Scilab

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Introduction

What is Scilab?

A free alternative to MATLAB

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A free alternative to MATLAB

What can it do?

- Advanced calculator
- 2 Programming
- Plotting, visualisation

Simple calculations

Try out these and see if they give expected results

```
1 2+3-4

2 4^2

3 4**4

4 6/4

5 2+(2^2-(1/2))

1 1e-3 + 1d-2
```

Simple calculations

Try out these and see if they give expected results

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```

See what happens when you add a semicolon

```
6/4;
```

Variables

All calculations are stored by default in ans

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ans

Variables

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```
6/4;
ans
```

You can specify a variable to store the value instead

```
pi_approx = 22/7;
```

And see its value later

```
pi_approx
disp(pi_approx)
```

More on variables

Some useful pre-defined variables

```
1 %pi
2 %e
3 %i
4 %t
5 %f
6 %inf
7 %nan
8 %eps
```

Pre-defined functions

See if the outputs of these lines are as expected

```
abs(-2)
\min(3,4,5)
\max(-2, -3, -4)
sin(%pi/2)
cos(%pi)
tan(%pi/4)
asin(1)/(%pi/2)
\exp(2)/\%e^2
log10(100)
log(%e)
```

Auto-completion: hit TAB

- ► Variable Browser
 - Only lists user-defined variables
 - To list all variables:

whos

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disp(pi_approx)
clear pi_approx
disp(pi_approx)
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- ► Command History
 - Execute an old command by double clicking
 - Can also navigate using ↑ and ↓ keys
 - Clear screen using clc

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- Command History
 - Execute an old command by double clicking
 - Can also navigate using ↑ and ↓ keys
 - Clear screen using clc
- ► File Browser
 - Useful when working with multiple files

Basic matrix creation

Wrap inside [], use, and; to separate columns and rows

$$x = [1,2,3]$$

$$y = [4;5;6;7]$$

$$A = [1,0;0,1]$$

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Scilab will warn you if the dimensions are inconsistent

$$B = [1,2,3;4,5]$$

Basics

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```
B = [1,2,3;4,5]
```

Adding will transpose the matrix

```
B = [1,2,3;4,5,6];
B'
```

You can fill matrices with pre-existing matrices

```
row1 = [1,2,3,4];
row2 = [5,6,7,8];
M = [row1;row2]
```

Special functions for matrix creation

Creating ranges

```
i = 1:10
j = 1:2:10
x = 0:0.1:1
y = linspace(0,1,25)
```

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Some useful commands for creating dummy matrices of required size

```
A = zeros(2,2)
B = ones(3,2)
M = eye(3,3)
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i = 1:10

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Some useful commands for creating dummy matrices of required size

```
A = zeros(2,2)
B = ones(3,2)
M = eye(3,3)
```

Can you make sense of this result?

```
M = [[zeros(1,2); ones(1,2); eye(2,2)], ones(4,1)]
```

Matrix operations

Scalar operations affect all elements of matrices

```
A = eye(3,3);
A*2
A/4
A+5
```

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Scilab automatically figures out matrix operations too

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B = 2*ones(3,3)
A+B
A*B
B^2
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A+B
A*B
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```

Special element wise operations

```
A.*B
A./B
A./2
```

How is A^2 different from A.^2?

Matrix functions

Most Scilab functions can operate element-wise on matrices

```
A = %pi/2*[0,1;2,3];
sin(A)
```

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Some special functions for matrices

```
length(A)
size(A)
sum(A)
det(A)
inv(A)
trace(A)
```

Access elements using (row,col)

```
A = eye(3,3);
A(1,2) = 2;
A
```

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A(4)
```

Extract rows and columns using :

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A(1,2) = 2;
A
```

A single index can also be used: increments column-wise

```
A(4)
```

Extract rows and columns using :

```
A(:,2)
A(1,:)
```

Special symbol \$

```
A($,3)
```

Access elements using (row,col)

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Extract rows and columns using :

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Special symbol \$

Arrays can also be used to access and modify

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A(4)
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Extract rows and columns using :

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A(:,2)
A(1,:)
```

Special symbol \$

Arrays can also be used to access and modify

```
A([1,2],2)
A(4,:) = [10,20,30]
```

See if this makes sense

```
A = eye(4,4);

j = [2,4];

A(1,j) = j

A([7,8]) = 50

A($,$) = -1

B = [9,10;j];

A(B) = 100
```

Strings

```
Wrap in "" or ''
fname = "Vachan";
lname = 'Potluri';
fname + lname
```

Strings

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Wrap in "" or ''
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fname = "Vachan";
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Function **string** converts variables to strings

```
A = eye(2,2)
string(A)
```

Saving and loading data

Scilab has a working directory

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Function save saves user-defined variables to a file in working directory

```
x = 1.5;
A = [1,2;3,4]
save("data.dat")
```

Saving and loading data

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Function save saves user-defined variables to a file in working directory

```
x = 1.5;
A = [1,2;3,4]
save("data.dat")
```

These variables can be loaded for use later

```
listvarinfile("data.dat")
load("data.dat")
```

Basics

Accessing help

Scilab's built-in help functionality is very useful

```
help
help save
```

Exercises¹

Exercise

The pressure drop Δp required for a flow rate Q in a pipe of diameter D is

$$\Delta p = 4.52 \frac{Q^{1.85}}{C^{1.7} D^{4.87}}$$

Find Δp for these combinations of flow rates and diameters:

- ► Q = 50, 100, 200, 400 and 1000
- ightharpoonup D = 0.5, 1, 1, 2 and 4

Use C = 2.5 for all cases

¹Amos Gilat. MATLAB: An Introduction with Applications. 6th ed. Wiley, 2017.

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Find Δp for these combinations of flow rates and diameters:

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Exercise

A magic square is a matrix in which all rows, columns and diagonals sum to same number.

- Generate a magic square of size 10
- Verify that all rows and columns sum up to the same value

Hint: search Scilab help for the function testmatrix, and use the sum function

¹Amos Gilat. MATLAB: An Introduction with Applications. 6th ed. Wiley, 2017.

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- ► Such files are called "scripts" or "executables"
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- Customary to save such files with .sce or .sci extension
- ► Comments begin with //, or can be wrapped with /* */

```
// this is a single line comment
/* this is a
   multi-line comment */
```

Conditional statements

Can you make sense of this?

```
x=6:
reminder = modulo(x,3);
if reminder==0 then
   disp("3 divides x")
elseif reminder==1 then
   disp("x leaves reminder 1 when divided by 3")
else
   disp("x leaves reminder 2 when divided by 3")
end
```

Hint: look at help for function modulo

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   disp("x leaves reminder 2 when divided by 3")
end
```

Hint: look at help for function modulo

Logical expressions generally use

```
==, ~=, <, <=, >, >=, &&, ||, %t, %f
```

Loops

```
array = 1:10;
value = 5;
for a=array
    if value==a then
        disp("Value exists in
    ⇔array");
        break;
    end
end
```

What does **break** statement do?

Loops

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array = 1:10;
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for a=array
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```

What does **break** statement do?

Scilab always loops over columns

Loops

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end
```

What does break statement do?

Scilab always loops over columns

Functions

```
function [Tf,Tk] = centigradeToFarenhietKelvin(Tc)
    Tf = Tc*9/5 + 32;
    Tk = Tc + 273;
endfunction

[Tf,Tk] = centigradeToFarenhietKelvin(37);
disp(Tf)
disp(Tk)
```

Here Tf and Tk are the "return" values; Tc is the parameter

Functions

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function [Tf,Tk] = centigradeToFarenhietKelvin(Tc)
    Tf = Tc*9/5 + 32;
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[Tf,Tk] = centigradeToFarenhietKelvin(37);
disp(Tf)
disp(Tk)
```

Here Tf and Tk are the "return" values; Tc is the parameter Can also have multiple parameters

```
function s = sum(a,b)
    s = a+b;
endfunction
disp(sum(1,2));
```

Exercise

Write a function to calculate the cross product of two 3d vectors

```
function v = cross_product(v1,v2)
    // fill this
endfunction
```

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Exercise

Write a function that takes in an array and a value, and returns the indices where the value occurs in an array.

Example: for array=[1,2,1,4,5,2] and value=2, the function should return [2,6] (since array(2)=array(6)=value)

```
function indices = multiple_find(array,value)
    // fill this
endfunction
```

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- ► How to access content from another file?

```
my_function_file.sce
```

```
function y=my_function(x)
    // do something
endfunction
```

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```
my_function_file.sce
```

```
function y=my_function(x)
    // do something
endfunction
```

```
main.sce
```

```
// 'include' the file
exec("my_function_file.sce",-1);
// use the function
result=my_function(2.5);
```

Exercise

• Recall the cross_product() function you have written previously.
Save it in a file cross_product.sce

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- Recall the cross_product() function you have written previously. Save it in a file cross_product.sce
- Write a file vector_norm.sce which contains a function vector_norm() to calculate the length (norm) of a 3d vector

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- Recall the cross_product() function you have written previously. Save it in a file cross_product.sce
- Write a file vector_norm.sce which contains a function vector_norm() to calculate the length (norm) of a 3d vector
- **3** Now in the file triangle_area.sce, write a function to calculate the area of an arbitrarily oriented triangle with points p_1 , p_2 and p_3

Hint: The area of a triangle is half the magnitude of cross product of any of its two sides

We will calculate π approximately here

• Write a function <code>get_random_point()</code> which generates a random point in a 2d square $x \in [0,1], y \in [0,1]$

Hint: Use the rand function of Scilab

We will calculate π approximately here

- Write a function get_random_point() which generates a random point in a 2d square $x \in [0,1]$, $y \in [0,1]$ Hint: Use the rand function of Scilab
- **2** Now write a function <code>inside_circle()</code> which takes any point and returns a boolean value saying whether or not the point lies inside the unit circle $x^2 + y^2 = 1$

We will calculate π approximately here

- Write a function get_random_point() which generates a random point in a 2d square $x \in [0,1], y \in [0,1]$ Hint: Use the rand function of Scilab
- Now write a function inside_circle() which takes any point and returns a boolean value saying whether or not the point lies inside the unit circle $x^2 + y^2 = 1$
- Now write a function approximate_pi() that takes N is an parameter and does the following
 - Generate N random points
 - Find out how many of these points (say N_i) lie inside the unit circle
 - Return the value N_i/N

$$rac{ extstyle N_i}{ extstyle N}
ightarrow rac{\pi}{ extstyle 4} ext{ as } extstyle N
ightarrow \infty$$



This is known as the Monte-Carlo simulation

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- ► High level programming languages like Scilab also have inbuilt plotting capability

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- Results are written to a file which is used by a different software for plotting
- ► High level programming languages like Scilab also have inbuilt plotting capability
- Our focus
 - 1 1d plotting: line plots
 - 2 2d plotting: surface, contour and vector plots

Single line plot

```
x = linspace(-%pi,%pi);
y = sin(x);

f = figure(1);
plot(x,y);
```

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Too plain, let's add some description

```
help xs2png
```

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plot(x,y);
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```
help axes_properties
help xs2png
```

```
ax = gca();
ax.parent.background = -2;
ax.tight_limits(1)="on";
ax.font_size=3;
ax.grid=[1,1];
ax.title.text="A sample plot";
ax.title.font size=5;
ax.y_label.text="sin(x)";
ax.y_label.font_size=4;
ax.x label.text="x";
ax.x_label.font_size=4;
xs2png(f, "sin_plot.png");
```

Multiple line plots

```
x = linspace(-%pi,%pi);
y1 = sin(x);
y2 = \cos(x);
v3 = 0.5 + \sin(x);
f = figure(1);
plot(x,y1,"r-^");
plot(x,y2,"b--o");
plot(x,y3,"g:*");
ax = gca();
legend_names = ["curve1", "cos(x)", "curve3"];
legend(ax, legened_names, 1);
```

Multiple line plots

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x = linspace(-\%pi,\%pi);
y1 = sin(x);
v2 = cos(x);
v3 = 0.5 + sin(x);
f = figure(1);
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plot(x,y2,"b--o");
plot(x,y3,"g:*");
ax = gca();
legend_names = ["curve1", "cos(x)", "curve3"];
legend(ax, legened_names, 1);
```

Consult help of LineSpec and legend

 $\bullet \ \mathsf{Plot} \ \rho(x) \ \mathsf{for} \ x \in [-5, 5]$

$$\rho(x) = \begin{cases} 1 + 0.2\sin(5x) & x \ge -4\\ 5 & \text{otherwise} \end{cases}$$

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Using a line plot, find the maximum of $f(x, y) = x^2 + 2y^2$ subjected to $y = \frac{1}{x} + 2$ Hint: Plot $f(x, \frac{1}{x} + 2)$ vs x

 $\bullet \text{ Plot } \rho(x) \text{ for } x \in [-5, 5]$

$$\rho(x) = \begin{cases} 1 + 0.2\sin(5x) & x \ge -4\\ 5 & \text{otherwise} \end{cases}$$

- Using a line plot, find the maximum of $f(x, y) = x^2 + 2y^2$ subjected to $y = \frac{1}{x} + 2$ Hint: Plot $f(x, \frac{1}{x} + 2)$ vs x
- 3 The following is a convergence history of a simulation

Iteration (n)	Error (E)
100	$1 imes 10^{-2}$
200	$1 imes 10^{-3}$

Assuming $\log(E)$ varies linearly with n, find at what iteration will the error reach 1×10^{-8}

Surface plot

```
x = \text{\%pi*linspace}(-1, 1, 100);
y = \text{\%pi*linspace}(-1,1,25);
z = zeros(length(x), length(y));
for i = 1:length(x)
    for j = 1:length(y)
        z(i,j) = \sin(x(i))*\sin(y(j)); // important z_{i,j} = z(x_i, y_i)
    end
end
f = figure(1);
f.color_map = jetcolormap(64);
grayplot(x,y,z);
colorbar(min(z), max(z));
ax = gca();
ax.parent.background = -2;
ax.tight_limits(1:2) = "on";
```

Surface plot

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```

Also see help for colormap and Sgrayplot

3d surface plot

```
x = \text{\%pi*linspace}(-1, 1, 100);
y = \%pi*linspace(-1,1,25);
z = zeros(length(x), length(y));
for i = 1:length(x)
    for j = 1:length(y)
        z(i,j) = \sin(x(i))*\sin(y(j));
    end
end
f = figure(1);
f.color_map = jetcolormap(64);
plot3d(x,y,z);
// gce().color_flag = 1; // color according to z values
colorbar(min(z), max(z));
ax = gca();
ax.parent.background = -2;
ax.tight_limits(1:2) = "on";
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3d surface plot

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f = figure(1);
f.color_map = jetcolormap(64);
plot3d(x,y,z);
// gce().color_flag = 1; // color according to z values
colorbar(min(z), max(z));
ax = gca();
ax.parent.background = -2;
ax.tight_limits(1:2) = "on";
```

You can interact with the 3d plot

Contour plot

```
x = \text{\%pi*linspace}(-1, 1, 100);
y = \%pi*linspace(-1,1,25);
z = zeros(length(x), length(y));
for i = 1:length(x)
    for j = 1:length(v)
        z(i,j) = \sin(x(i))*\sin(y(j));
    end
end
f = figure(1);
f.color_map = jetcolormap(16);
contour(x,y,z,16);
// xset("fpf", " "); // floating point format of contour values
colorbar(min(z), max(z));
ax = gca();
ax.parent.background = -2;
ax.tight limits(1:2) = "on";
```

Contour plot

```
x = \text{\%pi*linspace}(-1, 1, 100);
y = \%pi*linspace(-1,1,25);
z = zeros(length(x), length(y));
for i = 1:length(x)
    for j = 1:length(v)
        z(i,j) = \sin(x(i))*\sin(y(j));
    end
end
f = figure(1);
f.color_map = jetcolormap(16);
contour(x,y,z,16);
// xset("fpf", " "); // floating point format of contour values
colorbar(min(z), max(z));
ax = gca();
ax.parent.background = -2;
ax.tight_limits(1:2) = "on";
```

Also consult help of contourf and fpf

Vector plot

```
x = linspace(-1,1,20);
y = linspace(-1,1,20);
u = zeros(length(x), length(y));
v = zeros(length(x), length(y));
for i = 1:length(x)
    for j = 1:length(y)
        u(i,j) = -y(j);
        v(i,j) = x(i);
    end
end
vel_mag = (u.*u + v.*v).^0.5;
f = figure(1);
f.color_map = jetcolormap(64);
champ(x,y,u,v,arfact=0.5);
gce().colored = "on";
gca().parent.background=-2;
colorbar(min(vel mag), max(vel mag));
```

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colorbar(min(vel_mag), max(vel_mag));
```

What does arfact do? Tinker and see

► The stream function for inviscid potential flow around a cylinder of radius *R* immersed in a free stream of velocity *U* is given by

$$\psi = \left[r - \frac{R^2}{r}\right] U \sin \theta$$

Plot the contours of the stream function for a cylinder of radius 0.5 m in a free stream with velocity $U=1\,\mathrm{m\,s^{-1}}$ in the domain $x\in[-1,1]$ and $y\in[-1,1]$.

Hint: You may require $r = \sqrt{x^2 + y^2}$ and $\theta = \tan^{-1}(y/x)$

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► Similarly obtain a surface plot of the pressure coefficient

$$c_p = 2\frac{p - p_{\infty}}{\rho U^2} p = 2\frac{R^2}{r^2} \cos 2\theta - \frac{R^4}{r^4}$$

A mathematical rose is described by the curve

$$r(\theta) = \cos\left(\frac{n}{d}\theta\right)$$
$$x = r\cos\theta$$

 $y = r \sin \theta$

Here n and d are integers.

Generate mathematical roses for $1 \le n \le 7$ and $1 \le d \le 9$.

Hint: To put them all in a single picture, consult help for subplot

