

Clustering

↳ unsupervised machine

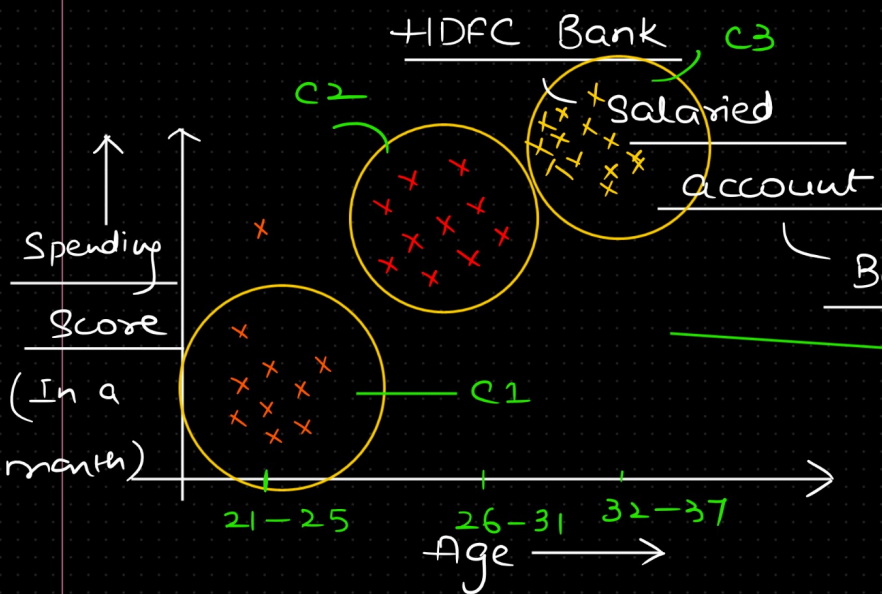
learning

labelled data not available

Bengaluru

Customers

segmentation



Clusters

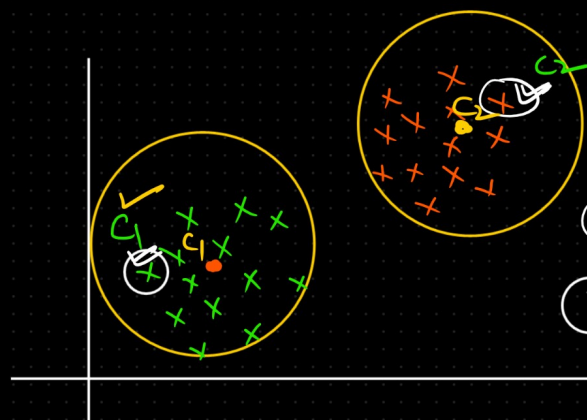
K-Means Clustering

↳ Elbow Method

Optimal value of k (num of clusters)

(1) Euclidean

(2) Manhattan



Euclidean Distance

$k = 2$

$P_1(x_1, y_1)$

$P_2(x_2, y_2)$

C1 (Distance of all data points from cluster c_1 & c_2)

C2

$$\sqrt{(y_2 - y_1)^2 + (x_2 - x_1)^2}$$

Manhattan Distance

P_1
 (x_1, y_1)

P_2
 (x_2, y_2)

$$|y_2 - y_1| + |x_2 - x_1|$$

$P_1(2,10)$ $P_2(2,5)$ $P_3(8,4)$ $P_4(5,8)$ $P_5(7,5)$

C_1 $P_6(6,4)$ $P_7(1,2)$ $P_8(4,9)$

(new value)
 $C_2 \rightarrow$

$$x = \frac{8+5+7+6+4}{5}$$

$$y = \frac{4+8+5+4+9}{5}$$

$k=3$

num
of
clusters

$P_1(2,10)$

$P_4(5,8)$

$P_7(1,2)$

C_1

C_2

C_3

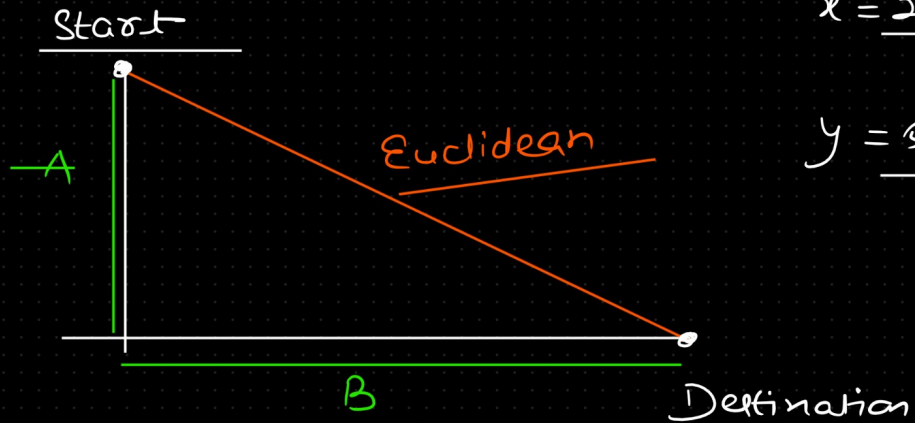
$P_1(2,10)$

P_3, P_4, P_5, P_6, P_8

P_2, P_7

$$x = \frac{2+1}{2}$$

$$y = \frac{5+2}{2}$$



$A + B = \text{manhattan}$

Distance

Distance \leftarrow Euclidean

$$(C_1, P_1) = 0$$

$$(C_1, P_2) = 10$$

$$(C_1, P_3)$$

$$(C_1, P_4)$$

$$(C_1, P_8)$$

$$(C_2, P_1) = 5$$

$$(C_2, P_2) = 7$$

$$(C_2, P_8)$$

$$(C_3, P_1) = 10$$

$$(C_3, P_2) = 5$$

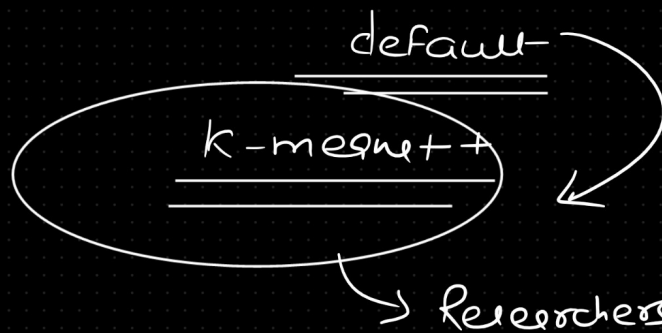
$$(C_3, P_8)$$

Stopping criteria

→ in the next iteration, new values of (c_1, c_2, c_3) if

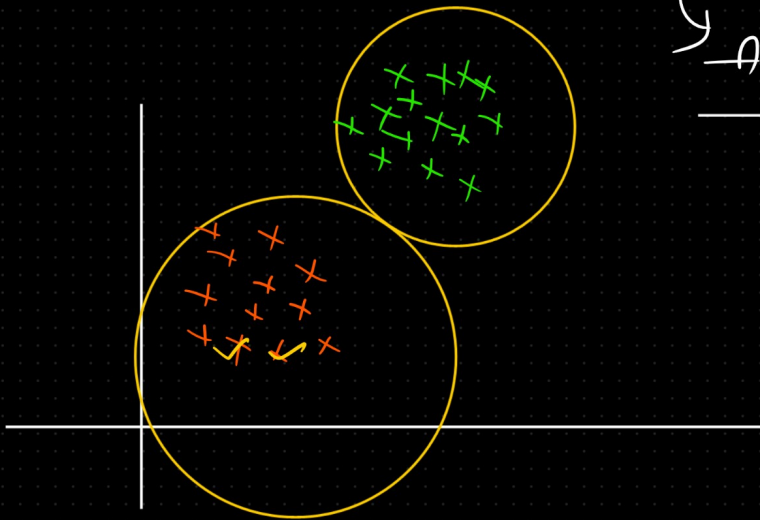
almost similar which we had in the previous iteration.

← form a stable cluster



→ Advance k-means

↓
Centroid
→ at far
distances



$k=1$

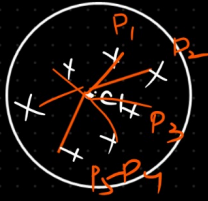
WCSS = max Optimal value of k

data points

\rightarrow WCSS \rightarrow Within cluster
Summation of
squares

$k=3$

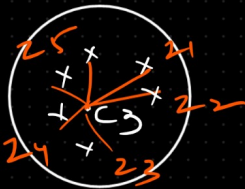
WCSS = 0



$$\Rightarrow (C_1 - P_1)^2 + (C_1 - P_2)^2 + \dots + (C_1 - P_7)^2$$



$$\Rightarrow (C_2 - X_1)^2 + (C_2 - X_2)^2 + \dots + (C_2 - X_5)^2$$



$$\Rightarrow (C_3 - Z_1)^2 + (C_3 - Z_2)^2 + \dots +$$

$$(C_3 - Z_5)^2$$

Elbow Method

