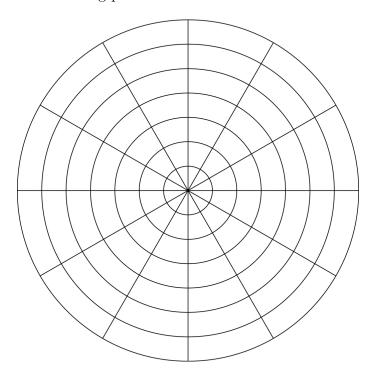
12.2: Polar Coordinates

Learning Objectives. Upon successful completion of Section 12.2, you will be able to...

- Answer conceptual questions involving polar coordinates.
- Graph with polar coordinates and give alternate polar representations of polar points.
- Convert between polar and Cartesian coordinates.
- Convert between polar equations and Cartesian equations.
- Graph simple polar curves.
- Identify corresponding points given Cartesian and polar graphs of the same curve.

Introduction to Polar Coordinates

△ Example. Plot the following polar coordinates.



Coordinate Conversion

Let the polar axis coincide with the positive x-axis and the pole with the origin.

Example. Find the Cartesian coordinates of the point with polar coordinates $\left(-4, \frac{3\pi}{4}\right)$.

Example. Find polar coordinates (with r > 0) of the point with Cartesian coordinates $(-4, 4\sqrt{3})$. Also find polar coordinates with r > 0 for this point.

Polar Curves

The graph of a polar equation $r = f(\theta)$ consists of all points P that have at least one polar representation (r, θ) whose coordinates satisfy the equation.

Basic Curves

r = a, Example: r = 3

 $\theta = b$, Example: $\theta = 5\pi/6$

Example. Convert the following equation to Cartesian coordinates. Describe the resulting curve.

$$r = 6\cos\theta + 8\sin\theta$$

Symmetry in Polar Equations

• We have symmetry about the **x-axis** (polar axis) if (r, θ) is on the graph whenever $(r, -\theta)$ is.

- We have symmetry about the **y-axis** $(\theta = \pi/2)$ if (r, θ) is on the graph whenever $(r, \pi \theta) = (-r, -\theta)$ is.
- We have symmetry about the origin (the pole) if (r, θ) is on the graph whenever $(-r, \theta) = (r, \theta + \pi)$ is.

Sketching Polar Curves

Example. Sketch the graph of the polar curve $r = 4 + 4\cos\theta$ using a table of values and symmetry.