## Random $\beta$ -expansions