Problem 3 (5 points)

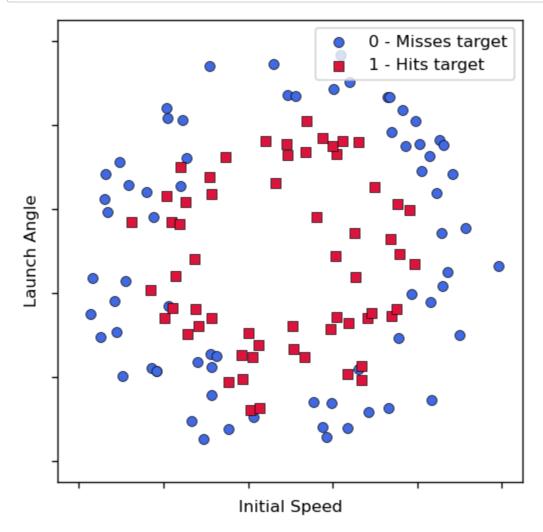
```
In [1]: import numpy as np
        import matplotlib.pyplot as plt
        def plot_data(data, c, title="", xlabel="$x_1$",ylabel="$x_2$",classes=["",""],a]
            N = len(c)
            colors = ['royalblue','crimson']
            symbols = ['o', 's']
            plt.figure(figsize=(5,5),dpi=120)
            for i in range(2):
                x = data[:,0][c==i]
                y = data[:,1][c==i]
                plt.scatter(x,y,color=colors[i],marker=symbols[i],edgecolor="black",line
            plt.legend(loc="upper right")
            plt.xlabel(xlabel)
            plt.ylabel(ylabel)
            ax = plt.gca()
            ax.set xticklabels([])
            ax.set_yticklabels([])
            plt.xlim([-0.05,1.05])
            plt.ylim([-0.05,1.05])
            plt.title(title)
        def plot_contour(predict, mapXY = None):
            res = 500
            vals = np.linspace(-0.05,1.05,res)
            x,y = np.meshgrid(vals,vals)
            XY = np.concatenate((x.reshape(-1,1),y.reshape(-1,1)),axis=1)
            if mapXY is not None:
                XY = mapXY(XY)
            contour = predict(XY).reshape(res, res)
            plt.contour(x, y, contour)
```

Generate Dataset

(Don't edit this code.)

```
In [2]: def sample_ring(N,x,y,ro,ri):
    theta = np.random.rand(N)*2*np.pi
    r = np.sqrt(r*(ro**2-ri**2)+ri**2)
    xs = x + r * np.cos(theta)
    ys = y + r * np.sin(theta)
    return xs, ys

def get_ring_dataset():
    np.random.seed(0)
    c0 = sample_ring(70,0.5,0.5,0.5,0.3)
    c1 = sample_ring(60,0.45,0.47,0.36,0.15)
    xs = np.concatenate([c0[0],c1[0]],0)
    ys = np.concatenate([c0[1],c1[1]],0)
    c = np.concatenate([np.zeros(70),np.ones(60)],0)
    return np.vstack([xs,ys]).T, c
```



Feature Expansion

Define a function to expand 2 features into more features For the features x_1 and x_2 , expand into:

- 1
- *x*₁
- X2
- x_1^2
- x_2^2
- $\sin(x_1)$
- $cos(x_1)$
- $\sin(x_2)$
- $cos(x_2)$
- $\sin^2(x_1)$
- $\cos^2(x_1)$
- $\sin^2(x_2)$
- $\cos^2(x_2)$
- $\exp(x_1)$
- $\exp(x_2)$

Dataset size: (130, 2) Expanded dataset size: (130, 15)

Logistic Regression

Use SciKit-Learn's Logistic Regression model to learn the decision boundary for this data, using regularization. (The C argument controls regularization strength.)

Train this model on your expanded feature set.

Details about how to use this are here: https://scikit-

<u>learn.org/stable/modules/generated/sklearn.linear_model.LogisticRegression.html (https://scikitlearn.org/stable/modules/generated/sklearn.linear_model.LogisticRegression.html)</u>

Notes:

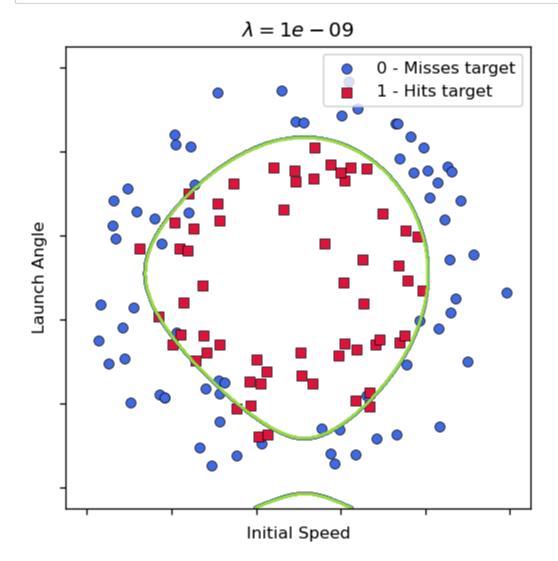
```
In [5]: from sklearn.linear_model import LogisticRegression

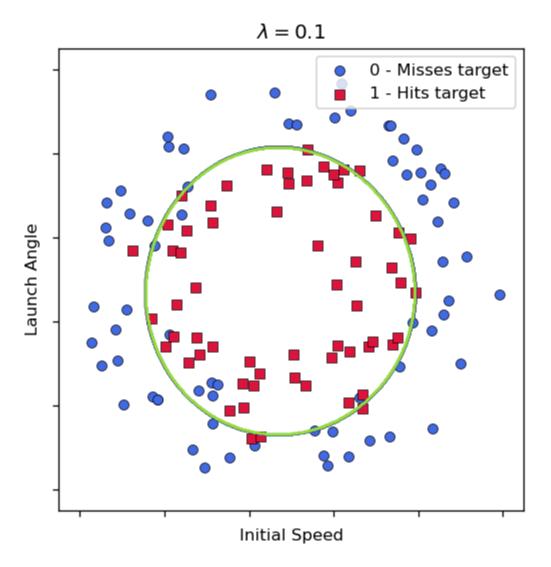
def get_logistic_regressor(features, classes, L = 1):
    # YOUR CODE GOES HERE

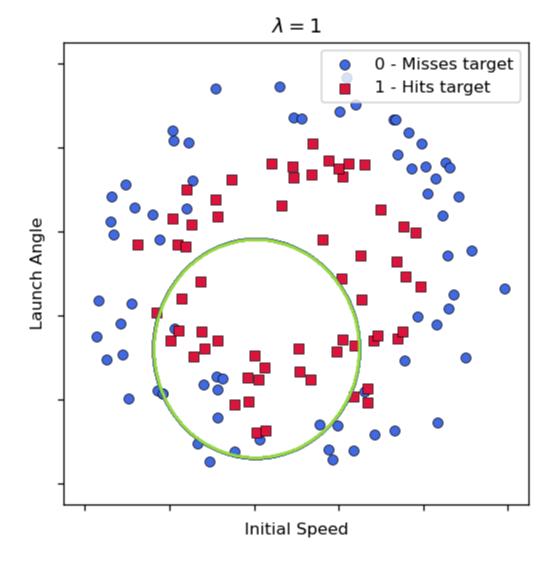
model = LogisticRegression(C=1/L,max_iter=10000)
model.fit(features,classes)

# - Instantiate model with regularization
# - Fit model to expanded data
return model
```

```
In [6]: for L in [1e-9, 1e-1, 1]:
    model = get_logistic_regressor(features, classes, L)
    plot_data(data, classes, **format, title=f"$\lambda={L}$")
    plot_contour(model.predict, feature_expand)
    plt.show()
```







As λ increases, note what happens to the decision boundary. Why does this occur?

As λ increases the regularization strength increases which leads to a smoother, simpler and more constrained decision boundry. It gives us a more fitted boundary. Increasing λ decreases the overfitting it. as the regularization strength increases the w-vector values become smaller which in turn simplifies the model and therefore leading to a better decision boundary

In []: