

## Homework 0: CS 436/ 580L: Introduction to Machine Learning

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Name: VAIBHAV CHAUHAN

B-Number: B00677602

### Academic Honesty Pledge

I have done this assignment completely on my own. I have not copied it, nor have I given my solution to anyone else. I understand that if I am involved in plagiarism or cheating I will have to sign an official form that I have cheated and that this form will be stored in my official university record. I also understand that I will receive a grade of 0 for the involved assignment for my first offense and that I will receive a grade of "F" for the course for any additional offense.

E-Signature: VAIBHAV CHAUHAN

Ans 1

Sample Space -  $(1,1)(1,2).... = 6*6=36$

Rolling Doubles =  $(1,1)(2,2)....(6,6)$

$P(\text{Rolling Doubles}) = 6/36 = 1/6$

Ans 2

For independent variables

$P[a,b]=P(a)P(b)$

$0.2 = 0.5 * P[Y]$

$P[Y] = 2/5$

Ans 3

For the person to be in starting position after 10 steps he has to take 5 steps forward and 5 steps backward.

$P(\text{Forward Step})=0.6$

$P(\text{Backward step})=0.4$

As all these steps are independent

There are  $10c5$  ways to do it.

$$P(\text{At starting position}) = 10c5 * (0.6^5) * (0.4^5)$$

Ans 4

$$E[Z] = E[X^2] * E[Y]$$

$$\text{But } E[X^2] = \text{var}[X] + (E[X])^2$$

$$E[Z] = (\text{var}[X] + (E[X])^2) * E[Y]$$

$$E[Z] = (1 + 2^2) * 3$$

$$E[Z] = 15$$

Ans 5

$$\text{Mean} = (-1 + 1 + 4 + 6 + 10) / 5 = 5$$

$$\text{Median} = 4$$

$$\text{Variance} = ((-1-5)^2 + (1-5)^2 + (4-5)^2 + (6-5)^2 + (10-5)^2) / 5 = 79/5 = 15.8$$

Ans 6

$$E(\text{Win}) = 0.2 * 10\$$$

$$E(\text{Loss}) = 0.8 * 5\$$$

$$E(\text{Gain}) = E(\text{Win}) - E(\text{Loss})$$

$$E(\text{Gain}) = 0.2 * 10 - 0.8 * 5 = 2 - 4 = -2\$$$

Ans 7

Given first card was spade

$$\text{Total spade} = 12$$

$$\text{Total Cards} = 51$$

$$P(\text{spade} | \text{first card is spade}) = 12/51 = 4/17$$

Ans 8

$$P(\text{Head} | \text{White Ball}) = P(\text{White Ball} | \text{Head})P(\text{Head})/P(\text{White Ball})$$

$$P(\text{White Ball} | \text{Head}) = 2/9$$

$$P(\text{Head}) = 1/2$$

$$P(\text{White Ball}) = 1/2 * 2/9 + 1/2 * 5/11$$

$$P(\text{Head} | \text{White Ball}) = (2/9 * 1/2) / (1/2 * 2/9 + 1/2 * 5/11)$$

$$P(\text{Head} | \text{White Ball}) = 22/67$$

Ans 9

$$P(6 \text{ heads and } 4 \text{ tails}) = {}^{10}C_6 * p^6(1-p)^4$$

$$P(7 \text{ heads and } 3 \text{ tails}) = {}^{10}C_7 * p^7(1-p)^3$$

Like this-

$${}^{10}C_6 * p^6(1-p)^4 + {}^{10}C_7 * p^7(1-p)^3 + {}^{10}C_8 * p^8(1-p)^2 + {}^{10}C_9 * p^9(1-p) + {}^{10}C_{10} * p^{10}$$

Ans 10

$$\text{If man wins in 1st chance} = p$$

$$\text{If man wins in 2nd chance} = p * (1-p)$$

$$\text{If man wins in 3rd chance} = p * (1-p)^2$$

$$\text{If man wins in nth chance} = p * (1-p)^n$$

This is Geometric Distribution.