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1 Oinarrizkoak

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 typedef vector<int> VI;
4 typedef vector<vector<int>> VVI;
5
6 typedef long double DOUBLE;
7 typedef vector<DOUBLE> VD;
8 typedef vector<VD> VVD;
9
10 typedef long long L;
11 typedef vector<L> VL;
12 typedef vector<VL> VVL;
13
14 typedef vector<bool> VB;
15
```

```

16 typedef pair<int, int> PII;
17 typedef vector<PII> VPII;
18
19 ios_base::sync_with_stdio(false);
20 cin.tie(NULL);

```

2 Math

2.1 EulerFunction.cpp

```

1 //  $a^{\phi(N)} \equiv 1 \pmod{N}$  if  $\gcd(a, N) = 1$ 
2 long long euler_totient2(long long n, long long ps) {
3     for (long long i = ps; i * i <= n; i++) {
4         if (n % i == 0) {
5             long long p = 1;
6             while (n % i == 0) {
7                 n /= i;
8                 p *= i;
9             }
10            return (p - p / i) * euler_totient2(n, i + 1);
11        }
12        if (i > 2) i++;
13    }
14    return n - 1;
15 }
16 long long euler_totient(long long n) {
17     return euler_totient2(n, 2);
18 }

```

2.2 NthPermutation.c

```

1 // e The number of entries
2 // n The index of the permutation
3 int fact[MAX]; // MAX >= n
4 int perm[MAX]; // MAX >= n
5 void nthPermutation(const int e, int n) {
6     int j, k = 0;
7
8     // compute factorial numbers
9     fact[k] = 1;
10    while (++k < e)
11        fact[k] = fact[k - 1] * k;
12
13    // compute factorial code
14    for (k = 0; k < n; ++k) {
15        perm[k] = i / fact[n - 1 - k];
16        n = n % fact[e - 1 - k];
17    }
18
19    // readjust values to obtain the permutation
20    // start from the end and check if preceding values are lower
21    for (k = e - 1; k > 0; --k)
22        for (j = k - 1; j >= 0; --j)
23            if (perm[j] <= perm[k])
24                perm[k]++;
25
26    // perm[0..e] contains the nth permutation
27 }

```

2.3 GaussJordan.cpp

```

1 // Gauss-Jordan elimination with full pivoting.
2 // Uses:
3 // (1) solving systems of linear equations ( $AX=B$ )
4 // (2) inverting matrices ( $AX=I$ )
5 // (3) computing determinants of square matrices
6 // Running time:  $O(n^3)$ 
7 // INPUT: a[][] = an n×n matrix
8 // b[][] = an n×m matrix
9 // OUTPUT: X = an n×m matrix (stored in b[][])
10 // A-1 = an n×n matrix (stored in a[][])
11 // returns determinant of a[][]
12 const double EPS = 1e-10;
13
14 double GaussJordan(VVD &a, VVD &b) {
15     const int n = a.size();
16     const int m = b[0].size();
17     VI irow(n), icol(n), ipiv(n);
18     double det = 1;
19
20     for (int i = 0; i < n; i++) {

```

```

21     int pj = -1, pk = -1;
22     for (int j = 0; j < n; j++) if (!ipiv[j])
23         for (int k = 0; k < n; k++) if (!ipiv[k])
24             if (pj == -1 || fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk = k; }
25     //if (fabs(a[pj][pk]) < EPS) { cerr << "Matrix is singular." << endl; exit(0); }
26     ipiv[pk]++;
27     swap(a[pj], a[pk]);
28     swap(b[pj], b[pk]);
29     if (pj != pk) det *= -1;
30     irow[i] = pj;
31     icol[i] = pk;
32
33     double c = 1.0 / a[pk][pk];
34     det *= a[pk][pk];
35     a[pk][pk] = 1.0;
36     for (int p = 0; p < n; p++) a[pk][p] *= c;
37     for (int p = 0; p < m; p++) b[pk][p] *= c;
38     for (int p = 0; p < n; p++) if (p != pk) {
39         c = a[p][pk];
40         a[p][pk] = 0;
41         for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
42         for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;
43     }
44 }
45
46 for (int p = n-1; p >= 0; p--) if (irow[p] != icol[p]) {
47     for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);
48 }
49
50 return det;
51 }

```

2.4 NthPermutationRepetitions.cpp

```

1  typedef map<char,int> mci;
2  L factorial(L i) {
3      if (i <= 1) return 1;
4
5      L totala = 2;
6      for (L j = 3; j <= i; ++j)
7          totala *= j;
8      return totala;
9  }
10 string nthPermutationRepetitions(string input, L n) {
11     mci mapa;
12     int input_len = input.length();
13     for (int i = 0; i < input_len; ++i) {
14         if (mapa.find(input[i]) == mapa.end())
15             mapa[input[i]] = 1;
16         else
17             mapa[input[i]]++;
18     }
19
20     string buffer;
21     buffer.resize(input_len);
22     L totala = 0;
23     for (int i = 0; i < input_len; ++i) {
24         for (mci::iterator elem = mapa.begin(); elem != mapa.end(); ++elem) {
25             if (elem->second > 0) {
26                 elem->second--;
27                 L perm = factorial(input_len - i - 1);
28                 for (mci::iterator c = mapa.begin(); c != mapa.end(); ++c)
29                     perm /= factorial(c->second);
30
31                 if (n < totala + perm) {
32                     buffer[i] = elem->first;
33                     break;
34                 }
35                 totala += perm;
36                 elem->second++;
37             }
38         }
39     }
40     return buffer;
41 }

```

2.5 NumberTheory.cpp

```

1  // This is a collection of useful code for solving problems that
2  // involve modular linear equations. Note that all of the
3  // algorithms described here work on nonnegative integers.

```

```

4
5 // return a % b (positive value)
6 int mod(int a, int b) {
7     return ((a%b)+b)%b;
8 }
9
10 // computes gcd(a,b)
11 int gcd(int a, int b) {
12     int tmp;
13     while(b){a%=b; tmp=a; a=b; b=tmp;}
14     return a;
15 }
16
17 // computes lcm(a,b)
18 int lcm(int a, int b) {
19     return a/gcd(a,b)*b;
20 }
21
22 // returns d = gcd(a,b); finds x,y such that d = ax + by
23 int extended_euclid(int a, int b, int &x, int &y) {
24     int xx = y = 0;
25     int yy = x = 1;
26     while (b) {
27         int q = a/b;
28         int t = b; b = a%b; a = t;
29         t = xx; xx = x-q*xx; x = t;
30         t = yy; yy = y-q*yy; y = t;
31     }
32     return a;
33 }
34
35 // finds all solutions to ax = b (mod n)
36 VI modular_linear_equation_solver(int a, int b, int n) {
37     int x, y;
38     VI solutions;
39     int d = extended_euclid(a, n, x, y);
40     if (!(b%d)) {
41         x = mod (x*(b/d), n);
42         for (int i = 0; i < d; i++)
43             solutions.push_back(mod(x + i*(n/d), n));
44     }
45     return solutions;
46 }
47
48 // computes b such that ab = 1 (mod n), returns -1 on failure
49 int mod_inverse(int a, int n) {
50     int x, y;
51     int d = extended_euclid(a, n, x, y);
52     if (d > 1) return -1;
53     return mod(x,n);
54 }
55
56 // Chinese remainder theorem (special case): find z such that
57 // z % x = a, z % y = b. Here, z is unique modulo M = lcm(x,y).
58 // Return (z,M). On failure, M = -1.
59 PII chinese_remainder_theorem(int x, int a, int y, int b) {
60     int s, t;
61     int d = extended_euclid(x, y, s, t);
62     if (a%d != b%d) return make_pair(0, -1);
63     return make_pair(mod(s*b*x+t*a*y,x*y)/d, x*y/d);
64 }
65
66 // Chinese remainder theorem: find z such that
67 // z % x[i] = a[i] for all i. Note that the solution is
68 // unique modulo M = lcm_i (x[i]). Return (z,M). On
69 // failure, M = -1. Note that we do not require the a[i]'s
70 // to be relatively prime.
71 PII chinese_remainder_theorem(const VI &x, const VI &a) {
72     PII ret = make_pair(a[0], x[0]);
73     for (int i = 1; i < x.size(); i++) {
74         ret = chinese_remainder_theorem(ret.second, ret.first, x[i], a[i]);
75         if (ret.second == -1) break;
76     }
77     return ret;
78 }
79
80 // computes x and y such that ax + by = c; on failure, x = y = -1
81 void linear_diophantine(int a, int b, int c, int &x, int &y) {
82     int d = gcd(a,b);

```

```

83 if (c%d) {
84     x = y = -1;
85 } else {
86     x = c/d * mod_inverse(a/d, b/d);
87     y = (c-a*x)/b;
88 }
89 }

```

2.6 Simplex.cpp

```

1 // Two-phase simplex algorithm for solving linear programs of the form
2 //      maximize      c^T x
3 //      subject to    Ax <= b
4 //                  x >= 0
5 // INPUT: A -- an m x n matrix
6 //        b -- an m-dimensional vector
7 //        c -- an n-dimensional vector
8 //        x -- a vector where the optimal solution will be stored
9 // OUTPUT: value of the optimal solution (infinity if unbounded
10 //        above, nan if infeasible)
11 // To use this code, create an LPSolver object with A, b, and c as
12 // arguments. Then, call Solve(x).
13
14 const DOUBLE EPS = 1e-9;
15
16 struct LPSolver {
17     int m, n;
18     VI B, N;
19     VVD D;
20
21     LPSolver(const VVD &A, const VD &b, const VD &c) :
22         m(b.size()), n(c.size()), N(n+1), B(m), D(m+2, VD(n+2)) {
23         for (int i = 0; i < m; i++) for (int j = 0; j < n; j++) D[i][j] = A[i][j];
24         for (int i = 0; i < m; i++) { B[i] = n+i; D[i][n] = -1; D[i][n+1] = b[i]; }
25         for (int j = 0; j < n; j++) { N[j] = j; D[m][j] = -c[j]; }
26         N[n] = -1; D[m+1][n] = 1;
27     }
28
29     void Pivot(int r, int s) {
30         for (int i = 0; i < m+2; i++) if (i != r)
31             for (int j = 0; j < n+2; j++) if (j != s)
32                 D[i][j] -= D[r][j] * D[i][s] / D[r][s];
33         for (int j = 0; j < n+2; j++) if (j != s) D[r][j] /= D[r][s];
34         for (int i = 0; i < m+2; i++) if (i != r) D[i][s] /= -D[r][s];
35         D[r][s] = 1.0 / D[r][s];
36         swap(B[r], N[s]);
37     }
38
39     bool Simplex(int phase) {
40         int x = phase == 1 ? m+1 : m;
41         while (true) {
42             int s = -1;
43             for (int j = 0; j <= n; j++) {
44                 if (phase == 2 && N[j] == -1) continue;
45                 if (s == -1 || D[x][j] < D[x][s] || D[x][j] == D[x][s] && N[j] < N[s]) s = j;
46             }
47             if (D[x][s] >= -EPS) return true;
48             int r = -1;
49             for (int i = 0; i < m; i++) {
50                 if (D[i][s] <= 0) continue;
51                 if (r == -1 || D[i][n+1] / D[i][s] < D[r][n+1] / D[r][s] ||
52                     D[i][n+1] / D[i][s] == D[r][n+1] / D[r][s] && B[i] < B[r]) r = i;
53             }
54             if (r == -1) return false;
55             Pivot(r, s);
56         }
57     }
58
59     DOUBLE Solve(VD &x) {
60         int r = 0;
61         for (int i = 1; i < m; i++) if (D[i][n+1] < D[r][n+1]) r = i;
62         if (D[r][n+1] <= -EPS) {
63             Pivot(r, n);
64             if (!Simplex(1) || D[m+1][n+1] < -EPS) return -numeric_limits<DOUBLE>::infinity();
65             for (int i = 0; i < m; i++) if (B[i] == -1) {
66                 int s = -1;
67                 for (int j = 0; j <= n; j++)
68                     if (s == -1 || D[i][j] < D[i][s] || D[i][j] == D[i][s] && N[j] < N[s]) s = j;
69                 Pivot(i, s);
70             }

```

```

71     }
72     if (!Simplex(2)) return numeric_limits<DOUBLE>::infinity();
73     x = VD(n);
74     for (int i = 0; i < m; i++) if (B[i] < n) x[B[i]] = D[i][n+1];
75     return D[m][n+1];
76 }
77 };

```

2.7 Factors.cpp

```

1 // COMPLEXITY: O(sqrt(n))
2 //Returns a list of all the factors of n
3 //Example: n = 12 -> result = [2, 2, 3]
4 // n > 1
5 VI factors(int n) {
6     int z = 2;
7     VI result;
8     while (z * z <= n) {
9         if (n % z == 0) {
10             result.push_back(z);
11             n /= z;
12         } else z++;
13     }
14     if (n > 1) result.push_back(n);
15     return result;
16 }

```

2.8 BrentCycleDetection.cpp

```

1 template<typename T, typename F>
2 class BrentCycleDetection {
3     F f;
4 public:
5     PII findCycle(T x0) {
6         // 1st part: search successive powers of two
7         int power = 1, lambda = 1; T tortoise = x0, hare = f(x0);
8         while (tortoise != hare) {
9             if (power == lambda) {
10                 tortoise = hare;
11                 power *= 2;
12                 lambda = 0;
13             }
14             hare = f(hare);
15             lambda++;
16         }
17         // 2nd part: Find the position of the first repetition of length lambda
18         int mu = 0;
19         tortoise = hare = x0;
20         for (int i = 0; i < lambda; i++) hare = f(hare);
21         // 3rd part: the hare and tortoise move at same speed till they agree
22         while (tortoise != hare) {
23             tortoise = f(tortoise);
24             hare = f(hare);
25             mu++;
26         }
27         return PII(mu, lambda);
28     }
29 };

```

2.9 ModularExponentiation.cpp

```

1 //Complexity: O(log b)
2 //Returns (a^b)%c
3 int modular_pow(int a, int b, int c) {
4     int result = 1;
5     while (b > 0) {
6         if (b % 2 == 1)
7             result = (result * a) % c;
8         b = b >> 1;
9         a = (a * a) % c;
10    }
11    return result;
12 }

```

3 StringProcessing

3.1 KMP.cpp

```

1 #define MAX_N 100010
2 char T[MAX_N], P[MAX_N]; // T = text, P = pattern
3 int b[MAX_N], n, m; // b = back table, n = length of T, m = length of P
4 void kmpPreprocess() {

```

```

5     int i = 0, j = -1; b[0] = -1;
6     while (i < m) {
7         while (j >= 0 && P[i] != P[j]) j=b[j];
8         i++; j++;
9         b[i] = j; // observe i = 8, 9, 10,
10    } }
11
12    void kmpSearch() {
13        int i = 0, j = 0;
14        while (i < n) {
15            while (j >= 0 && T[i] != P[j]) j = b[j];
16            i++; j++;
17            if (j == m) {
18                printf("P is found at index %d in T\n", i - j);
19                j = b[j]; // prepare j for the next possible match
20            } } }

```

3.2 EditDistance.java

```

1    public class EditDistance {
2
3        public static final EditDistance LEVENSHTein_DISTANCE = new EditDistance(2, -1, -1, -1);
4        public static final EditDistance LONGEST_COMMON_SUBSEQUENCE = new EditDistance(1, -1000000000, 0, 0
5        );
6
7        public final int matchScore; // Character a[i] and b[i] match and we do nothing
8        public final int mismatchScore; // Character a[i] and b[i] mismatch and we replace a[i] with b[i]
9        public final int insertScore; // We insert a space in A[i]
10       public final int deleteScore; // We delete a letter from A[i]
11
12       public EditDistance(int matchScore, int mismatchScore, int insertScore, int deleteScore) {
13           this.matchScore = matchScore;
14           this.mismatchScore = mismatchScore;
15           this.insertScore = insertScore;
16           this.deleteScore = deleteScore;
17       }
18
19       public int getMaxScore(String a, String b) { // Needleman-Wunsch's algorithm
20           final int[][] table = new int[a.length()+1][b.length()+1];
21           for (int i = 1; i <= a.length(); i++) table[i][0] = i * deleteScore;
22           for (int j = 1; j <= b.length(); j++) table[0][j] = j * insertScore;
23           for (int i = 1; i <= a.length(); i++) {
24               for (int j = 1; j <= b.length(); j++) {
25                   table[i][j] = table[i-1][j-1] + (a.charAt(i-1) == b.charAt(j-1) ? matchScore :
26                       mismatchScore);
27                   table[i][j] = Math.max(table[i][j], table[i-1][j] + deleteScore);
28                   table[i][j] = Math.max(table[i][j], table[i][j-1] + insertScore);
29               }
30           }
31           return table[a.length()][b.length()];
32       }
33   }

```

3.3 SuffixArray.cpp

```

1    #define MAX_N 100010
2    //O(nlogn)
3    char T[MAX_N]; // the input string, up to 100K characters
4    int n; // the length of input string
5    int RA[MAX_N], tempRA[MAX_N]; // rank array and temporary rank array
6    int SA[MAX_N], tempSA[MAX_N]; // suffix array and temporary suffix array
7    int c[MAX_N]; // for counting/radix sort
8
9    void countingSort(int k) { // O(n)
10       int i, sum, maxi = max(300, n); // up to 255 ASCII chars or length of n
11       memset(c, 0, sizeof c); // clear frequency table
12       for (i = 0; i < n; i++) // count the frequency of each integer rank
13           c[i + k < n ? RA[i + k] : 0]++;
14       for (i = sum = 0; i < maxi; i++) {
15           int t = c[i]; c[i] = sum; sum += t;
16       }
17       for (i = 0; i < n; i++) // shuffle the suffix array if necessary
18           tempSA[c[SA[i]+k < n ? RA[SA[i]+k] : 0]++] = SA[i];
19       for (i = 0; i < n; i++) // update the suffix array SA
20           SA[i] = tempSA[i];
21   }
22
23   void constructSA() { // this version can go up to 100000 characters
24       int i, k, r;
25       for (i = 0; i < n; i++) RA[i] = T[i]; // initial rankings

```

```

26 for (i = 0; i < n; i++) SA[i] = i; // initial SA: {0, 1, 2, ..., n-1}
27 for (k = 1; k < n; k <= 1) { // repeat sorting process log n times
28     countingSort(k); // actually radix sort: sort based on the second item
29     countingSort(0); // then (stable) sort based on the first item
30     tempRA[SA[0]] = r = 0; // re-ranking; start from rank r = 0
31     for (i = 1; i < n; i++) // compare adjacent suffixes
32         tempRA[SA[i]] = // if same pair => same rank r; otherwise, increase r
33             (RA[SA[i]] == RA[SA[i-1]] && RA[SA[i]+k] == RA[SA[i-1]+k]) ? r : ++r;
34     for (i = 0; i < n; i++) // update the rank array RA
35         RA[i] = tempRA[i];
36     if (RA[SA[n-1]] == n-1) break; // nice optimization trick
37 } }
38
39 int main() {
40     n = (int)strlen(gets(T)); // input T as per normal, without the $
41     T[n++] = $; // add terminating character
42     constructSA();
43     for (int i = 0; i < n; i++) printf("%2d\t%s\n", SA[i], T + SA[i]);
44 } // return 0;
45
46
47 ii stringMatching() { // string matching in O(m log n)
48     int lo = 0, hi = n-1, mid = lo; // valid matching = [0..n-1]
49     while (lo < hi) { // find lower bound
50         mid = (lo + hi) / 2; // this is round down
51         int res = strncmp(T + SA[mid], P, m); // try to find P in suffix mid
52         if (res >= 0) hi = mid; // prune upper half (notice the >= sign)
53         else lo = mid + 1; // prune lower half including mid
54         // observe = in "res >= 0" above
55     if (strncmp(T + SA[lo], P, m) != 0) return ii(-1, -1); // if not found
56     ii ans; ans.first = lo;
57     lo = 0; hi = n - 1; mid = lo;
58     while (lo < hi) { // if lower bound is found, find upper bound
59         mid = (lo + hi) / 2;
60         int res = strncmp(T + SA[mid], P, m);
61         if (res > 0) hi = mid; // prune upper half
62         else lo = mid + 1; // prune lower half including mid
63     } // (notice the selected branch when res == 0)
64     if (strncmp(T + SA[hi], P, m) != 0) hi--; // special case
65     ans.second = hi;
66     return ans;
67 } // return lower/upperbound as first/second item of the pair, respectively
68
69 int main() {
70     n = (int)strlen(gets(T)); // input T as per normal, without the $
71     T[n++] = $; // add terminating character
72     constructSA();
73     for (int i = 0; i < n; i++) printf("%2d\t%s\n", SA[i], T + SA[i]);
74     while (m = (int)strlen(gets(P)), m) { // stop if P is an empty string
75         ii pos = stringMatching();
76         if (pos.first != -1 && pos.second != -1) {
77             printf("%s found, SA[%d..%d] of %s\n", P, pos.first, pos.second, T);
78             printf("They are:\n");
79             for (int i = pos.first; i <= pos.second; i++)
80                 printf("%s\n", T + SA[i]);
81         } else printf("%s is not found in %s\n", P, T);
82     } // return 0;
83
84
85 void computeLCP() {
86     int i, L;
87     Phi[SA[0]] = -1; // default value
88     for (i = 1; i < n; i++) // compute Phi in O(n)
89         Phi[SA[i]] = SA[i-1]; // remember which suffix is behind this suffix
90     for (i = L = 0; i < n; i++) { // compute Permuted LCP in O(n)
91         if (Phi[i] == -1) { PLCP[i] = 0; continue; } // special case
92         while (T[i + L] == T[Phi[i] + L]) L++; // L increased max n times
93         PLCP[i] = L;
94         L = max(L-1, 0); // L decreased max n times
95     }
96     for (i = 0; i < n; i++) // compute LCP in O(n)
97         LCP[i] = PLCP[SA[i]]; // put the permuted LCP to the correct position
98 }

```

4 JavaFastIO

4.1 MyScanner.java

```

1 import java.io.*;
2 import java.util.*;

```



```

3
4 //-----PrintWriter for faster output-----
5 public static PrintWriter out;
6
7 //-----MyScanner class for faster input-----
8 public static class MyScanner {
9     BufferedReader br;
10    StringTokenizer st;
11
12    public MyScanner() {
13        br = new BufferedReader(new InputStreamReader(System.in));
14    }
15
16    String next() {
17        while (st == null || !st.hasMoreElements()) {
18            try {
19                st = new StringTokenizer(br.readLine());
20            } catch (IOException e) {
21                e.printStackTrace();
22            }
23        }
24        return st.nextToken();
25    }
26
27    int nextInt() { return Integer.parseInt(next()); }
28    long nextLong() { return Long.parseLong(next()); }
29    double nextDouble() { return Double.parseDouble(next()); }
30
31    String nextLine(){
32        String str = "";
33        try {
34            str = br.readLine();
35        } catch (IOException e) {
36            e.printStackTrace();
37        }
38        return str;
39    }
40 }
41 //-----

```

5 Misc

5.1 LongestIncreasingSubsequence.cpp

```

1 inline VI longestIncreasingSubsequence(const vector<int> &a) { // O(n log k)
2     int n = a.size(), lsize = 0;
3     VI lval(n), lind(n), rec(n);
4     for (int i = 0; i < n; i++) {
5         int pos = lower_bound(lval.begin(), lval.begin() + lsize, a[i]) - lval.begin();
6         lval[pos] = a[i]; lind[pos] = i;
7         rec[i] = pos == 0 ? -1 : lind[pos-1];
8         if (pos == lsize) lsize++;
9     }
10    // Recover the solution (return lsize and remove lind and rec if you only need its length)
11    VI res(lsize);
12    for (int i = lind[lsize-1]; i != -1; i = rec[i]) res[--lsize] = a[i];
13    return res;
14 }

```

6 DataStructures

6.1 SparseTableRMQ.java

```

1 public class SparseTableRMQ {
2
3     private final int a[], logTable[], rmq[][];
4
5     public SparseTableRMQ(int[] a) {
6         final int n = a.length;
7         this.a = a;
8         this.logTable = new int[n+1];
9         for (int i = 2; i <= n; i++) logTable[i] = logTable[i>>1] + 1;
10        this.rmq = new int[logTable[n]+1][n];
11        for (int i = 0; i < n; i++) rmq[0][i] = i;
12        for (int k = 1; (1<<k) < n; k++) {
13            for (int i = 0; i+(1<<k) <= n; i++) {
14                final int x = rmq[k-1][i], y = rmq[k-1][i+(1<<k-1)];
15                rmq[k][i] = a[x] <= a[y] ? x : y;
16            }
17        }
18    }
19 }

```

```

18 }
19
20 public int minPos(int i, int j) { // Both inclusive
21     final int k = logTable[j-i], x = rmq[k][i], y = rmq[k][j-(1<<k)+1];
22     return a[x] <= a[y] ? x : y;
23 }
24
25 public int minVal(int i, int j) { // Both inclusive
26     final int k = logTable[j-i];
27     return Math.min(a[rmq[k][i]], a[rmq[k][j-(1<<k)+1]]);
28 }
29
30 }

```

6.2 SegmentTreeRangeUpdate.java

```

1 public class SegmentTreeRangeUpdate {
2     public long[] leaf;
3     public long[] update;
4     public int origSize;
5     public SegmentTreeRangeUpdate(int[] list) {
6         origSize = list.length;
7         leaf = new long[4*list.length];
8         update = new long[4*list.length];
9         build(1,0,list.length-1,list);
10    }
11    public void build(int curr, int begin, int end, int[] list) {
12        if(begin == end)
13            leaf[curr] = list[begin];
14        else {
15            int mid = (begin+end)/2;
16            build(2 * curr, begin, mid, list);
17            build(2 * curr + 1, mid+1, end, list);
18            leaf[curr] = leaf[2*curr] + leaf[2*curr+1];
19        }
20    }
21    public void update(int begin, int end, int val) {
22        update(1,0,origSize-1,begin,end,val);
23    }
24    public void update(int curr, int tBegin, int tEnd, int begin, int end, int val) {
25        if(tBegin >= begin && tEnd <= end)
26            update[curr] += val;
27        else {
28            leaf[curr] += (Math.min(end,tEnd)-Math.max(begin,tBegin)+1) * val;
29            int mid = (tBegin+tEnd)/2;
30            if(mid >= begin && tBegin <= end)
31                update(2*curr, tBegin, mid, begin, end, val);
32            if(tEnd >= begin && mid+1 <= end)
33                update(2*curr+1, mid+1, tEnd, begin, end, val);
34        }
35    }
36    public long query(int begin, int end) {
37        return query(1,0,origSize-1,begin,end);
38    }
39    public long query(int curr, int tBegin, int tEnd, int begin, int end) {
40        if(tBegin >= begin && tEnd <= end) {
41            if(update[curr] != 0) {
42                leaf[curr] += (tEnd-tBegin+1) * update[curr];
43                if(2*curr < update.length){
44                    update[2*curr] += update[curr];
45                    update[2*curr+1] += update[curr];
46                }
47                update[curr] = 0;
48            }
49            return leaf[curr];
50        }
51        else {
52            leaf[curr] += (tEnd-tBegin+1) * update[curr];
53            if(2*curr < update.length){
54                update[2*curr] += update[curr];
55                update[2*curr+1] += update[curr];
56            }
57            update[curr] = 0;
58            int mid = (tBegin+tEnd)/2;
59            long ret = 0;
60            if(mid >= begin && tBegin <= end)
61                ret += query(2*curr, tBegin, mid, begin, end);
62            if(tEnd >= begin && mid+1 <= end)
63                ret += query(2*curr+1, mid+1, tEnd, begin, end);
64            return ret;

```

```

65     }
66 }
67 }

```

6.3 SegmentTree.cpp

```

1  template<typename T, typename Op>
2  class SegmentTree {
3      Op op; vector<T> a, st; size_t n;
4      T update(int p, int l, int r, int lo, int hi) {
5          return l == r ? a[l] : hi < l || lo > r ? st[p] : st[p] = op(update(2*p, l, (l+r)/2, lo, hi),
6              update(2*p+1, (l+r)/2+1, r, lo, hi));
7      }
8      T query(int p, int l, int r, int lo, int hi) {
9          if (l == r) return a[l];
10         if (lo <= l && hi >= r) return st[p];
11         if (!(hi < l || lo > (l+r)/2)) {
12             T left = query(2*p, l, (l+r)/2, lo, hi);
13             return !(hi < (l+r)/2+1 || lo > r) ? op(left, query(2*p+1, (l+r)/2+1, r, lo, hi)) : left;
14         } else {
15             return query(2*p+1, (l+r)/2+1, r, lo, hi);
16         }
17     public:
18         SegmentTree() : n(0), st(0) {}
19         template <typename InputIterator>
20         SegmentTree(InputIterator first, InputIterator last, const Op &op = Op()) : n(last-first), a(first,
21             last), st(2*(last-first)), op(op) {
22             update(0, n-1);
23         }
24         T get(int i) { return a[i]; }
25         T query(int lo, int hi) { return query(1, 0, n-1, lo, hi); } // Both inclusive
26         void set(int i, int v) { a[i] = v; update(i); }
27         void update(int i) { update(i, i); }
28         void update(int lo, int hi) { update(1, 0, n-1, lo, hi); } // Both inclusive
29     };
30     template<typename T, typename Compare>
31     class MinimumIndexSegmentTree {
32     public:
33         struct Op {
34             Compare cmp; vector<T> *a;
35             int operator()(int i, int j) { return cmp((*a)[i], (*a)[j]) ? i : j; }
36         }; vector<T> a; SegmentTree<size_t, Op> st;
37     public:
38         template <typename InputIterator>
39         MinimumIndexSegmentTree(InputIterator first, InputIterator last) : a(first, last) {
40             VI aux(last-first);
41             for (int i = 0; i < aux.size(); i++) aux[i] = i;
42             Op op; op.a = &a;
43             st = SegmentTree<size_t, Op>(aux.begin(), aux.end(), op);
44         }
45         T get(int i) { return a[i]; }
46         int query(int lo, int hi) { return st.query(lo, hi); } // Both inclusive
47         void set(int i, int v) { a[i] = v; st.update(i); }
48     };
49     typedef SegmentTree<int, plus<int> > RSQ;
50     typedef MinimumIndexSegmentTree<int, less<int> > RMQ;

```

6.4 SparseTable.cpp

```

1  struct RMQ {
2      VI A, logtable;
3      VVI spt; // SpT[i][j] = RMQ of range starting at i and length (2^j)
4      RMQ(int N, VI data) : A(data), logtable(N + 1) {
5          for (int i = 2; i <= N; i++)
6              logtable[i] = logtable[i >> 1] + 1;
7          spt = VVI(logtable[N] + 1, VI(N));
8          for (int i = 0; i < N; i++)
9              spt[0][i] = i;
10         for (int j = 1; (1 << j) <= N; j++)
11             for (int i = 0; i + (1 << j) - 1 < N; i++)
12                 if (A[spt[j-1][i]] < A[spt[j-1][i + (1 << (j-1))]])
13                     spt[j][i] = spt[j-1][i];
14                 else
15                     spt[j][i] = spt[j-1][i + (1 << (j-1))];
16     }
17     int query(int i, int j) {
18         int k = logtable[j-i+1]; // 2^k <= (j-i+1)
19         if (A[spt[k][i]] <= A[spt[k][j - (1 << k) + 1]])
20             return spt[k][i];
21         else

```

```

22         return spt[k][j - (1 << k) + 1];
23     }
24 };

```

6.5 UnionFindDisjointSet.cpp

```

1  class UnionFindDisjointSet {
2      VI p, setSize; int numSets;
3  public:
4      explicit UnionFindDisjointSet(int n) : p(n,-1), setSize(n,1), numSets(n) {}
5      int findSet(int i) { return (p[i] < 0) ? i : (p[i] = findSet(p[i])); }
6      bool isSameSet(int i, int j) { return findSet(i) == findSet(j); }
7      int numDisjointSets() { return numSets; }
8      int sizeOfSet(int i) { return setSize[findSet(i)]; }
9      void unionSet(int i, int j) {
10         if (!isSameSet(i, j)) {
11             numSets--;
12             int x = findSet(i), y = findSet(j);
13             if (p[x] < p[y]) { // rank[x] > rank[y]
14                 p[y] = x;
15                 setSize[x] += setSize[y];
16             } else {
17                 p[x] = y;
18                 setSize[y] += setSize[x];
19                 if (p[x] == p[y]) p[y]--;
20             }
21         }
22     }
23 };

```

6.6 BinaryIndexedTree.cpp

```

1  #define LSONe(S) (S & (-S))
2
3  class FenwickTree { // Queries for dynamic RSQ in O(log n), elements numbered from 1 to n
4  private:
5      VI ft;
6  public:
7      FenwickTree(int n) : ft(n+1, 0) {} // initialization: n + 1 zeroes, ignore index 0
8      int rsq(int b) { int sum = 0; for (; b; b -= LSONe(b)) sum += ft[b]; return sum; } // RSQ(1, b)
9      int rsq(int a, int b) { return rsq(b) - (a == 1 ? 0 : rsq(a - 1)); } // RSQ(a, b)
10     // adjusts value of the k-th element by v (v can be +ve/inc or -ve/dec)
11     void adjust(int k, int v) { for (; k < (int)ft.size(); k += LSONe(k)) ft[k] += v; }
12 };

```

7 Graphs

7.1 MinCostMaxFlow.cpp

```

1  // Implementation of min cost max flow algorithm using adjacency
2  // matrix. This implementation keeps track of forward and reverse
3  // edges separately (so you can set cap[i][j] != cap[j][i]).
4  // For a regular max flow, set all edge costs to 0.
5  // Note that negative cost values are not allowed.
6  // INPUT: - graph, constructed using AddEdge()
7  //         - source
8  //         - sink
9  // OUTPUT: - (maximum flow value, minimum cost value)
10 //         - To obtain the actual flow, look at positive values only.
11 #include <cmath>
12
13 const L INF = 1LL << 60;
14
15 struct MinCostMaxFlow {
16     int N;
17     VVL cap, flow, cost;
18     VI found;
19     VL dist, pi, width;
20     VPII dad;
21
22     MinCostMaxFlow(int N) :
23         N(N), cap(N, VL(N)), flow(N, VL(N)), cost(N, VL(N)),
24         found(N), dist(N), pi(N), width(N), dad(N) {}
25
26     void AddEdge(int from, int to, L cap, L cost) {
27         this->cap[from][to] = cap;
28         this->cost[from][to] = cost;
29     }
30
31     void Relax(int s, int k, L cap, L cost, int dir) {
32         L val = dist[s] + pi[s] - pi[k] + cost;

```

```

33     if (cap && val < dist[k]) {
34         dist[k] = val;
35         dad[k] = make_pair(s, dir);
36         width[k] = min(cap, width[s]);
37     }
38 }
39
40 L Dijkstra(int s, int t) {
41     fill(found.begin(), found.end(), false);
42     fill(dist.begin(), dist.end(), INF);
43     fill(width.begin(), width.end(), 0);
44     dist[s] = 0;
45     width[s] = INF;
46
47     while (s != -1) {
48         int best = -1;
49         found[s] = true;
50         for (int k = 0; k < N; k++) {
51             if (found[k]) continue;
52             Relax(s, k, cap[s][k] - flow[s][k], cost[s][k], 1);
53             Relax(s, k, flow[k][s], -cost[k][s], -1);
54             if (best == -1 || dist[k] < dist[best]) best = k;
55         }
56         s = best;
57     }
58
59     for (int k = 0; k < N; k++)
60         pi[k] = min(pi[k] + dist[k], INF);
61     return width[t];
62 }
63
64 pair<L, L> GetMaxFlow(int s, int t) {
65     L totflow = 0, totcost = 0;
66     while (L amt = Dijkstra(s, t)) {
67         totflow += amt;
68         for (int x = t; x != s; x = dad[x].first) {
69             if (dad[x].second == 1) {
70                 flow[dad[x].first][x] += amt;
71                 totcost += amt * cost[dad[x].first][x];
72             } else {
73                 flow[x][dad[x].first] -= amt;
74                 totcost -= amt * cost[x][dad[x].first];
75             }
76         }
77     }
78     return make_pair(totflow, totcost);
79 }
80 };

```

7.2 StronglyConnectedComponents.cpp

```

1 VII adj, scc;
2 VI num, low;
3 VI S;
4 VB visited, currentSCC;
5 int nodeCount, numSCC;
6
7 /* num[i] = orden en el que se visita por primera vez el nodo i */
8 /* low[i] = minimo num alcanzable desde el nodo i y desde sus hijos en la busqueda */
9 /* currentSCC[i] <=> el nodo i forma parte del SCC que se est explorando */
10 /* S = Pila que guarda los nodos seg n el orden en que se exploran */
11 /* Los nodos que forman cada componente quedan en scc */
12 /* Inicializar 'nodeCount' y 'numSCC' a 0 antes de llamar a la funci n */
13 void dfs(int u) {
14     num[u] = low[u] = nodeCount++;
15     S.push_back(u);
16     visited[u] = currentSCC[u] = true;
17     int v;
18     for (int i = 0; i < (int)adj[u].size(); ++i) {
19         v = adj[u][i];
20         if (!visited[v])
21             dfs(v);
22         if (currentSCC[v]) /* si es parte de la misma componente que u */
23             low[u] = min(low[u], low[v]); /* desde u alcanzo lo mismo que desde v */
24     }
25     if (low[u] == num[u]) /* si u es ra z de una SCC */
26         scc.push_back(VI());
27         do { /* El SCC lo forman los nodos en la pila hasta alcanzar u */
28             v = S.back(); S.pop_back(); currentSCC[v] = 0;
29             scc[numSCC].push_back(v);

```

```

30     } while (u != v);
31     numSCC++; /* Si solo se desea el n mero de SCCs, el vector scc sobra */
32 }
33 }
34 /* Ejemplo de main, donde N es el n mero de nodos */
35 // adj = VII(N, VI()); scc = VII(); num = VI(N); low = VI(N);
36 // S = VI(); visited = VB(N);
37 // currentSCC = VB(N); nodeCount = numSCC = 0;
38 /* Rellenar la lista de adyacencia */
39 // for (int i = 0; i < N; ++i)
40 //     if (!visited[i])
41 //         dfs(i);

```

7.3 MaxBipartiteMatching.cpp

```

1 // Maximum Cardinality Bipartite Matching
2 // -- Representaci n con matriz de adyacencia
3 // -- Pasar a la constructora el tama o de las dos particiones (izquierda y derecha)
4 // -- Aadir ejes con addEdge(origen, destino)
5 // La funci n getMatching devuelve la cardinalidad del matching, y rellena los vectores mr y mc:
6 //     mr[i] = nodo asignado al nodo izquierdo i
7 //     mc[j] = nodo asignado al nodo derecho j
8 // Tambi n es til para:
9 //     Maximum Independent Set = |V| - MCBM
10 //     Minimum Vertex Cover = MCBM
11 class MCBM {
12     int nLeft, nRight;
13     VVI mat_adj;
14     VI mr, mc;
15     bool FindMatch(int i, const VVI &mat_adj, VI &seen) {
16         for (int j = 0; j < nRight; j++) {
17             if (mat_adj[i][j] && !seen[j]) {
18                 seen[j] = true;
19                 if (mc[j] < 0 || FindMatch(mc[j], mat_adj, seen)) {
20                     mr[i] = j; mc[j] = i; return true;
21                 }
22             }
23         }
24         return false;
25     }
26 public:
27     MCBM(int NLeft, int NRight) : nLeft(NLeft), nRight(NRight), mr(NLeft, -1), mc(NRight, -1) {
28         mat_adj = VVI(NLeft, VI(NRight));
29     }
30     void addEdge(int u, int v) { mat_adj[u][v] = 1; }
31     int getMatching() {
32         int ct = 0;
33         for (int i = 0; i < nLeft; i++) {
34             VI seen(nRight);
35             if (FindMatch(i, mat_adj, seen)) ct++;
36         }
37         return ct;
38     }
39     VI getLeftMatches() { return mr; };
40     VI getRightMatches() { return mc; };
41 };

```

7.4 ArticulationPoints.cpp

```

1 VVI adj;
2 VI num, low;
3 VI parent;
4 vb visited;
5 vb artPoint;
6 int nodeCount, root, rootChildren;
7
8 /* num[i] = orden en el que se visita por primera vez el nodo i */
9 /* low[i] = m nimo num alcanzable desde el nodo i y desde sus hijos en la b squeda */
10 /* Establecer 'root' al nodo ra z de la b squeda, y 'rootChildren' y 'nodeCount' a 0 antes de llamar
    a dfs(root) */
11 void dfs(int u) {
12     num[u] = low[u] = nodeCount++;
13     visited[u] = true;
14     for (int i = 0; i < (int)adj[u].size(); ++i) {
15         int v = adj[u][i];
16         if (!visited[v]) {
17             parent[v] = u;
18             if (u == root) rootChildren++;
19             dfs(v);
20             if (low[v] >= num[u]) /* si desde v no puedo alcanzar nada m s arriba de u */
21                 artPoint[u] = true;

```

```

22         if (low[v] > num[u]) /* si desde v no puedo alcanzar ni u */
23             cout << "(u,v) is a bridge" << endl;
24         low[u] = min(low[u], low[v]); /* desde u alcanzo lo mismo que desde v */
25     } else if (v != parent[u])
26         low[u] = min(low[u], num[v]); /* desde u alcanzo v */
27 }
28 }
29
30 /* Despues de la llamada: 'root' es un punto de articulacion sii 'rootChildren' > 1 */
31 artPoint[root] = (rootChildren > 1);

```

7.5 MinCostBipartiteMatching.cpp

```

1 // Min cost bipartite matching via shortest augmenting paths
2 //
3 // This is an  $O(n^3)$  implementation of a shortest augmenting path
4 // algorithm for finding min cost perfect matchings in dense
5 // graphs. In practice, it solves  $1000 \times 1000$  problems in around 1
6 // second. Note that both partitions must be of equal size!!
7 //
8 // cost[i][j] = cost for pairing left node i with right node j
9 // Lmate[i] = index of right node that left node i pairs with
10 // Rmate[j] = index of left node that right node j pairs with
11 //
12 // The values in cost[i][j] may be positive or negative. To perform
13 // maximization, simply negate the cost[][] matrix.
14 #include <cmath>
15
16 double MinCostMatching(const VVD &cost, VI &Lmate, VI &Rmate) {
17     int n = int(cost.size());
18     // construct dual feasible solution
19     VD u(n);
20     VD v(n);
21     for (int i = 0; i < n; i++) {
22         u[i] = cost[i][0];
23         for (int j = 1; j < n; j++)
24             u[i] = min(u[i], cost[i][j]);
25     }
26     for (int j = 0; j < n; j++) {
27         v[j] = cost[0][j] - u[0];
28         for (int i = 1; i < n; i++)
29             v[j] = min(v[j], cost[i][j] - u[i]);
30     }
31     // construct primal solution satisfying complementary slackness
32     Lmate = VI(n, -1);
33     Rmate = VI(n, -1);
34     int mated = 0;
35     for (int i = 0; i < n; i++) {
36         for (int j = 0; j < n; j++) {
37             if (Rmate[j] != -1) continue;
38             if (fabs(cost[i][j] - u[i] - v[j]) < 1e-10) {
39                 Lmate[i] = j;
40                 Rmate[j] = i;
41                 mated++;
42                 break;
43             }
44         }
45     }
46
47     VD dist(n);
48     VI dad(n);
49     VI seen(n);
50     // repeat until primal solution is feasible
51     while (mated < n) {
52         // find an unmatched left node
53         int s = 0;
54         while (Lmate[s] != -1) s++;
55         // initialize Dijkstra
56         fill(dad.begin(), dad.end(), -1);
57         fill(seen.begin(), seen.end(), 0);
58         for (int k = 0; k < n; k++)
59             dist[k] = cost[s][k] - u[s] - v[k];
60
61         int j = 0;
62         while (true) {
63             // find closest
64             j = -1;
65             for (int k = 0; k < n; k++) {
66                 if (seen[k]) continue;
67                 if (j == -1 || dist[k] < dist[j]) j = k;

```

```

68     }
69     seen[j] = 1;
70     // termination condition
71     if (Rmate[j] == -1) break;
72     // relax neighbors
73     const int i = Rmate[j];
74     for (int k = 0; k < n; k++) {
75         if (seen[k]) continue;
76         const double new_dist = dist[j] + cost[i][k] - u[i] - v[k];
77         if (dist[k] > new_dist) {
78             dist[k] = new_dist;
79             dad[k] = j;
80         }
81     }
82 }
83 // update dual variables
84 for (int k = 0; k < n; k++) {
85     if (k == j || !seen[k]) continue;
86     const int i = Rmate[k];
87     v[k] += dist[k] - dist[j];
88     u[i] -= dist[k] - dist[j];
89 }
90 u[s] += dist[j];
91 // augment along path
92 while (dad[j] >= 0) {
93     const int d = dad[j];
94     Rmate[j] = Rmate[d];
95     Lmate[Rmate[j]] = j;
96     j = d;
97 }
98 Rmate[j] = s;
99 Lmate[s] = j;
100 mated++;
101 }
102
103 double value = 0;
104 for (int i = 0; i < n; i++)
105     value += cost[i][Lmate[i]];
106
107 return value;
108 }

```

7.6 LowestCommonAncestor.cpp

```

1 // Lowest Common Ancestor with adjacency list
2 // Requires an RMQ implementation
3 // Par[i] = parent of node i in the DFS, root is its own parent
4 // E[i] = i-th node visited in the DFS (Euler tour)
5 // L[i] = levels of the i-th node visited in the DFS (Euler tour)
6 // H[i] = index of the first occurrence of node i in E
7 struct LCA {
8     int idx;
9     VVI adj;
10    VI Par, E, L, H;
11    RMQ * rmq;
12
13    LCA(int N, VVI adjlist) :
14        idx(0), adj(adjlist), Par(N, -1), E(2*N-1), L(2*N-1), H(N, -1) {
15        dfs(0, 0, 0); // We fix the root at index 0
16        rmq = new RMQ(2*N-1, L);
17    }
18
19    void dfs(int cur, int depth, int parent) {
20        Par[cur] = parent;
21        H[cur] = idx;
22        E[idx] = cur;
23        L[idx++] = depth;
24        for (int i = 0; i < (int) adj[cur].size(); i++) {
25            if (Par[adj[cur][i]] == -1) {
26                dfs(adj[cur][i], depth + 1, cur);
27                E[idx] = cur;
28                L[idx++] = depth;
29            }
30        }
31    }
32
33    int depth(int u) { return L[H[u]]; } // Depth of u
34    int parent(int u) { return Par[u]; } // Parent of u
35    int find(int u, int v) { // LCA(u, v)
36        if (H[u] > H[v]) swap(u, v);

```



```

37     return E[rmq->query(H[u], H[v])];
38 }
39 };

```

7.7 MaxFlow.cpp

```

1 // Adjacency list implementation of Dinic's blocking flow algorithm.
2 // This is very fast in practice, and only loses to push-relabel flow.
3 // INPUT: - graph, constructed using AddEdge()
4 //         - source
5 //         - sink
6 // OUTPUT: - maximum flow value
7 //         - To obtain the actual flow values, look at all edges with
8 //           capacity > 0 (zero capacity edges are residual edges).
9 #include <cmath>
10
11 const int INF = 2000000000;
12
13 struct Edge {
14     int from, to, cap, flow, index;
15     Edge(int from, int to, int cap, int flow, int index) :
16         from(from), to(to), cap(cap), flow(flow), index(index) {}
17 };
18
19 struct Dinic {
20     int N;
21     vector<vector<Edge>> > G;
22     vector<Edge *> dad;
23     VI Q;
24
25     Dinic(int N) : N(N), G(N), dad(N), Q(N) {}
26
27     void AddEdge(int from, int to, int cap) {
28         G[from].push_back(Edge(from, to, cap, 0, G[to].size()));
29         if (from == to) G[from].back().index++;
30         G[to].push_back(Edge(to, from, 0, 0, G[from].size() - 1));
31     }
32
33     long long BlockingFlow(int s, int t) {
34         fill(dad.begin(), dad.end(), (Edge *) NULL);
35         dad[s] = &G[0][0] - 1;
36
37         int head = 0, tail = 0;
38         Q[tail++] = s;
39         while (head < tail) {
40             int x = Q[head++];
41             for (int i = 0; i < G[x].size(); i++) {
42                 Edge &e = G[x][i];
43                 if (!dad[e.to] && e.cap - e.flow > 0) {
44                     dad[e.to] = &G[x][i];
45                     Q[tail++] = e.to;
46                 }
47             }
48         }
49         if (!dad[t]) return 0;
50
51         long long totflow = 0;
52         for (int i = 0; i < G[t].size(); i++) {
53             Edge *start = &G[G[t][i].to][G[t][i].index];
54             int amt = INF;
55             for (Edge *e = start; amt && e != dad[s]; e = dad[e->from]) {
56                 if (!e) { amt = 0; break; }
57                 amt = min(amt, e->cap - e->flow);
58             }
59             if (amt == 0) continue;
60             for (Edge *e = start; amt && e != dad[s]; e = dad[e->from]) {
61                 e->flow += amt;
62                 G[e->to][e->index].flow -= amt;
63             }
64             totflow += amt;
65         }
66         return totflow;
67     }
68
69     long long GetMaxFlow(int s, int t) {
70         long long totflow = 0;
71         while (long long flow = BlockingFlow(s, t))
72             totflow += flow;
73         return totflow;
74     }

```

```
75 };
```

7.8 SPFA.cpp

```
1 // Shortest Path Faster Algorithm
2 // SSSP adjacency-list implementation that handles negative weight cycles.
3 // The function returns true if such a cycle is detected (i.e., it can be reached from s).
4 // If not, dist[i] = distance from source node s to node i.
5 // Worst-case complexity:  $O(VE)$ , in practice better than Bellman-Ford, but not than Dijkstra.
6 #define INF 1 << 30
7
8 bool spfa(int s, const vector<VPII>& adj, VI& dist) {
9     int N = adj.size(), u, i;
10    queue<int> cola;
11    VI encolado(N), veces(N);
12
13    dist = VI(N, INF);
14    dist[s] = 0;
15
16    cola.push(s);
17    encolado[s] = veces[s] = 1;
18    while (!cola.empty()) {
19        u = cola.front();
20        cola.pop();
21        encolado[u] = 0;
22        for (i = 0; i < (int) adj[u].size(); ++i) {
23            PII p = adj[u][i];
24            if (dist[u] + p.second < dist[p.first]) {
25                dist[p.first] = dist[u] + p.second;
26                if (!encolado[p.first]) {
27                    cola.push(p.first);
28                    encolado[p.first] = 1;
29                    veces[p.first]++;
30                    // Tratar ciclo negativo si se desea
31                    if (veces[p.first] == N) return true;
32                }
33            }
34        }
35    }
36    return false;
37 }
```

7.9 Kruskal.cpp

```
1 // COMPLEXITY:  $O(E \log E)$ 
2 #include "UnionFindDisjointSet.cpp"
3 //Returns the cost of the msp
4 int Kruskal(vector<pair<int, PII>> edgeList, int graphSize) {
5     sort(edgeList.begin(), edgeList.end());
6
7     int mst_cost = 0;
8     UnionFindDisjointSet UF(graphSize);
9
10    for (int i = 0; i < edgeList.size(); ++i) {
11        pair<int, PII> front = edgeList[i];
12        if (!UF.isSameSet(front.second.first, front.second.second)) {
13            mst_cost += front.first;
14            UF.unionSet(front.second.first, front.second.second);
15        }
16    }
17    return mst_cost;
18 }
```

7.10 Dijkstra.cpp

```
1 // COMPLEXITY:  $O((V+E) \log V)$  ( $V, E < 300K$ )
2 const int INF = 1e9; //Use long long if something bigger is needed
3 VVI graph, weight;
4 VI dist;
5 void dijkstra(int source) {
6     dist = VI(graph.size(), INF);
7     dist[source] = 0;
8     priority_queue<pii, vector<pii>, greater<pii> > pq;
9     pq.push(pii(0, source));
10    while (!pq.empty()) {
11        int d = pq.top().first;
12        int u = pq.top().second;
13        pq.pop();
14        if (d > dist[u]) continue;
15        for (int i = 0; i < (int) graph[u].size(); ++i) {
16            int v = graph[u][i];
17            int w = weight[u][i];
```

```

18         if (dist[u] + w < dist[v]) {
19             dist[v] = dist[u] + w ;
20             pq.push(pii(dist[v], v));
21         }
22     }
23 }
24 }

```

7.11 FloydWarshall.cpp

```

1 // COMPLEXITY:  $O(V^3)$  ( $V < 400$ )
2 // adj_mat = matriz de adyacencia del grafo
3 // adj_mat[i][j] = INF si no hay arista
4 // adj_mat[i][i] = 0
5 // V = cantidad de nodos
6 // Si despues de todo la diagonal tiene un valor menor que cero, tiene ciclos negativos
7 void FloydWarshall (VVI &adj_mat) {
8     int V = adj_mat.size();
9     for (int k = 0; k < V; ++k)
10         for (int i = 0; i < V; ++i)
11             for (int j = 0; j < V; ++j)
12                 adj_mat[i][j] = min(adj_mat[i][j], adj_mat[i][k] + adj_mat[k][j]);
13 }

```

8 Geometry

8.1 ConvexHull.cpp

```

1 // Running time:  $O(n \log n)$ 
2 // INPUT: a vector of input points, unordered.
3 // OUTPUT: a vector of points in the convex hull, counterclockwise, starting
4 // with bottommost/leftmost point
5 #include <cstdio>
6 #include <cmath>
7
8 // #define REMOVE_REDUNDANT // To eliminate redundant points from hull
9
10 typedef double T;
11 const T EPS = 1e-7;
12 struct PT {
13     T x, y;
14     PT() {}
15     PT(T x, T y) : x(x), y(y) {}
16     bool operator<(const PT &rhs) const { return make_pair(y,x) < make_pair(rhs.y,rhs.x); }
17     bool operator==(const PT &rhs) const { return make_pair(y,x) == make_pair(rhs.y,rhs.x); }
18 };
19
20 T cross(PT p, PT q) { return p.x*q.y-p.y*q.x; }
21 T area2(PT a, PT b, PT c) { return cross(a,b) + cross(b,c) + cross(c,a); }
22
23 #ifdef REMOVE_REDUNDANT
24 bool between(const PT &a, const PT &b, const PT &c) {
25     return (fabs(area2(a,b,c)) < EPS && (a.x-b.x)*(c.x-b.x) <= 0 && (a.y-b.y)*(c.y-b.y) <= 0);
26 }
27 #endif
28
29 void ConvexHull(vector<PT> &pts) {
30     sort(pts.begin(), pts.end());
31     pts.erase(unique(pts.begin(), pts.end()), pts.end());
32     vector<PT> up, dn;
33     for (int i = 0; i < pts.size(); i++) {
34         while (up.size() > 1 && area2(up[up.size()-2], up.back(), pts[i]) >= 0) up.pop_back();
35         while (dn.size() > 1 && area2(dn[dn.size()-2], dn.back(), pts[i]) <= 0) dn.pop_back();
36         up.push_back(pts[i]);
37         dn.push_back(pts[i]);
38     }
39     pts = dn;
40     for (int i = (int) up.size() - 2; i >= 1; i--) pts.push_back(up[i]);
41
42 #ifdef REMOVE_REDUNDANT
43     if (pts.size() <= 2) return;
44     dn.clear();
45     dn.push_back(pts[0]);
46     dn.push_back(pts[1]);
47     for (int i = 2; i < pts.size(); i++) {
48         if (between(dn[dn.size()-2], dn[dn.size()-1], pts[i])) dn.pop_back();
49         dn.push_back(pts[i]);
50     }
51     if (dn.size() >= 3 && between(dn.back(), dn[0], dn[1])) {
52         dn[0] = dn.back();

```

```

53     dn.pop_back();
54 }
55 pts = dn;
56 #endif
57 }
58
59 int main() {
60     PT val[] = {PT(0, 0), PT(1, 1), PT(2, 2), PT(-1, 0)};
61     vector<PT> puntuak;
62     for (int i = 0; i < 4; i++)
63         puntuak.push_back(val[i]);
64     ConvexHull(puntuak);
65     for (int i = 0; i < puntuak.size(); i++)
66         cout << puntuak[i].x << " " << puntuak[i].y << endl;
67     return 0;
68 }

```

8.2 GeometryMiscellaneous.cpp

```

1  #include <cmath>
2
3  double INF = 1e100;
4  double EPS = 1e-12;
5
6  struct PT {
7      double x, y;
8      PT() {}
9      PT(double x, double y) : x(x), y(y) {}
10     PT(const PT &p) : x(p.x), y(p.y) {}
11     PT operator + (const PT &p) const { return PT(x+p.x, y+p.y); }
12     PT operator - (const PT &p) const { return PT(x-p.x, y-p.y); }
13     PT operator * (double c) const { return PT(x*c, y*c); }
14     PT operator / (double c) const { return PT(x/c, y/c); }
15 };
16
17 double dot(PT p, PT q) { return p.x*q.x+p.y*q.y; }
18 double dist2(PT p, PT q) { return dot(p-q,p-q); }
19 double cross(PT p, PT q) { return p.x*q.y-p.y*q.x; }
20 ostream &operator<<(ostream &os, const PT &p) {
21     os << "(" << p.x << ", " << p.y << ")";
22 }
23 // rotate a point CCW or CW around the origin
24 PT RotateCCW90(PT p) { return PT(-p.y,p.x); }
25 PT RotateCW90(PT p) { return PT(p.y,-p.x); }
26 PT RotateCCW(PT p, double t) {
27     return PT(p.x*cos(t)-p.y*sin(t), p.x*sin(t)+p.y*cos(t));
28 }
29 // project point c onto line through a and b
30 // assuming a != b
31 PT ProjectPointLine(PT a, PT b, PT c) {
32     return a + (b-a)*dot(c-a, b-a)/dot(b-a, b-a);
33 }
34 // project point c onto line segment through a and b
35 PT ProjectPointSegment(PT a, PT b, PT c) {
36     double r = dot(b-a,b-a);
37     if (fabs(r) < EPS) return a;
38     r = dot(c-a, b-a)/r;
39     if (r < 0) return a;
40     if (r > 1) return b;
41     return a + (b-a)*r;
42 }
43 // compute distance from c to segment between a and b
44 double DistancePointSegment(PT a, PT b, PT c) {
45     return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
46 }
47 // compute distance between point (x,y,z) and plane ax+by+cz=d
48 double DistancePointPlane(double x, double y, double z,
49                             double a, double b, double c, double d)
50 {
51     return fabs(a*x+b*y+c*z-d)/sqrt(a*a+b*b+c*c);
52 }
53 // determine if lines from a to b and c to d are parallel or collinear
54 bool LinesParallel(PT a, PT b, PT c, PT d) {
55     return fabs(cross(b-a, c-d)) < EPS;
56 }
57 bool LinesCollinear(PT a, PT b, PT c, PT d) {
58     return LinesParallel(a, b, c, d)
59         && fabs(cross(a-b, a-c)) < EPS
60         && fabs(cross(c-d, c-a)) < EPS;
61 }

```

```

62 // determine if line segment from a to b intersects with
63 // line segment from c to d
64 bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
65     if (LinesCollinear(a, b, c, d)) {
66         if (dist2(a, c) < EPS || dist2(a, d) < EPS ||
67             dist2(b, c) < EPS || dist2(b, d) < EPS) return true;
68         if (dot(c-a, c-b) > 0 && dot(d-a, d-b) > 0 && dot(c-b, d-b) > 0)
69             return false;
70         return true;
71     }
72     if (cross(d-a, b-a) * cross(c-a, b-a) > 0) return false;
73     if (cross(a-c, d-c) * cross(b-c, d-c) > 0) return false;
74     return true;
75 }
76 // compute intersection of line passing through a and b
77 // with line passing through c and d, assuming that unique
78 // intersection exists; for segment intersection, check if
79 // segments intersect first
80 PT ComputeLineIntersection(PT a, PT b, PT c, PT d) {
81     b=b-a; d=c-d; c=c-a;
82     return a + b*cross(c, d)/cross(b, d);
83 }
84
85 // compute center of circle given three points
86 PT ComputeCircleCenter(PT a, PT b, PT c) {
87     b=(a+b)/2;
88     c=(a+c)/2;
89     return ComputeLineIntersection(b, b+RotateCW90(a-b), c, c+RotateCW90(a-c));
90 }
91
92 // determine if point is in a possibly non-convex polygon (by William
93 // Randolph Franklin); returns 1 for strictly interior points, 0 for
94 // strictly exterior points, and 0 or 1 for the remaining points.
95 // Note that it is possible to convert this into an *exact* test using
96 // integer arithmetic by taking care of the division appropriately
97 // (making sure to deal with signs properly) and then by writing exact
98 // tests for checking point on polygon boundary
99 bool PointInPolygon(const vector<PT> &p, PT q) {
100     bool c = 0;
101     for (int i = 0; i < p.size(); i++){
102         int j = (i+1)%p.size();
103         if ((p[i].y <= q.y && q.y < p[j].y ||
104             p[j].y <= q.y && q.y < p[i].y) &&
105             q.x < p[i].x + (p[j].x - p[i].x) * (q.y - p[i].y) / (p[j].y - p[i].y))
106             c = !c;
107     }
108     return c;
109 }
110
111 // determine if point is on the boundary of a polygon
112 bool PointOnPolygon(const vector<PT> &p, PT q) {
113     for (int i = 0; i < p.size(); i++)
114         if (dist2(ProjectPointSegment(p[i], p[(i+1)%p.size()], q), q) < EPS)
115             return true;
116     return false;
117 }
118
119 // compute intersection of line through points a and b with
120 // circle centered at c with radius r > 0
121 vector<PT> CircleLineIntersection(PT a, PT b, PT c, double r) {
122     vector<PT> ret;
123     b = b-a;
124     a = a-c;
125     double A = dot(b, b);
126     double B = dot(a, b);
127     double C = dot(a, a) - r*r;
128     double D = B*B - A*C;
129     if (D < -EPS) return ret;
130     ret.push_back(c+a+b*(-B+sqrt(D+EPS))/A);
131     if (D > EPS)
132         ret.push_back(c+a+b*(-B-sqrt(D))/A);
133     return ret;
134 }
135
136 // compute intersection of circle centered at a with radius r
137 // with circle centered at b with radius R
138 vector<PT> CircleCircleIntersection(PT a, PT b, double r, double R) {
139     vector<PT> ret;
140     double d = sqrt(dist2(a, b));

```

```

141 if (d > r+R || d+min(r, R) < max(r, R)) return ret;
142 double x = (d*d-R*R+r*r)/(2*d);
143 double y = sqrt(r*r-x*x);
144 PT v = (b-a)/d;
145 ret.push_back(a+v*x + RotateCCW90(v)*y);
146 if (y > 0)
147     ret.push_back(a+v*x - RotateCCW90(v)*y);
148 return ret;
149 }
150
151 // This code computes the area or centroid of a (possibly nonconvex)
152 // polygon, assuming that the coordinates are listed in a clockwise or
153 // counterclockwise fashion. Note that the centroid is often known as
154 // the "center of gravity" or "center of mass".
155 double ComputeSignedArea(const vector<PT> &p) {
156     double area = 0;
157     for(int i = 0; i < p.size(); i++) {
158         int j = (i+1) % p.size();
159         area += p[i].x*p[j].y - p[j].x*p[i].y;
160     }
161     return area / 2.0;
162 }
163 double ComputeArea(const vector<PT> &p) {
164     return fabs(ComputeSignedArea(p));
165 }
166 PT ComputeCentroid(const vector<PT> &p) {
167     PT c(0,0);
168     double scale = 6.0 * ComputeSignedArea(p);
169     for (int i = 0; i < p.size(); i++){
170         int j = (i+1) % p.size();
171         c = c + (p[i]+p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);
172     }
173     return c / scale;
174 }
175 // tests whether or not a given polygon (in CW or CCW order) is simple
176 bool IsSimple(const vector<PT> &p) {
177     for (int i = 0; i < p.size(); i++) {
178         for (int k = i+1; k < p.size(); k++) {
179             int j = (i+1) % p.size();
180             int l = (k+1) % p.size();
181             if (i == l || j == k) continue;
182             if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
183                 return false;
184         }
185     }
186     return true;
187 }

```