

Motivação

n

1000

da ordem
de

$O(n)$

10^3

$\ll 1 \text{ seg}$

10^9

10^9

$\approx 1 \text{ seg}$

1 GHz

||

10^9 operações
por seg.

$O(n^2)$

$(10^3)^2 = 10^6$
 $\ll 1 \text{ seg}$

$(10^9)^2 = 10^{18}$
 $\approx 10^9 \text{ seg}$

$3600 \frac{\text{seg}}{\text{h}}$

$24 \frac{\text{h}}{\text{dia}}$

$365 \frac{\text{dias}}{\text{ano}}$

Recursão

resolva um prob. a partir de sol. de
instâncias menores do mesmo problema

Seq de Fibonacci

$F_0 F_1 F_2 F_3 \dots$
0 1 1 2 3 5 8 13 21 34 55 ...

dado $n \in \mathbb{Z}_{\geq 0}$ devolva F_n

$$F_n = \begin{cases} 0, & \text{se } n=0 \\ 1, & \text{se } n=1 \\ F_{n-1} + F_{n-2}, & \text{se } n \geq 2 \end{cases}$$

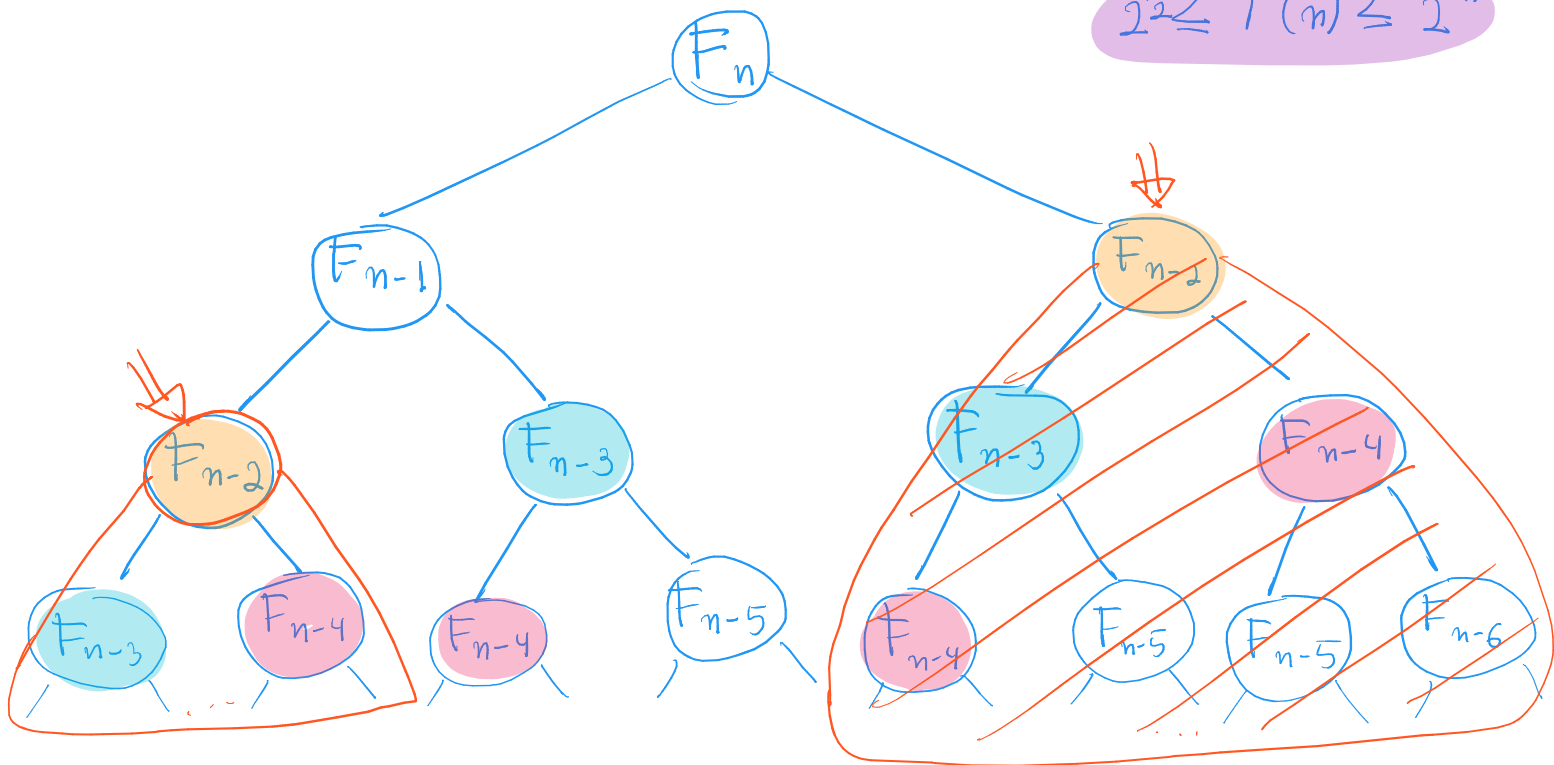
FibRec(n):

se $n=0$: return 0

se $n=1$: return 1

return FibRec(n-1) + FibRec(n-2)

$$2^{\frac{n}{2}} \leq T(n) \leq 2^n$$



FibRecMem(n) := F(n) $n=3$

se $n=0$: return 0

se $n=1$: return 1

se $\text{Mem}[n] > 0$: return $\text{Mem}[n]$

$\text{Mem}[n] = \text{FibRecMem}(n-1) + \text{FibRecMem}(n-2)$

return $\text{Mem}[n]$

$\text{Mem} \begin{bmatrix} 0 & 1 & 2 & 3 & 4 & \dots \\ & & 1 & 2 & \dots \end{bmatrix}$

$F(3) \Rightarrow 2$

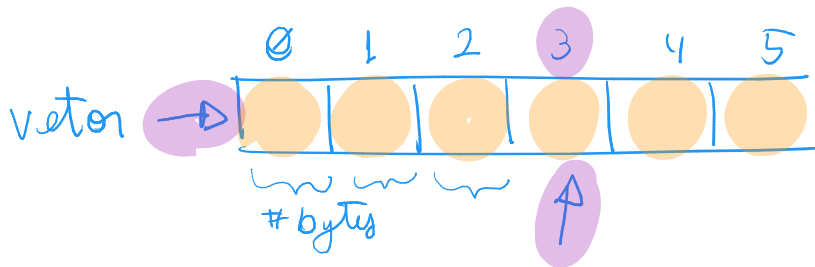
$F(2) \Rightarrow 1$

$F(1) \Rightarrow 1$

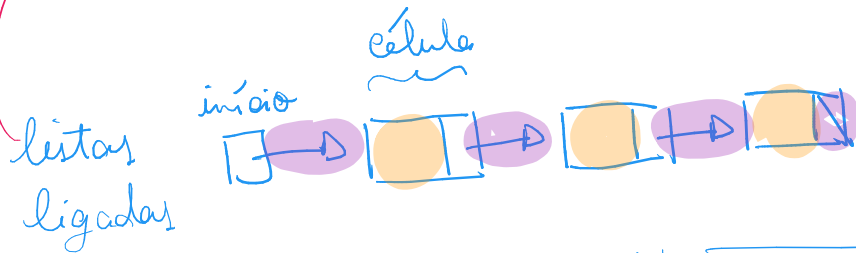
$F(0) \Rightarrow 0$

$F(1) \Rightarrow 1$

Vetores e Listas Ligadas



array
dinâmico



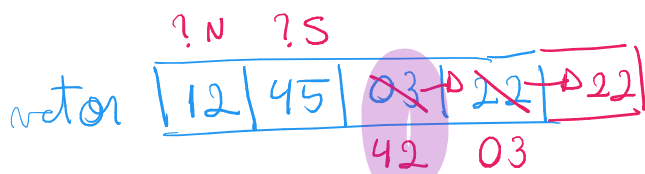
↑ acesso arbitrário

↑ acesso sequencial

↓ acesso arbitrário

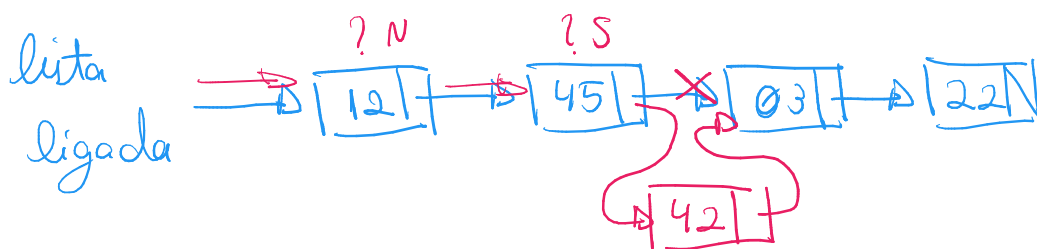
↑ acesso sequencial

operações de inserção e remoção



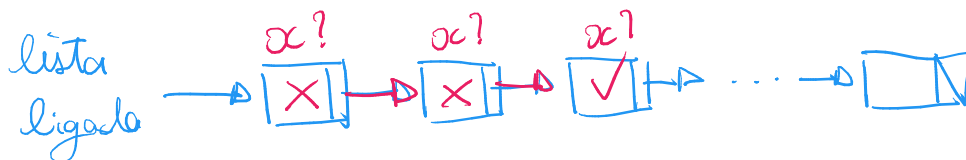
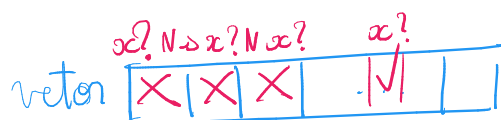
↓ inserção e
remoção

inserir 42 depois
do 45



↑ inserção
e remoção

Busca linear e binária

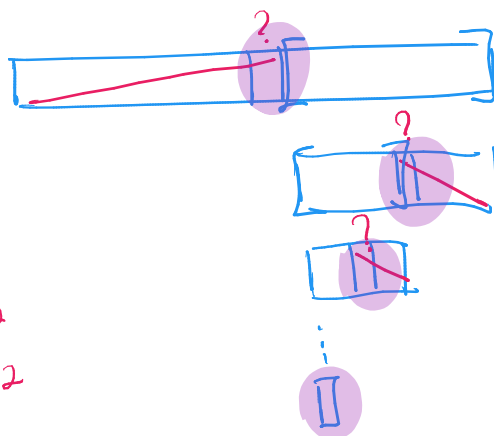
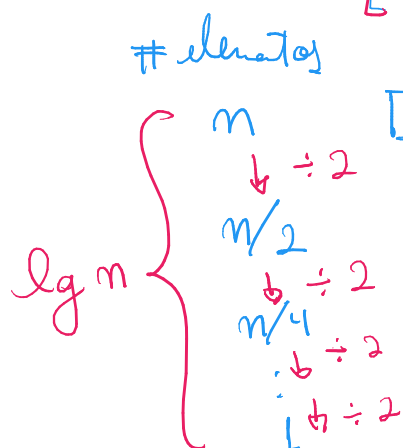
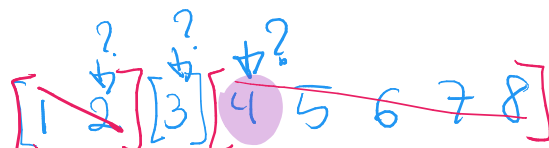


busca linear pelo x

busca binária

Os dados em ordem

Os acesso arbitrário



$$n = 10^9$$

busca linear 10^9

busca binária $\lg 10^9 \approx 30$