

## ESTRUCTURA DE DATOS 1

### Código ST0245

#### Laboratory practice No. 1: Recursion

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### 3) Practice for final project defense presentation

#### 3.1

The asymptotic complexity is:  $F(n) = F(n-1) + F(n-2) + c$   
 In big O notation:  $O(2^n)$

#### 3.2

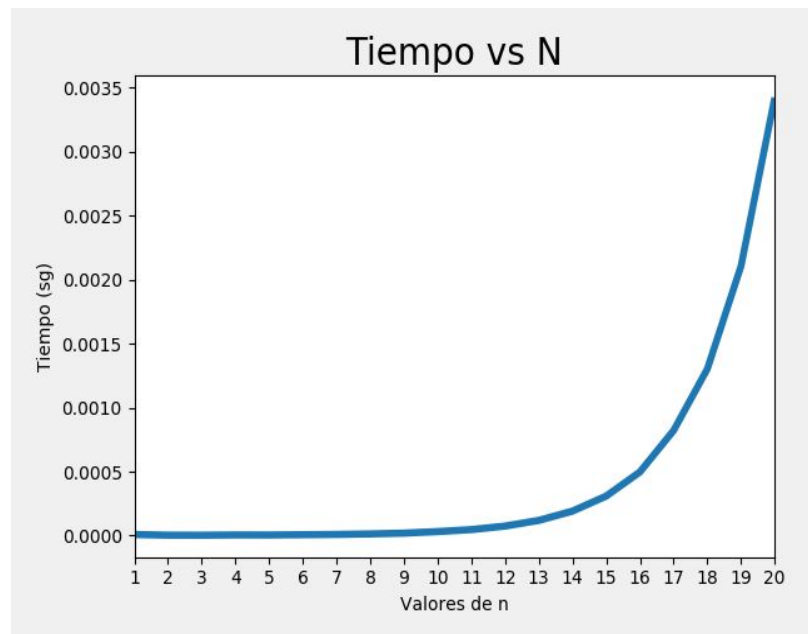
According to big O notation there are  $2^{50}$  instructions to do in order to get with a solution. Since one of my CPU cores performs 798 MHz (798000000 operations per second):  
 $\frac{2^{50}}{798000000} = 1410902.14$  seconds to find the solution.

#### 3.3

In no way is this algorithm useful when the values of  $n$  are very large. It is not useful when solves the problem for a  $2*n$  square, and much less when is a  $n*n*n$  container. The algorithm efficiency is not so good when the problem sizes become larger.

#### 3.4

When the value of *start* is greater than or equal to the size of *nums* will return the value of *target*==0, and this will be our base case. This will stop the algorithm when we have evaluated all the branches of our tree. In problems like this, the idea is to somehow iter over the array creating 2 cases: one on which we subtract the actual number to the target and another case on which we do not. If we get to our base case and the value of target equals 0 we return *True*. If target does not equals to 0 we return *False*. The way that we iter over the array is by calling *groupSum5* adding 1 to *start* and giving the same



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array. In the first call we subtract  $nums[start]$  to target and on the second call we do not. But we have not taken into account the 2 constraints that have been given to us in this exercise. If the value of  $nums[start]$  equals a multiple of 5 we must subtract it to target, and if the consequent value to a multiple of 5 is one, it cannot be subtracted to target. So, when the value of  $nums[start]$  is not a multiple of 5 we should operate as indicated above. In other cases, if  $nums[start] \% 5$  equals 0 it means we have to look for to cases:

- **If it is the last value of the array:** in this case we will call *groupSum5* adding 1 to *start*, giving the same array and subtracting  $nums[start]$  to target in order to get to our base case.
- **In other cases:** we evaluate the value of  $nums[start + 1]$ . If it equals 1 we evaluate *groupSum5* with  $start+2$  and subtracting the actual number to target. If  $nums[start + 1]$  is not 1 we evaluate *groupSum5* adding 1 to start and subtracting  $nums[start]$  to target.

### 3.5

#### Recursion 1 : factorial

$$T(n) = T(n - 1) + c \text{ or}$$

$$T(n) = cn + c_1 \text{ (} c_1 \text{ is an arbitrary parameter)}$$

Function in terms of n, taken from WolframAlpha.

**Big O:**  $O(n)$

```
public int factorial(int n) {
    if(n==0 || n==1){
        return 1;    // c
    }else{
        return n*factorial(n-1);    // T(n - 1) + c
    }
}
```

#### Recursion 1 : fibonacci

$$T(n) = T(n - 2) + T(n - 1) + c \text{ or}$$

$$T(n) = c_1 F_n + c_2 L_n - c \text{ (} c_1, c_2 \text{ are arbitrary parameters)}$$

Function in terms of n, taken from WolframAlpha.

**Big O:**  $O(2^n)$

```
public int fibonacci(int n) {
    if(n<=1){
        return n;    // c
    }
}
```

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```

}else{
    return fibonacci(n-2)+fibonacci(n-1); //  $T(n-2) + T(n-1) + c$ 
}
}

```

**Recursion 1 : powerN**

$T(n) = T(n-1) + c$  or  
 $T(n) = c n + c_1$  ( $c_1$  is an arbitrary parameter)  
 Function in terms of n, taken from WolframAlpha.

**Big O:**  $O(n)$

```

public int powerN(int base, int n) {
    if(n <= 1){
        return base;           // c
    }
    return base * powerN(base, n - 1);           //  $T(n-1) + c$ 
}

```

**Recursion 1 : sumDigits**

$T(n) = T(\frac{n}{10}) + c$  or  
 $T(n) = \frac{c \log(n)}{\log(10)} + c_1$  ( $c_1$  is an arbitrary parameter)  
 Function in terms of n, taken from WolframAlpha.

**Big O:**  $O(n)$

```

public int sumDigits(int n) {
    if(n == 0){
        return 0;           // c
    }else
        return n % 10 + sumDigits(n / 10);           //  $T(\frac{n}{10}) + c$ 
}

```

**Recursion 1 : triangle**

$T(n) = T(n-1) + c$  or

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$T(n) = c n + c_1$  ( $c_1$  is an arbitrary parameter)

Function in terms of  $n$ , taken from WolframAlpha.

**Big O:**  $O(n)$

```
public int triangle(int n) {
    if(rows==0){
        return 0;    // c
    }else{
        return n + triangle(n-1);    // T(n-1) + c
    }
}
```

### Recursion 2 : groupNoAdj

$T(n) = T(n-2) + T(n-1) + c$  or

$T(n) = c_1 F_n + c_2 L_n - c$  ( $c_1, c_2$  are arbitrary parameters)

Function in terms of  $n$ , taken from WolframAlpha.

**Big O:**  $O(2^n)$

```
public boolean groupNoAdj(int start, int[] nums, int target) {
    if(start >= nums.length) return (target==0); // c

    if(groupNoAdj(start+2,nums,target-nums[start])){ // T(n-2)
        return true;
    }
    if(groupNoAdj(start+1,nums,target)){ // T(n-1)
        return true;
    }
    return false;
}
```

### Recursion 2 : groupSum5

$T(n) = 2T(n-1) + c$  or

$T(n) = c_1 2^{n-1}$  ( $c_1$  is an arbitrary parameter)

Function in terms of  $n$ , taken from WolframAlpha.

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**Big O:**  $O(2^{n-1})$

```
public boolean groupSum5(int start, int[] nums, int target) {
    if(start >= nums.length) return (target==0); // c

    if(nums[start]%5==0){ c
        if(start+1<nums.length){
            if(nums[start+1]==1){
                if(groupSum5(start+2,nums,target-nums[start])) return true;
            }
            else{
                if(groupSum5(start+1,nums,target-nums[start])) return true;
            }
        }else{
            if(groupSum5(start+1,nums,target-nums[start])) return true;
        }
    }else{
        if(groupSum5(start+1,nums,target-nums[start])) return true;    //  $T(n-1)$ 
        if(groupSum5(start+1,nums,target)) return true;                //  $T(n-1)$ 
    }
    return false;
}
```

#### Recursion 2 : groupSum6

$$T(n) = 2T(n-1) + c \text{ or}$$

$$T(n) = c_1 2^{n-1} \text{ (} c_1 \text{ is an arbitrary parameter)}$$

Function in terms of n, taken from WolframAlpha.

**Big O:**  $O(2^{n-1})$

```
public boolean groupSum6(int start, int[] nums, int target) {
    if(start >= nums.length) return (target == 0); // c
    if(nums[start]!=6){ // c
        if(groupSum6(start+1,nums,target-nums[start])) return true; //  $T(n-1)$ 
        if(groupSum6(start+1,nums,target)) return true; //  $T(n-1)$ 
    }else{

```

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```

    if(groupSum6(start+1,nums,target-6)) return true;
}
return false;
}

```

#### Recursion 2 : splitArray

$T(n) = 2T(n-1) + c$  or  
 $T(n) = c_1 2^{n-1}$  ( $c_1$  is an arbitrary parameter)  
 Function in terms of n, taken from WolframAlpha.

**Big O:**  $O(2^{n-1})$

```

public boolean splitArray(int[] nums) {
    return fill(0,nums,0,0); //c1
}
public boolean fill(int index,int[] nums,int uno,int dos){
    if(index >= nums.length) return uno==dos; // c
    return fill(index+1,nums,uno+nums[index],dos) || // T(n-1)
    fill(index+1,nums,uno,dos+nums[index]); // T(n-1)
}

```

#### Recursion 2 : groupSumClump

$T(n) = 2T(n-1) + c$  or  
 $T(n) = c_1 2^{n-1}$  ( $c_1$  is an arbitrary parameter)  
 Function in terms of n, taken from WolframAlpha.

**Big O:**  $O(2^{n-1})$

```

public boolean groupSumClump(int start, int[] nums, int target) {
    int cont=1;
    if(start >= nums.length) return target==0; // c
    if(start+1 < nums.length){ // c
        if(nums[start] == nums[start+1]){ // c
            for(int i =start+1;i<nums.length; i++){
                if(nums[i] != nums[start]) break;
                Cont++; //c6
            }
        }
    }
}

```

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```

    }
    }
    }

    if(groupSumClump(start+cont,nums,target-nums[start]*cont)) return true;    //  $T(n-1)$ 
    if(groupSumClump(start+cont,nums,target)) return true;    //  $T(n-1)$ 

    return false;
}

```

### 3.6

#### Recursion 1 : factorial

**n** is the number whose factorial will be calculated by the algorithm.

#### Recursion 1 : fibonacci

**n** represents the nth number in the fibonacci sequence.

#### Recursion 1 : powerN

**base** represents the number that is going to be elevated.

**n** represents the power to which the base will be elevated.

#### Recursion 1 : sumDigits

**n** represents the input number of which the digits will be added together.

#### Recursion 1 : triangle

**n** represents the  $n^{th}$  row of a triangle made of wooden blocks.

#### Recursion 2 : groupNoAdj

**start** represents the position of the array from which each individual traversal will begin.

**target** represents the sum that is being looked for in the array.

**nums** represents the collection of numbers the target is being searched for on.

**n** in the complexity analysis represents the length of the section of the array that will be traversed.

#### Recursion 2 : groupSum5

**start** represents the position of the array from which each individual traversal will begin.

**target** represents the sum that is being looked for in the array.

**nums** represents the collection of numbers the target is being searched for on.

**n** in the complexity analysis represents the length of the section of the array that will be traversed.

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#### Recursion 2 : groupSum6

**start** represents the position of the array from which each individual traversal will begin.

**target** represents the sum that is being looked for in the array.

**nums** represents the collection of numbers the target is being searched for on.

**n** in the complexity analysis represents the length of the section of the array that will be traversed.

#### Recursion 2 : groupSumClump

**start** represents the position of the array from which each individual traversal will begin.

**target** represents the sum that is being looked for in the array.

**nums** represents the collection of numbers the target is being searched for on.

**n** in the complexity analysis represents the length of the section of the array that will be traversed.

#### Recursion 2 : splitArray

**nums** represents the collection of numbers on which the algorithm will be used.

**n** in the complexity analysis represents the length of the subsection of the array that will be traversed.

#### 4) Practice for midterms

4.2 a)  $T(n) = T(n/2) + c$

4.3.1 `int res = solucionar(n - a, a, b, c) + 1;`

4.3.2 `res = Math.max(res, solucionar(n - b, b, a, c) + 1);`

4.3.3 `res = Math.max(res, solucionar(n - c, c, a, b) + 1);`

4.5.1

2. `if (n <= 2) return n;`

3. `return formas(n-1) +`

4. `return formas(n-2);`

4.5.2 b)  $T(n-1) + T(n+2) + c$

4.6.1 `10. return sumAux(n, i+2);`

4.6.2 `12. return (n.charAt(i) - '0' + sumAux(n, i+1));`

4.8.1 `9. return 0;`

4.8.2 `int suma = ni + nj;`

4.10 `6`

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