# **HW1 Programming Problem 5 (30 points)**

## **Problem Description**

Here, you will perform weighted KNN regression.

After you write your own code for weighted KNN regression, you will also try out sklearn's built-in KNN regressor.

Fill out the notebook as instructed, making the requested plots and printing necessary values.

### Summary of deliverables:

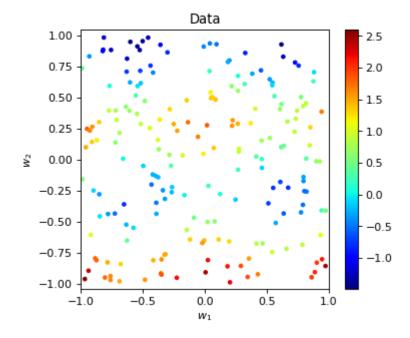
#### Functions:

weighted\_knn(w1, w2, k)

### Plots:

- 3 plots of by-hand KNN results
- 3 plots of sklearn.

```
In [96]: import numpy as np
         import matplotlib.pyplot as plt
         from sklearn.neighbors import KNeighborsRegressor
         # Data generation -- don't change
         np.random.seed(42)
         N = 200
         w1 data = np.random.uniform(-1,1,N)
         w2 data = np.random.uniform(-1,1,N)
         L_data = np.cos(4*w1_data) + np.sin(5*w2_data) + 2*w1_data**2 - w2_data/2
         # (end of data generation)
         plt.figure(figsize=(5,4.2),dpi=80)
         plt.scatter(w1 data,w2 data,s=10,c=L data,cmap="jet")
         plt.colorbar()
         plt.axis("equal")
         plt.xlabel("$w 1$")
         plt.ylabel("$w_2$")
         plt.xlim(-1,1)
         plt.ylim(-1,1)
         plt.title("Data")
         plt.show()
```



## Weighted KNN function

Here, define a function, weighted\_knn(w1, w2, k), which takes in a point at [ w1, w2 ] and a k value, and returns the weighted KNN prediction.

- As in the lecture activity, data is in the variables w1\_data, w2\_data, and L\_data.
- · You can create as many helper functions as you want
- The key difference between unweighted and weighted KNN is summarized below:

### **Unweighted KNN**

- 1. Find the k data points closest to the target point w
- 2. Get the output values at each of these points
- 3. Average these values together: this is the prediction at w

### Weighted KNN

- 1. Find the k data points closest to the target point w
- 2. Compute the proximity of each of these points as  $prox_i = 1/(distance(w, w_i) + 1e 9)$
- 3. For each  $w_i$ , multiply  $prox_i$  by the output value at  $w_i$ , and divide by the sum of all k proximities
- 4. Add all k of these results together: this is the prediction at w

```
In [97]: def distance(w1,w2):
             return np.sqrt((w1-w1 data)**2 + (w2-w2 data)**2)
         def knn indices(w1,w2,k):
             d = distance(w1, w2)
             return np.argpartition(d,k)[:k]
         def weighted knn(w1, w2, k):
             dist = distance(w1,w2)
             indices = knn indices(w1,w2,k)
             val = 0
             prox_sum = 0
             prox = 0
             for j in range(k):
                 prox_sum += 1/(dist[indices[j]] + 10**(-9))
             for i in range(k):
                 prox = 1/(dist[indices[i]] + 10**(-9))
                 w = prox/prox sum
                 val += L_data[indices[i]]*w
             return val
         print(weighted_knn(3,2,5))
```

-0.6155380702535808

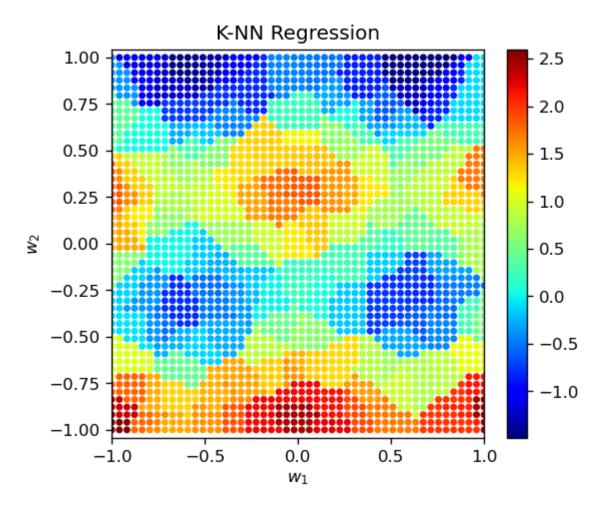
## **Plotting**

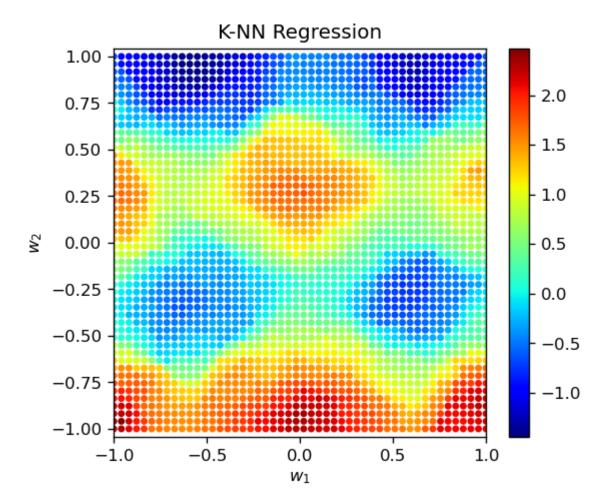
Now create 3 plots showing KNN regressor predictions for k values [1, 5, 25].

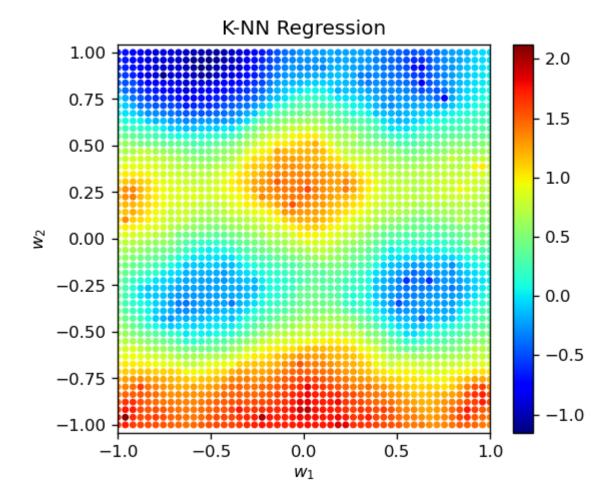
You should plot a 50x50 grid of points on a grid for w1 and w2 values between -1 and 1. Consult the lecture activity for how to do this.

We recommend creating a function, e.g. plot(k), so that you need to rewrite less code.

```
In [117]: w1 vals = np.linspace(-1,1,50)
          w2 vals = np.linspace(-1,1,50)
          w1s, w2s = np.meshgrid(w1_vals,w2_vals)
          w1 grid, w2 grid = w1s.flatten(), w2s.flatten()
          k 1 = 1
          L_grid_1 = np.zeros_like(w1_grid)
          k 2 = 5
          L_grid_2 = np.zeros_like(w1_grid)
          k \ 3 = 25
          L_grid_3 = np.zeros_like(w1_grid)
          for i in range(len(L grid)):
              L_grid_1[i] = weighted_knn(w1_grid[i], w2_grid[i],k_1)
              L_grid_2[i] = weighted_knn(w1_grid[i], w2_grid[i],k_2)
              L_grid_3[i] = weighted_knn(w1_grid[i], w2_grid[i],k_3)
          def plot(L grid):
              plt.figure(figsize=(5,4.2),dpi=120)
              plt.scatter(w1_grid,w2_grid,s=10,c=L_grid,cmap="jet")
              plt.colorbar()
              plt.axis("equal")
              plt.xlabel("$w 1$")
              plt.ylabel("$w 2$")
              plt.xlim(-1,1)
              plt.ylim(-1,1)
              plt.title("K-NN Regression")
              plt.show()
          plot(L grid 1)
          plot(L_grid_2)
          plot(L_grid_3)
          # Visualize results for k = 1, 5, and 25
```







## **Using SciKit-Learn**

We can also use sklearn's KNeighborsRegressor(), which is a very efficient implementation of KNN regression.

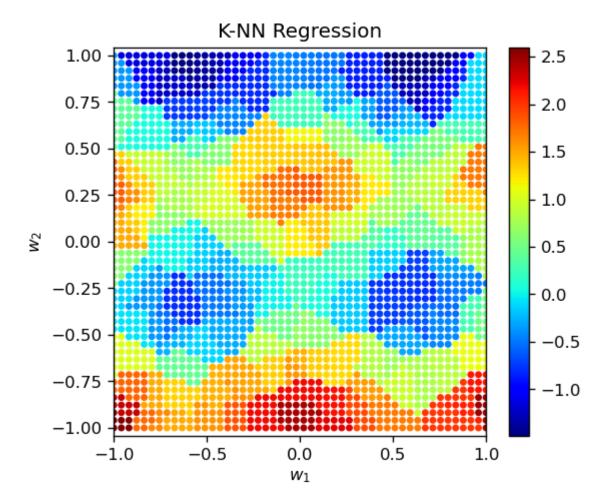
The code to do this has been done for one case below. First, make note of how this is done.

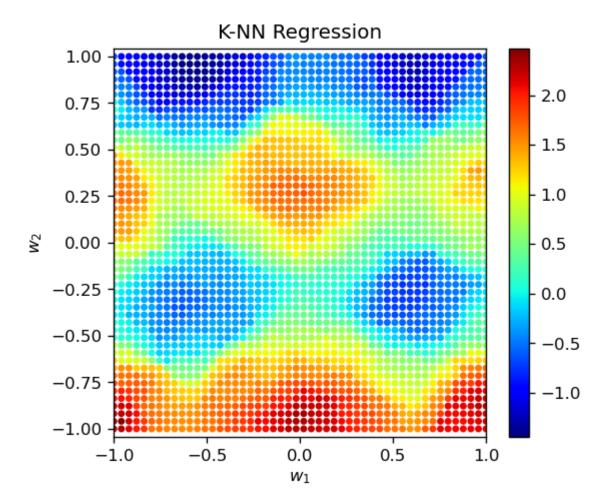
```
In [118]: model = KNeighborsRegressor(n_neighbors = 1, weights="distance")
X = np.vstack([w1_data,w2_data]).T
model.fit(X, L_data)

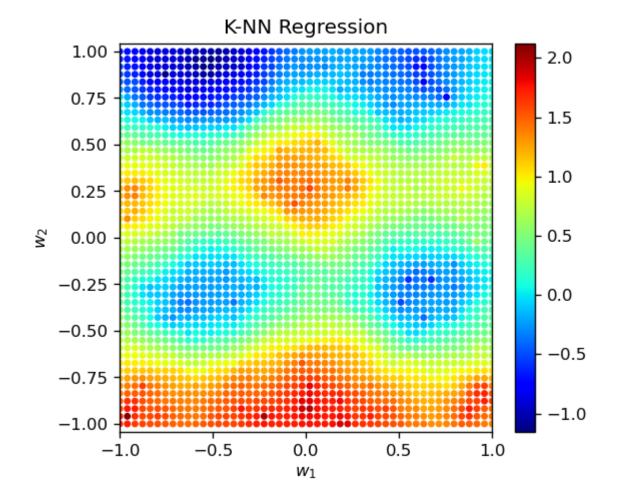
# Get a prediction at a point (0, 0):
print(model.predict(np.array([[0,0]])))
[1.19743607]
```

Now create 3 plots for the same values of k as before, using this KNN implementation instead. You can make sure these are visually the same as your from-scratch KNN regressor.

```
In [120]: def plot(k):
              model = KNeighborsRegressor(n_neighbors = k, weights="distance")
              X = np.vstack([w1_data,w2_data]).T
              model.fit(X,L data)
              w1_vals = np.linspace(-1,1,50)
              w2_vals = np.linspace(-1,1,50)
              w1s, w2s = np.meshgrid(w1_vals,w2_vals)
              w1 grid, w2 grid = w1s.flatten(), w2s.flatten()
              L_grid = np.zeros_like(w1_grid)
              for i in range(len(L grid)):
                  L_grid[i] = model.predict([[w1_grid[i],w2_grid[i]]])
              plt.figure(figsize=(5,4.2),dpi=120)
              plt.scatter(w1_grid,w2_grid,s=10,c=L_grid,cmap="jet")
              plt.colorbar()
              plt.axis("equal")
              plt.xlabel("$w_1$")
              plt.ylabel("$w_2$")
              plt.xlim(-1,1)
              plt.ylim(-1,1)
              plt.title("K-NN Regression")
              plt.show()
          plot(1)
          plot(5)
          plot(25)
          # Visualize sklearn results for k = 1, 5, and 25
```







In [ ]: