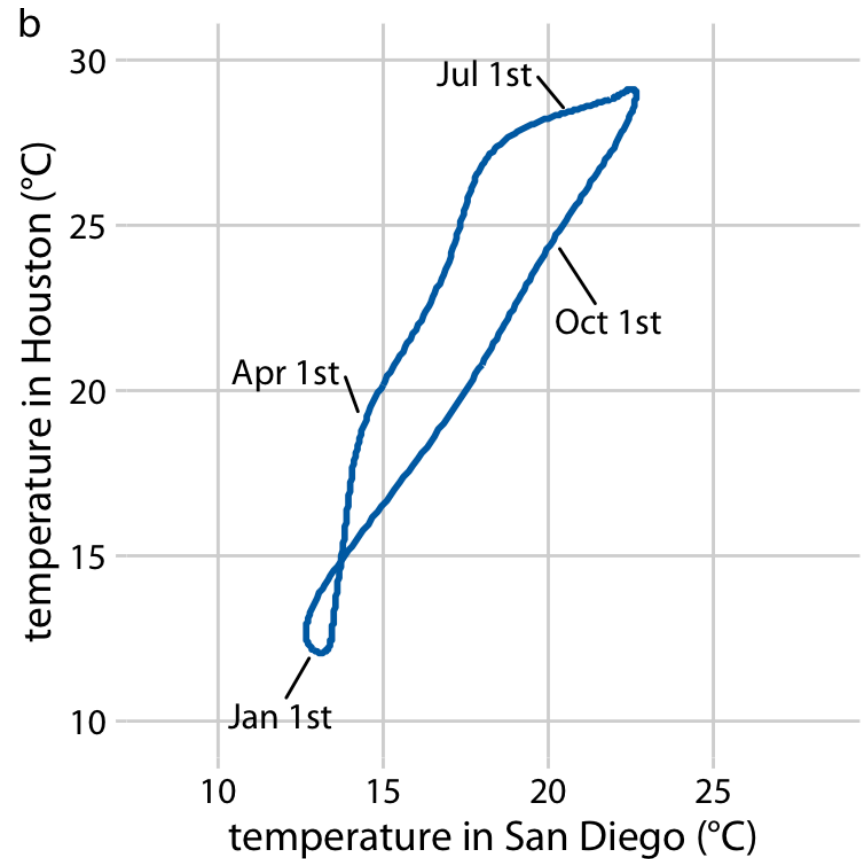
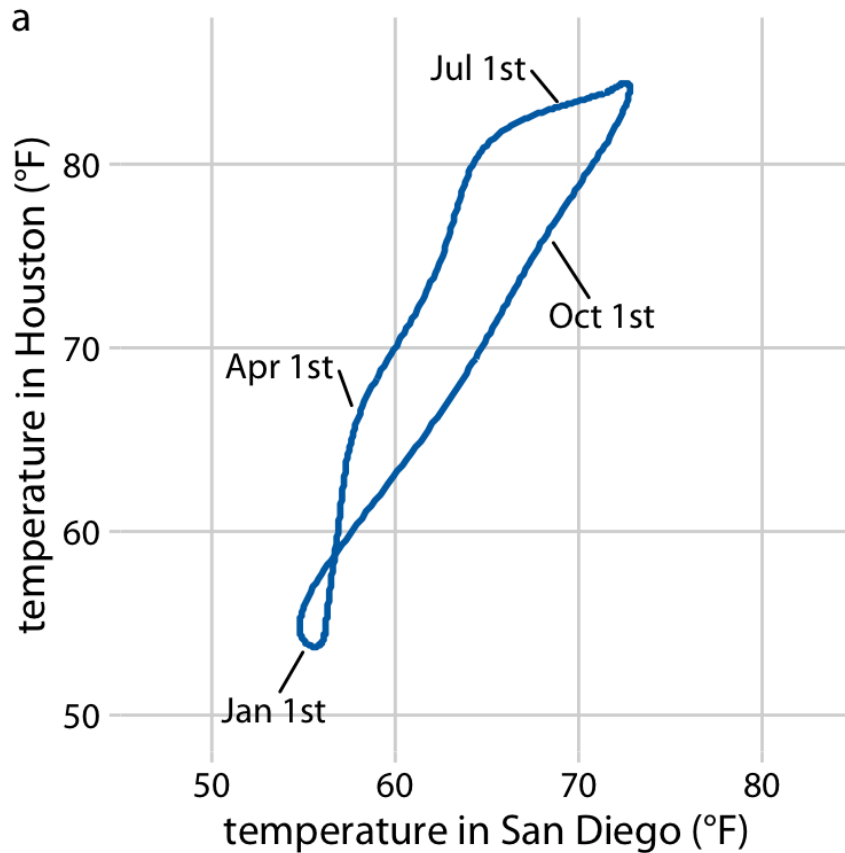
- Axis are at the base of many scientific plots
- Cartesian coordinate systems are composed of two orthogonal axis
- Values are positioned proportionally on the axes



Cartesian diagram with different scales

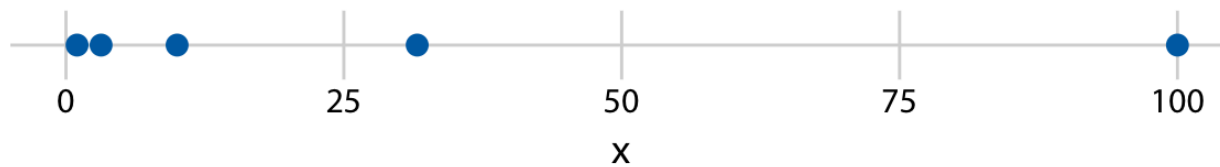


Cartesian axes with same scale

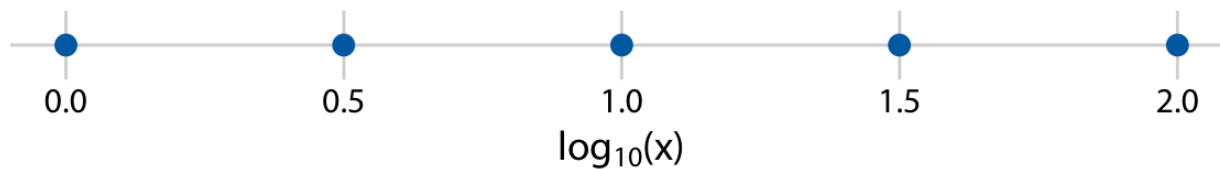


Non linear axes

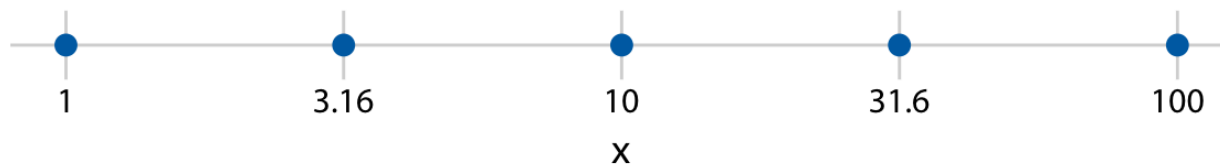
original data, linear scale



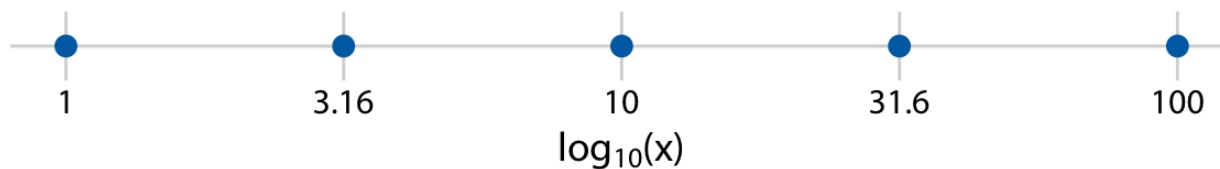
log-transformed data, linear scale



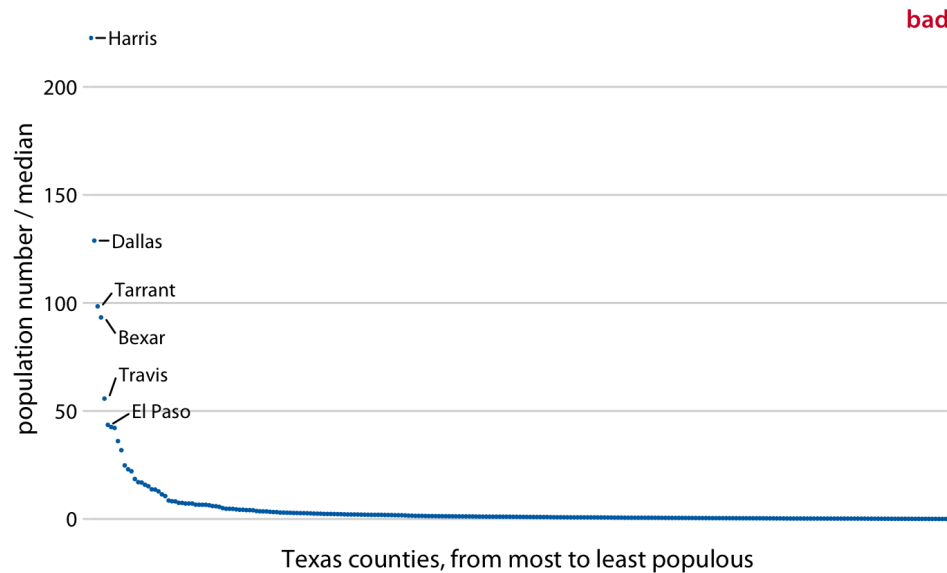
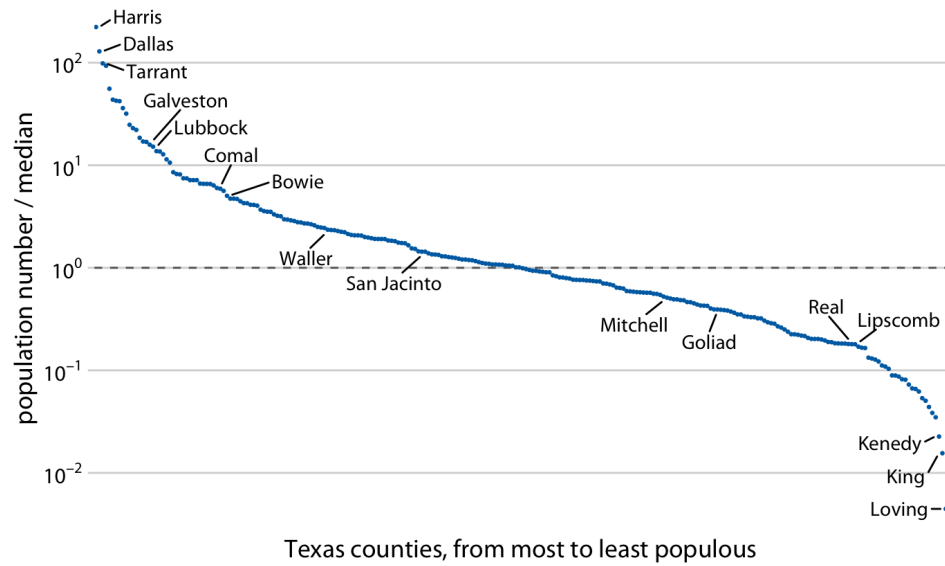
original data, logarithmic scale



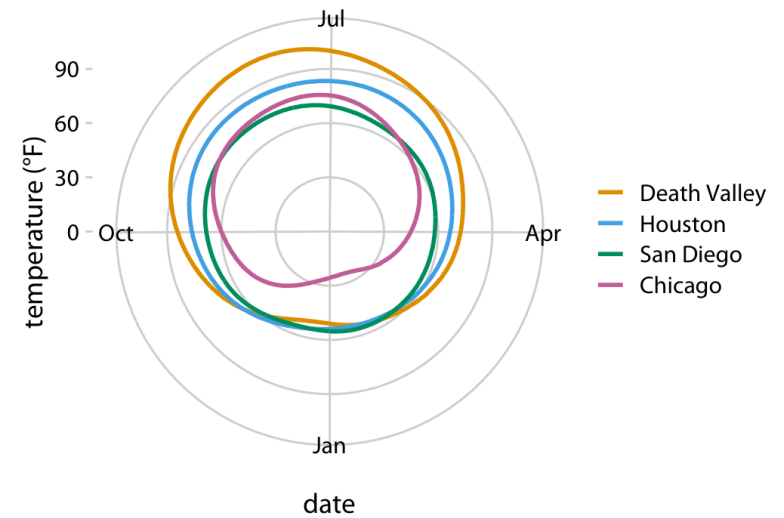
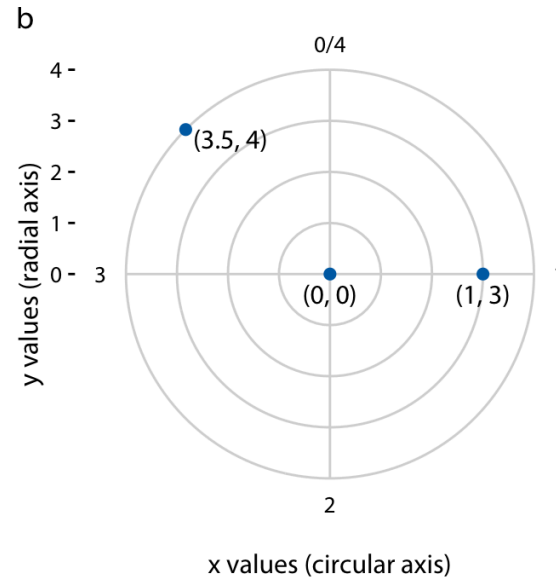
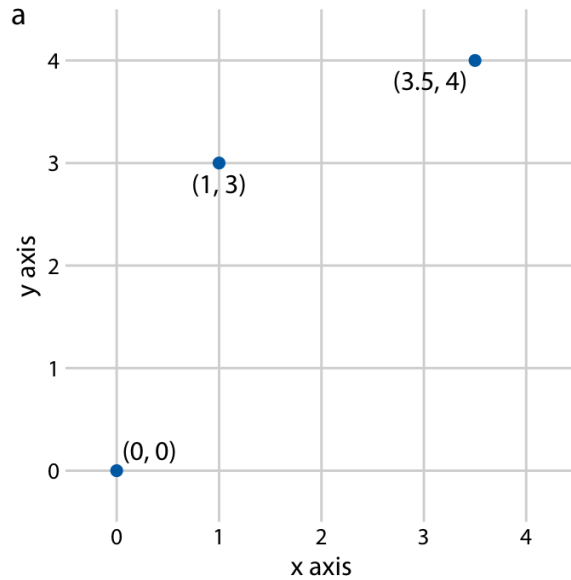
logarithmic scale with incorrect axis title



Non linera axes



Curved axes



Example

Table 2.2: First 12 rows of a dataset listing daily temperature normals for four weather stations. Data source: NOAA.

Month	Day	Location	Station ID	Temperature
Jan	1	Chicago	USW00014819	25.6
Jan	1	San Diego	USW00093107	55.2
Jan	1	Houston	USW00012918	53.9
Jan	1	Death Valley	USC00042319	51.0
Jan	2	Chicago	USW00014819	25.5
Jan	2	San Diego	USW00093107	55.3
Jan	2	Houston	USW00012918	53.8
Jan	2	Death Valley	USC00042319	51.2
Jan	3	Chicago	USW00014819	25.3
Jan	3	San Diego	USW00093107	55.3
Jan	3	Death Valley	USC00042319	51.3
Jan	3	Houston	USW00012918	53.8

Ordinal

Ordinal

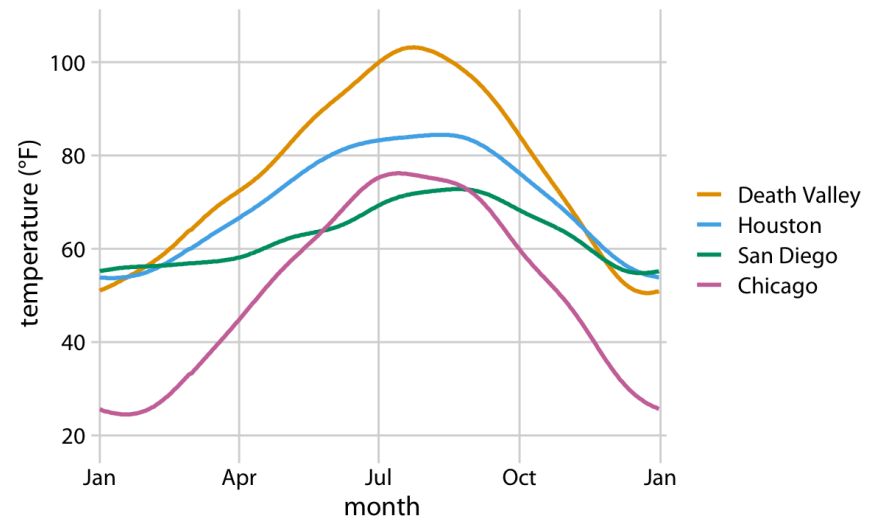
Nominal

Nominal

Quantitative

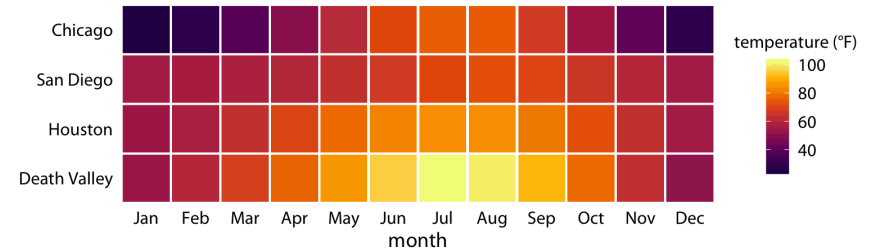
Example

- Temperature (quantitative) on a linear axis (y)
- Month and day (ordinal) on a linear axis (x)
- City (nominal) on a color hue scale



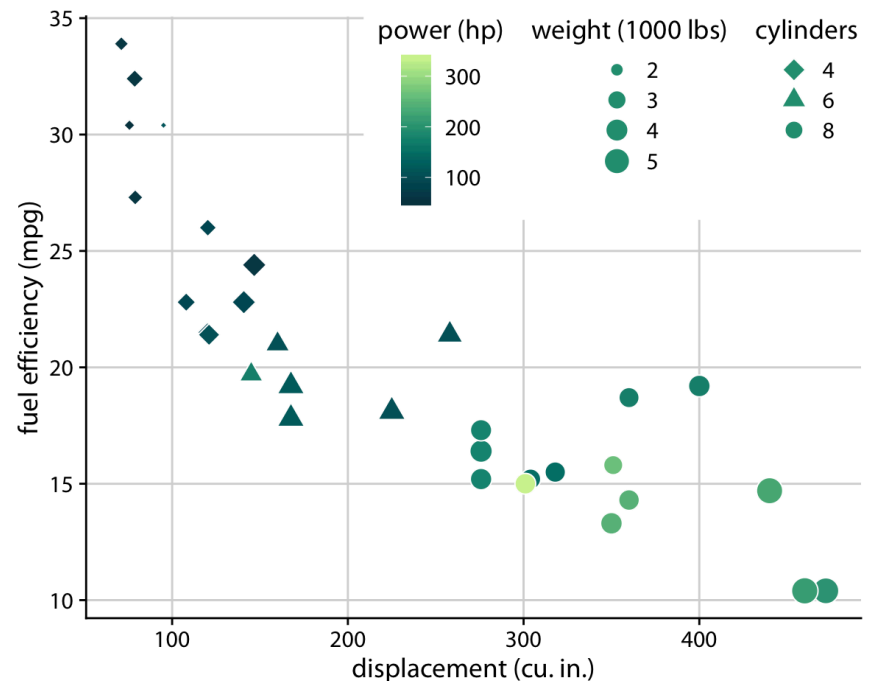
Example

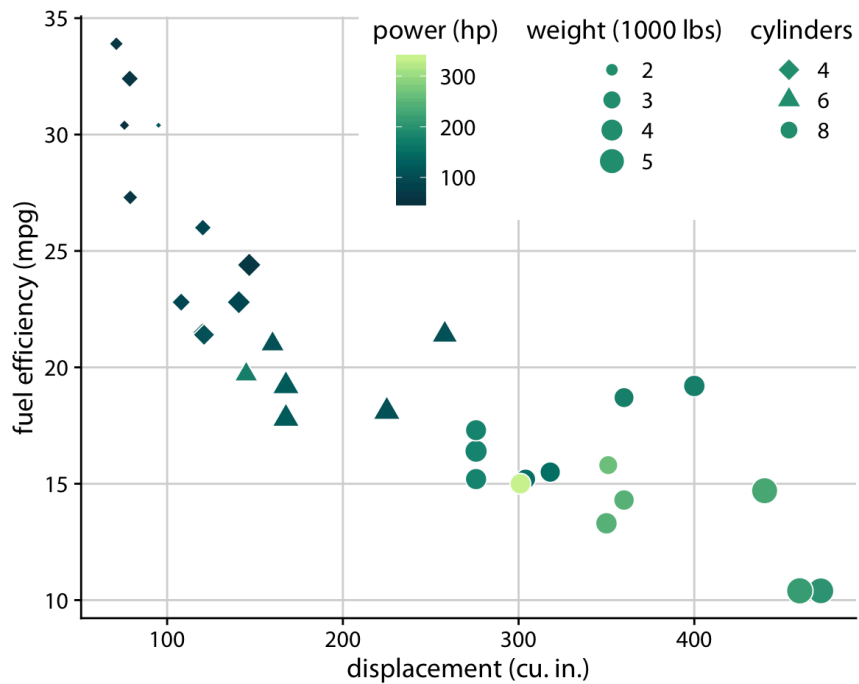
- Month (ordinal) on a ordinal axis (x)
- City (nominal) on a ordinal axis (y) (order determined on sum of temperatures on the line)
- Temperature (quantitative) on a color scale



Example

- Displacement (quantitative) on linear axis (x)
- Fuel efficiency (quantitative) on linear axis (y)
- Power (quantitative) on lineal color scale
- Weight (quantitative -> ordinal) on ~~linear~~ squared size scale
- Cylinders (ordinal -> nominal) on shape scale



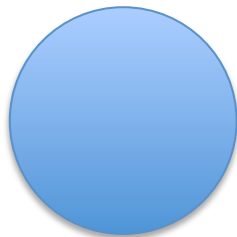


weight (1000 lbs)



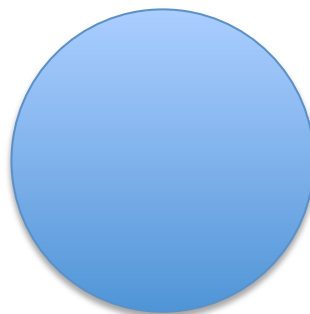
$$r=2$$

$$A = 4 \cdot \pi$$



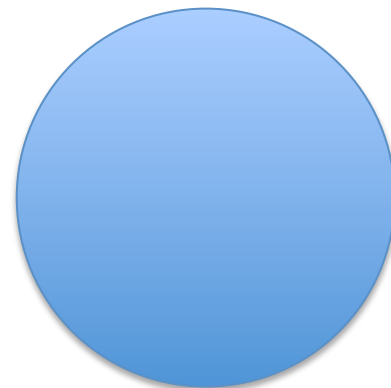
$$r=3$$

$$A = 9 \cdot \pi$$



$$r=4$$

$$A = 16 \cdot \pi$$

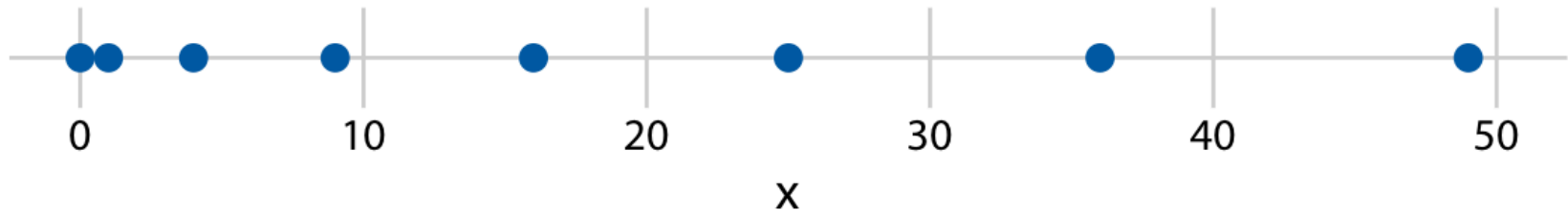


$$r=5$$

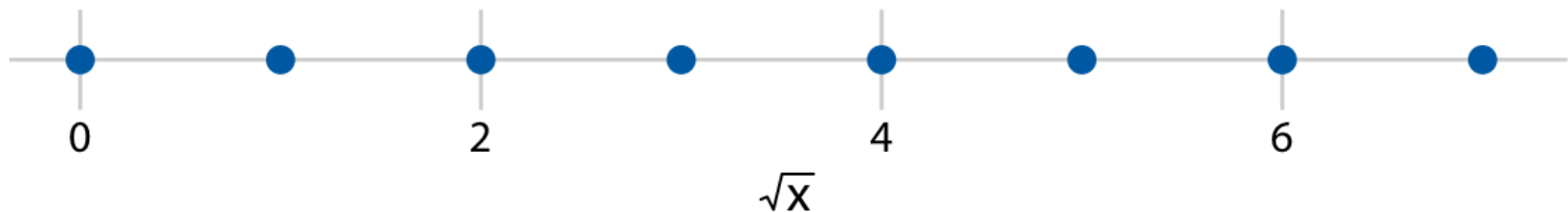
$$A = 25 \cdot \pi$$

Non linear axes

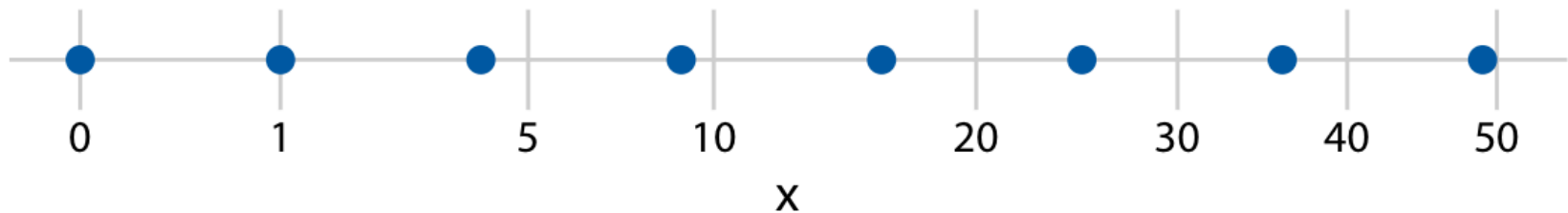
original data, linear scale



square-root-transformed data, linear scale

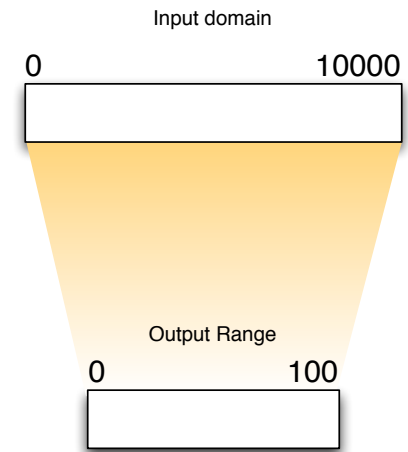


original data, square-root scale



Manual Mapping

1. For input domain
 1. Select the largest number in original interval (10000)
 2. Select the smallest number in original interval (0)
 3. Select the difference of the two values (10000)
 2. For output range
 1. Select the largest number in the new interval (100)
 2. Select the minimum number in the new interval (0)
 3. Select the difference of the two values (100)
 3. Compute the ratio of the two intervals' range
($10000/100 = 100$)
- This is an example of a linear scaling
 - $y = mx + b$, where $b=0$ and $m=1/100$
 - 100 units in the original interval correspond to 1 unit in the destination interval



An example – an alternative solution

```
join.enter()  
  .append("rect")  
  .attr("x", function(d,i){  
    return i*barw;  
  })  
  .attr("y",function(d){  
    return height - d*4;  
  })  
  .attr("width", barw)  
  .attr("height",function(d){  
    return d*4;  
  });
```

```
join.enter()  
  .append("rect")  
  .attr("x", function(d,i){  
    return x(i);  
  })  
  .attr("y",function(d){  
    return y(d);  
  })  
  .attr("width", barw)  
  .attr("height",function(d){  
    return h(d);  
  });  
function x(d){return m*d + b};  
function y(d){return m'*d + b'};  
function h(d){return m''*d + b''};
```

D3.js Scales generator

- D3 provides several scale types
 - Quantitative
 - Continuous
 - Identity
 - Linear ($y=mx+b$)
 - Power ($y=mx^k+b$)
 - Log ($y=m \log(x) + b$)
 - Discrete
 - Quantize
 - Quantile
 - Threshold
 - Ordinal
 - Time

Creating a scale

```
var scale = d3.scaleLinear();
```

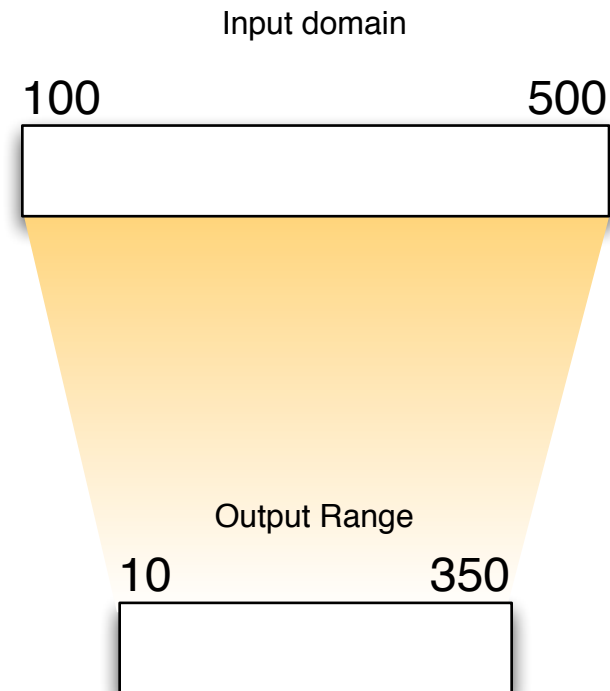
- Default scale uses
 - Domain is [0,1]
 - Range is [0,1]
 - Function is Identity
 - `scale(2.5);` //returns 2.5

Creating a scale – setting domain and range

```
var scale = d3.scaleLinear()  
  .domain([100, 500])  
  .range([10, 350]);
```

- Default scale uses

- `scale(100);` //returns 10
- `scale(300);` //returns 180
- `scale(500);` //returns 350



Quantitative power scale – circle radius

Previous example

```
g.append("circle")
  .attr("fill", "pink")
  .attr("stroke", "red")
  .attr("r", function(d){
    return Math.sqrt(d*100);
  })
```

Refined solution

```
var r = d3.scaleSqrt()
  .domain([0,20])
  .range([0,30]);

g.append("circle")
  .attr("fill", "pink")
  .attr("stroke", "red")
  .attr("r", function(d){
    return r(d);
  })
```

Domains & Ranges

- Typically, domains are derived from data while ranges are constant.

```
var x = d3.scale.linear()  
  .domain([0, d3.max(numbers)])  
  .range([0, 720]);
```

```
var x = d3.scale.log()  
  .domain(d3.extent(numbers))  
  .range([0, 720]);
```

```
function value(d) { return d.value; }  
  
var x = d3.scale.log()  
  .domain(d3.extent(objects, value))  
  .range([0, 720]);
```

Utility functions: d3.min, d3.max, d3.extent

- To determine the domain and range interval we should know min and max of the two intervals
- D3.js provides utility functions to access such values
 - `d3.min(array[, accessor])`
 - `d3.max(array[, accessor])`
 - `d3.extent(array[, accessor])`

Utility Functions: examples

```
d3.min([10,30,40,70,100]) //returns 10  
d3.max([10,30,40,70,100]) //returns 100  
d3.extent([10,30,40,70,100]) //returns  
[10,100]
```


Interpolators

```
var x = d3.scaleLinear()  
  .domain([12, 24])  
  .range(["steelblue", "brown"]);  
  
x(16); // #666586
```

```
var x = d3.scaleLinear()  
  .domain([12, 24])  
  .range(["0px", "720px"]);  
  
x(16); // 240px
```

```
var x = d3.scaleLinear()  
  .domain([12, 24])  
  .range(["steelblue", "brown"])  
  .interpolate(d3.interpolateHsl);  
  
x(16); // #3cb05f
```

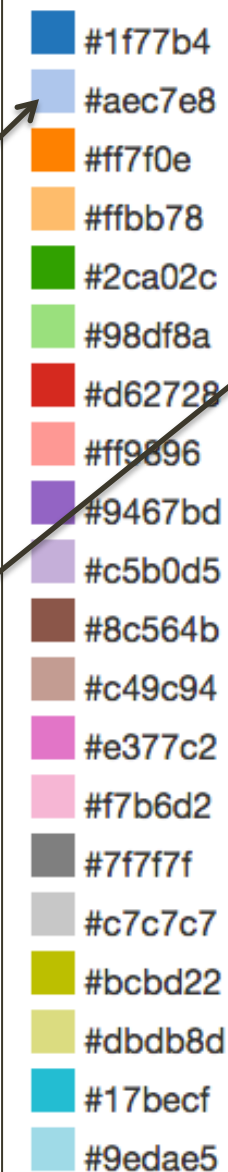
Ordinal Scales

```
var x = d3.scaleOrdinal()  
  .domain(["A", "B", "C", "D"])  
  .range([0, 10, 20, 30]);  
  
x("B"); // 10
```

```
var x = d3.scaleCategory20()  
  .domain(["A", "B", "C", "D"]);  
  
x("B"); // #aec7e8
```

```
var x = d3.scale.category20b()  
  .domain(["A", "B", "C", "D"]);  
  
x("E"); // #637939  
x.domain(); // A, B, C, D, E
```

category20



A vertical list of 20 color swatches, each with a corresponding hex code. The colors are arranged in a gradient from blue at the top to light blue at the bottom. An arrow points from the second color swatch (#aec7e8) to the code in the second code block.

#1f77b4
#aec7e8
#ff7f0e
#ffbb78
#2ca02c
#98df8a
#d62728
#ff9896
#9467bd
#c5b0d5
#8c564b
#c49c94
#e377c2
#f7b6d2
#7f7f7f
#c7c7c7
#bcbd22
#dbdb8d
#17becf
#9edae5

category20b



A vertical list of 20 color swatches, each with a corresponding hex code. The colors are arranged in a gradient from dark blue at the top to light purple at the bottom. An arrow points from the fifth color swatch (#637939) to the code in the third code block.

#393b79
#5254a3
#6b6ecf
#9c9ede
#637939
#8ca252
#b5cf6b
#cedb9c
#8c6d31
#bd9e39
#e7ba52
#e7cb94
#843c39
#ad494a
#d6616b
#e7969c
#7b4173
#a55194
#ce6dbd
#de9ed6