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## Generating Signals and Mitures

```
clc;
clear all;
close all;

% Defining the time period and frequency for the signals.
tp = 0:0.1:5;
freq = 0.5;

% Genrating 3 signals. Three types of waveforms have been used -
% Sine, Sawtooth and Square
signal1 = sin(2*pi*freq*tp);
signal2 = sawtooth(2*pi*freq*tp);
signal3 = square(2*pi*freq*tp);

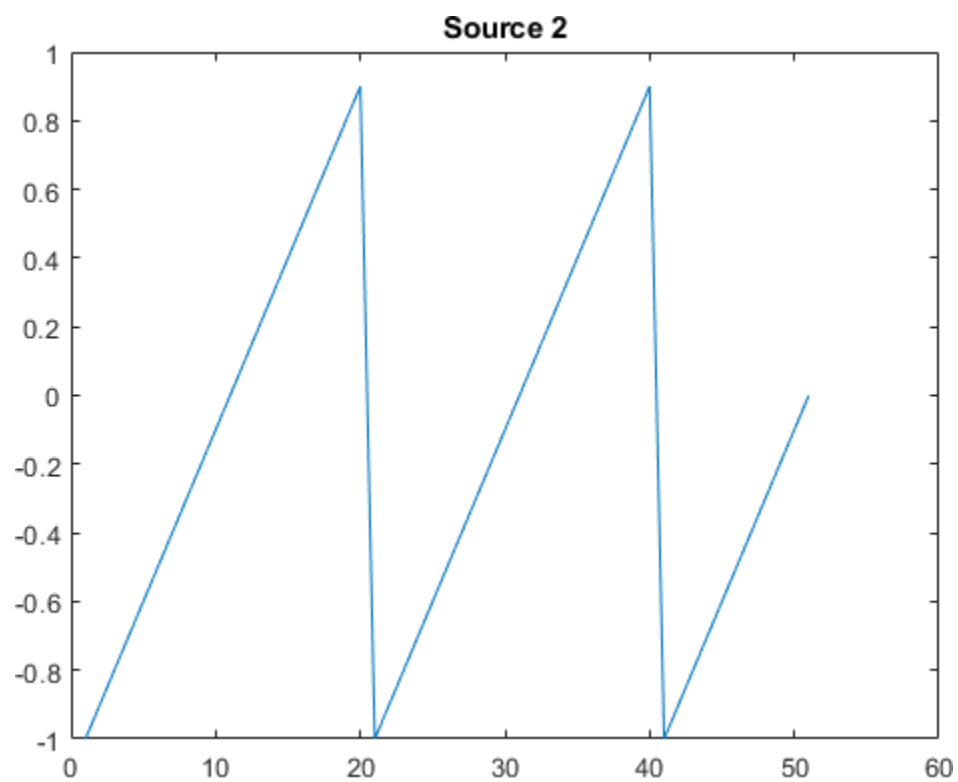
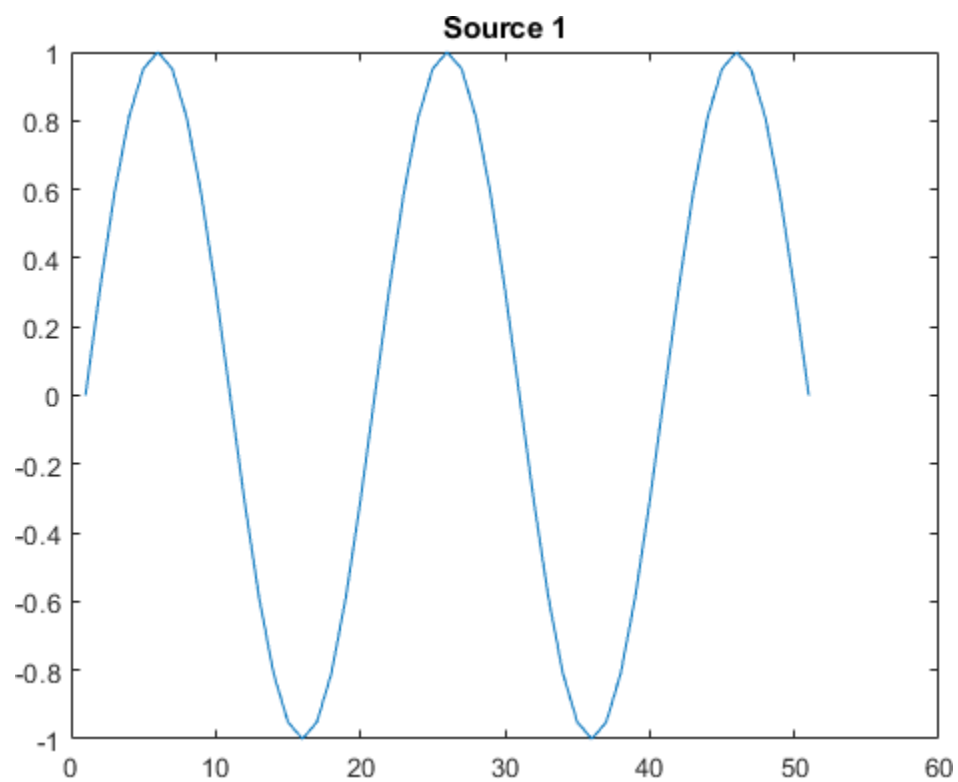
% Plotting the 3 source sigals
figure, plot(signal1),title('Source 1');
figure, plot(signal2),title('Source 2');
figure, plot(signal3),title('Source 3');

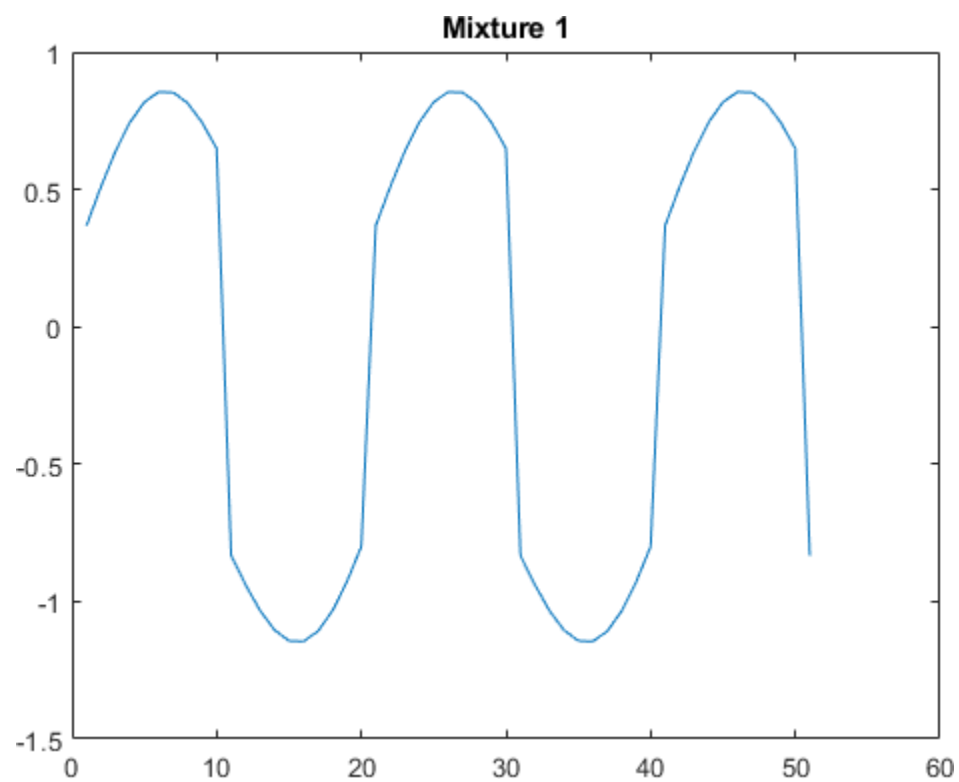
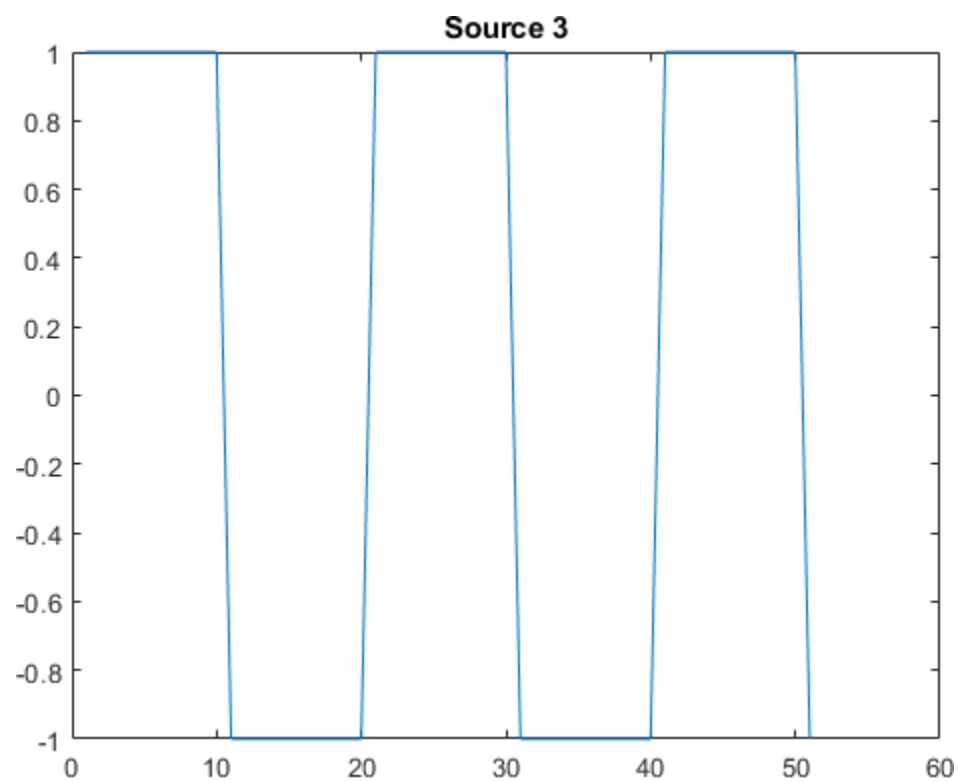
% Generating two mixtures of signals by multiplying each signal with a
% random number and adding them up.
x1 = rand(1)*signal1 + rand(1)*signal2 + rand(1)*signal3;
x1 = x1/max(x1);
x2 = rand(1)*signal1 + rand(1)*signal2 + rand(1)*signal3;
x2 = x2/max(x2);
x1_bar = x1 - mean(x1);
x2_bar = x2 - mean(x2);

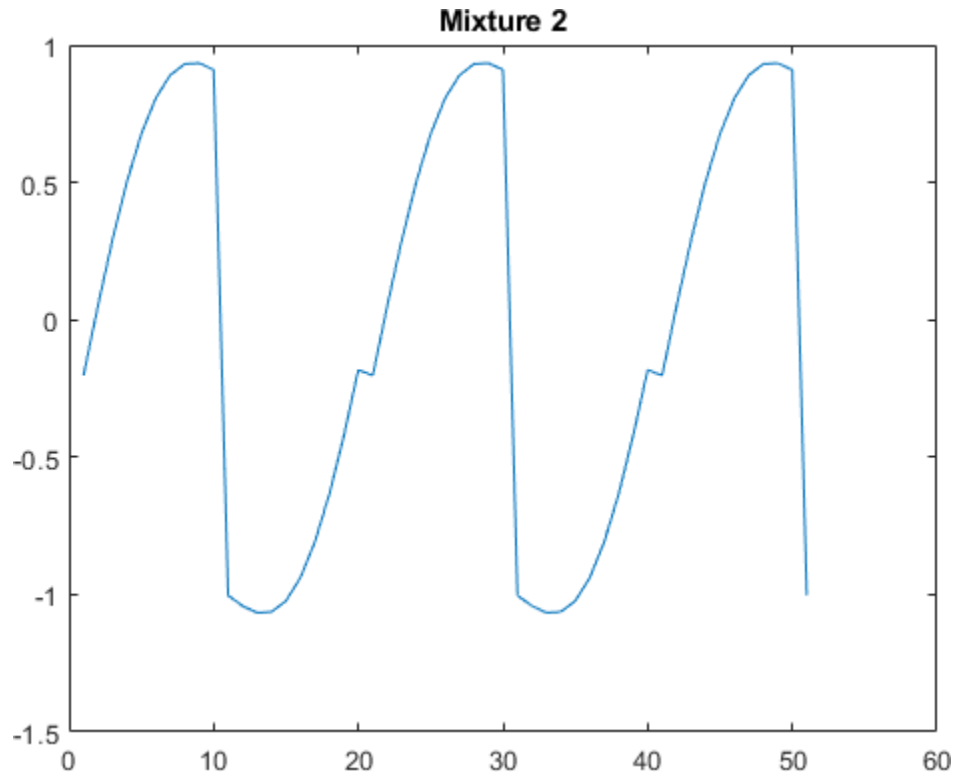
% Plot for generated mitures
figure, plot(x1_bar),title('Mixture 1');
figure, plot(x2_bar),title('Mixture 2');

% Combining the mixtures into a matrix
X = [x1 ; x2];

% Combining the sources into a matrix
S = [signal1 ; signal2 ; signal3];
```







## Obtaining Signals back from given Mixtures

```
% A has been initialised with the values suggested in the paper
% Columns of A i.e  $a_i = (\cos(\alpha_i), \sin(\alpha_i))$  with  $\alpha$  between
% 0 and  $\pi$ .
alpha1 = pi/4;
alpha2 = pi/2;
alpha3 = 3*pi/4;
A = [cos(alpha1), cos(alpha2), cos(alpha3); -cos(alpha1), -
cos(alpha2), sin(alpha3)];

% Initializing Weights(Neurons) as suggested in the paper

w1 = [cos(alpha1)];
w_1 = [-cos(alpha1)];
w2 = [cos(alpha2)];
w_2 = [-cos(alpha2)];
w3 = [cos(alpha3)];
w_3 = [sin(alpha3)];

% Learning rate
n = 0.5;

% There are a total of 6 weights in the mixing matrix and each weight
```

```

% has been updated 50 times to obtain suitable values of weights for
    further
% calculations.
% Pie function as mentioned in the paper has been used.

for i= 2:51 % Updation of weight 1 for x1
    y = pie(x1_bar(1,1:i-1));
    a = w1 + n * pie(-1*y-w1);
    w1 = [1/3 pie(a)];
end
w1_f = w1(1,51);

for i= 2:51 % Updation of weight 1 for x1
    y = pie(x1_bar(1,1:i-1));
    a = w2 + n * pie(y-w2);
    w2 = [2/3 pie(a)];
end
w2_f = w2(1,51);

for i= 2:51 % Updation of weight 3 for x1
    y = pie(x1_bar(1,1:i-1));
    a = w3 + n * pie(-1*y-w3);
    e1 = i-1;
    if(isnan(a))
        break;
    end
    w3 = [1 pie(a)];
end

if(e1 == 50)
    w3_f = w3(1,51);
else
    w3_f = w3(1,e1);
end

for i= 2:51 % Updation of weight 1 for x2
    y = pie(x2_bar(1,1:i-1));
    a = w_1 + n * pie(y-w_1);
    w_1 = [-1/3 pie(a)];
end
w_1_f = w_1(1,51);

for i= 2:51 % Updation of weight 2 for x2
    y = pie(x2_bar(1,1:i-1));
    a = w_2 + n * pie(y-w_2);
    w_2 = [-2/3 pie(a)];
end
w_2_f = w_2(1,51);

for i= 2:51 % Updation of weight 3 for x2
    y = pie(x2_bar(1,1:i-1));
    a = w_3 + n * pie(-1*y-w_3);
    e2 = i-1;
    if(isnan(a))
        break;
    end
end

```

```

        end
        w_3 = [-1 pie(a)];
    end

    if(e2 == 50)
        w_3_f = w_3(1,51);
    else
        w_3_f = w_3(1,e2);
    end

    %Final mixing matrix has been obtained after getting updated weights
    A_obtained = [w1_f, w2_f, w3_f ; w_1_f, w_2_f, w_3_f];

    %Scaling matrix L has been initialised
    L = [0.5, 0, 0 ; 0, 0.5, 0 ; 0, 0, 1];

    %Permuation matrix
    P = eye(3);

    %Approximation matrix of A
    B = A_obtained*P*L;
    E = B-A;
    error = norm(E);
    disp(error);

    %Psuedo inverse of B has been used to find the source
    S_pred = pinv(B)*X;

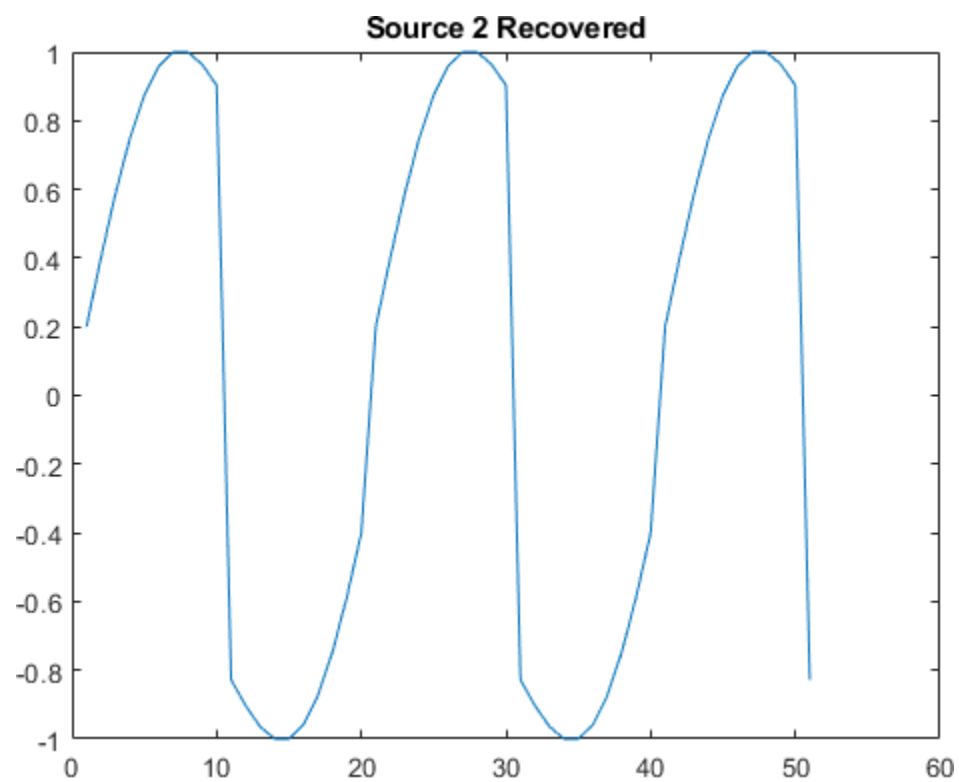
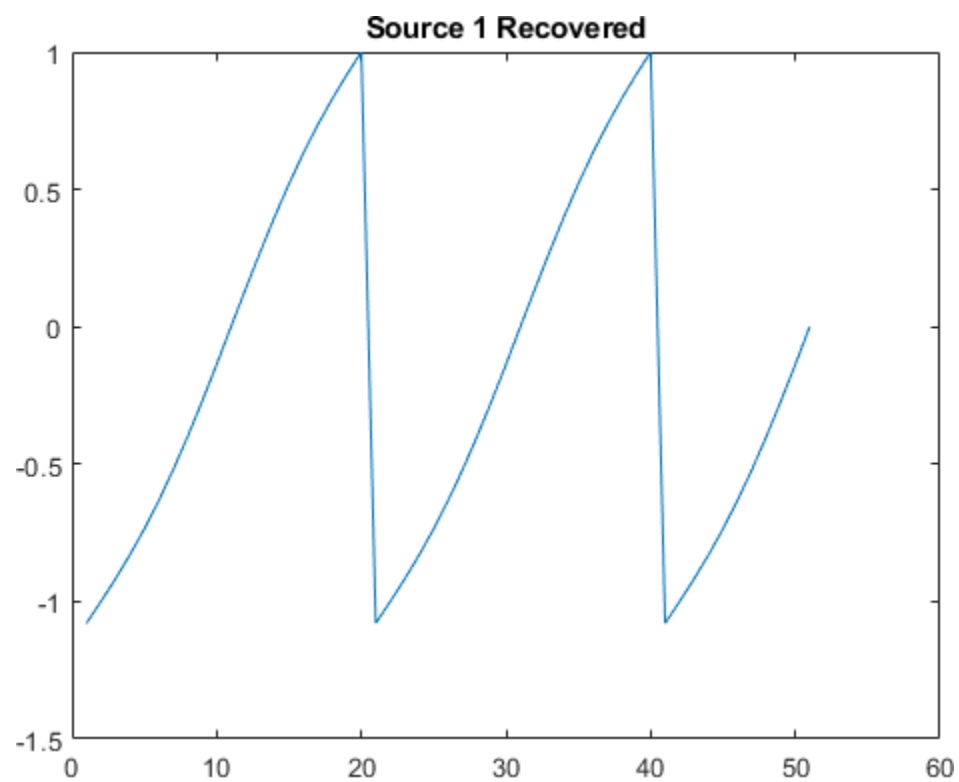
    %Plotting the obtained source signals
    s11 = S_pred(1,:);
    s11 = s11/max(s11);
    figure,plot(s11),title('Source 1 Recovered');

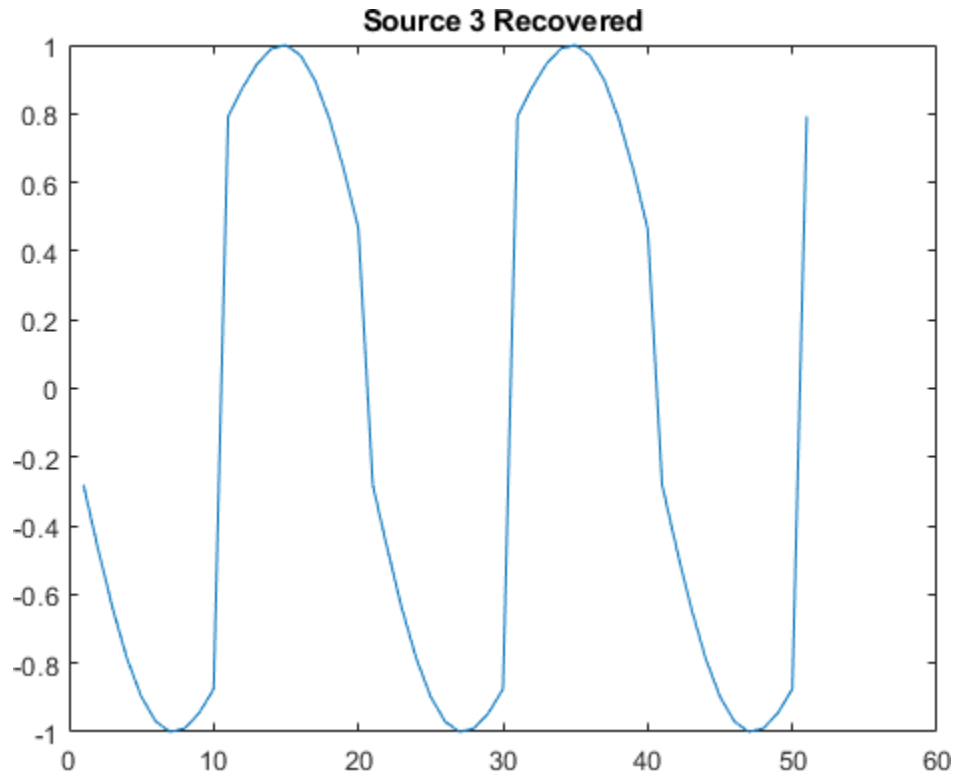
    s22 = S_pred(2,:);
    s22 = s22/max(s22);
    figure,plot(s22), title('Source 2 Recovered');

    s33 = S_pred(3,:);
    s33 = s33/max(s33);
    figure,plot(s33),title('Source 3 Recovered');

    1.5097

```





## K means Clustering

```
% Taking transpose of mixture x1
x1 = x1_bar';
% Taking transpose of mixture x2
x2 = x2_bar';

% All classification of mixture x1 are represented by the vector
idx_mean
[idx_mean, C_mean] = kmeans(x1,3);
% All classification of mixture x2 are represented by the vector
idx2_mean
[idx2_mean, C2_mean] = kmeans(x2,3);

% Plotting cluster of mixture x1
figure;
gscatter(x1(:,1),idx_mean),title('Clusters of mixture 1');
% Plotting cluster of mixture x2
figure;
gscatter(x2(:,1),idx2_mean),title('Clusters of mixture 2');

% Initializing frequencies of clusters in mixture x1
p1_mean = 0;
p2_mean = 0;
```



```

p3_mean = 0;

for i=1:51
    if idx_mean(i,1)==1
        p1_mean = p1_mean+1; % Calculating frequency of cluster 1 in
mixture x1
    elseif idx_mean(i,1)==2
        p2_mean = p2_mean+1; % Calculating frequency of cluster 2 in
mixture x1
    else
        p3_mean = p3_mean+1; % Calculating frequency of cluster 3 in
mixture x1
    end
end

% Calculating posterior probabilities using the frequency of each
cluster
% in the mixture x1
posterior11_mean = p1_mean/51;
posterior21_mean = p2_mean/51;
posterior31_mean = p3_mean/51;

% Initializing frequencies of clusters in mixture x2
p11_mean = 0;
p22_mean = 0;
p33_mean = 0;

for i=1:51
    if idx2_mean(i,1)==1
        p11_mean = p11_mean+1; % Calculating frequency of cluster 1 in
mixture x2
    elseif idx2_mean(i,1)==2
        p22_mean = p22_mean+1; % Calculating frequency of cluster 2 in
mixture x2
    else
        p33_mean = p33_mean+1; % Calculating frequency of cluster 3 in
mixture x2
    end
end

% Calculating posterior probabilities using the frequency of each
cluster
% in the mixture x2
posterior12_mean = p11_mean/51;
posterior22_mean = p22_mean/51;
posterior32_mean = p33_mean/51;

% Finding mixing matrix A from obtained posterior values after
clustering
A1 = [posterior11_mean, posterior21_mean, posterior31_mean ;
posterior12_mean, posterior22_mean, posterior32_mean];

% Scaling matrix L
L = [0.5, 0, 0 ; 0, 0.5, 0 ; 0, 0, 1];

```

```

% Permutation matrix
P = eye(3);

% Approximation matrix of A1
B_mean = A1*P*L;
E_mean = B_mean-A;
error_mean = norm(E_mean);
disp(error_mean);

% Pseudoinverse of B has been used to approximate the source
S2_mean = pinv(B_mean)*X;

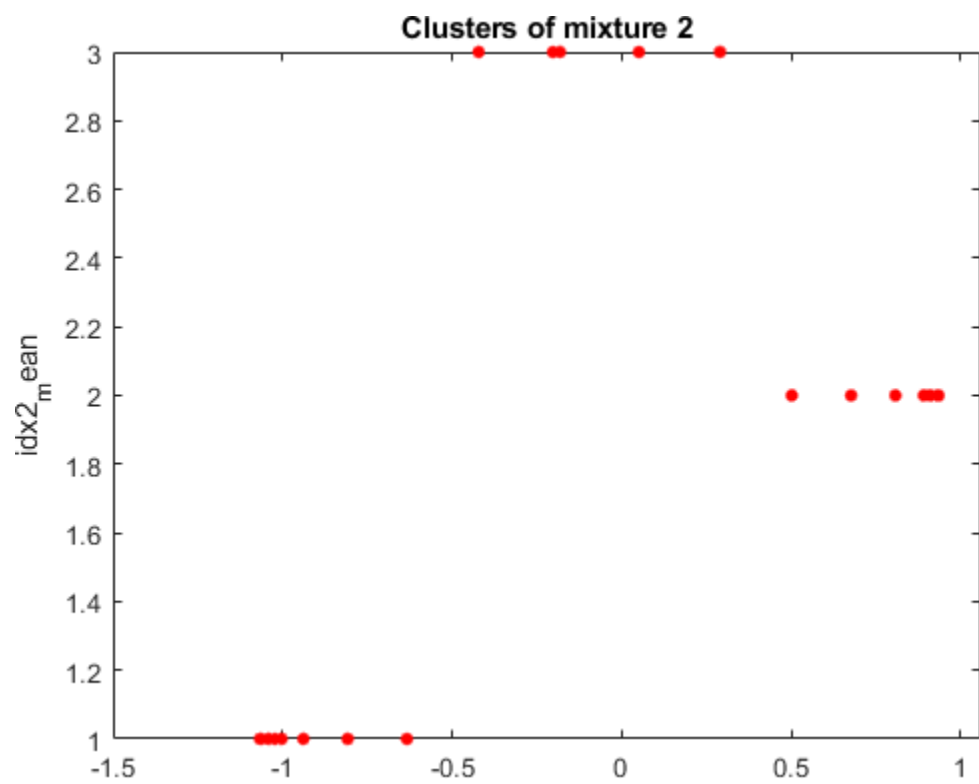
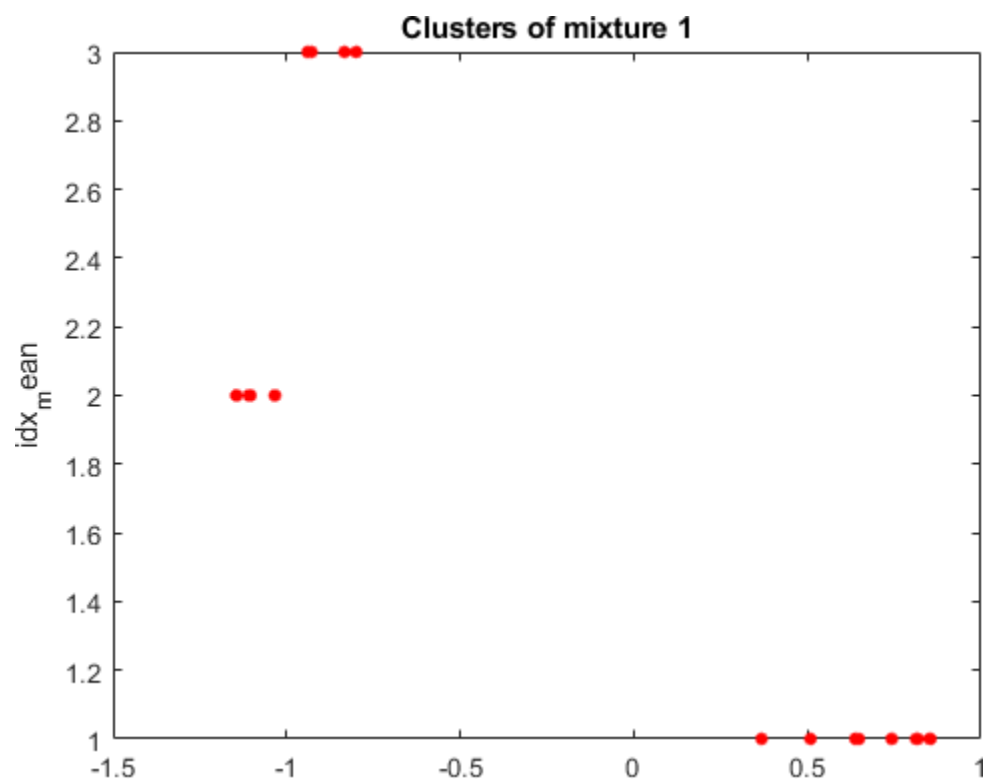
% Plotting the obtained source signals
S_11_mean = S2_mean(1,:);
figure, plot(S_11_mean),title('Source 1 Recovered by K-means
Clustering');

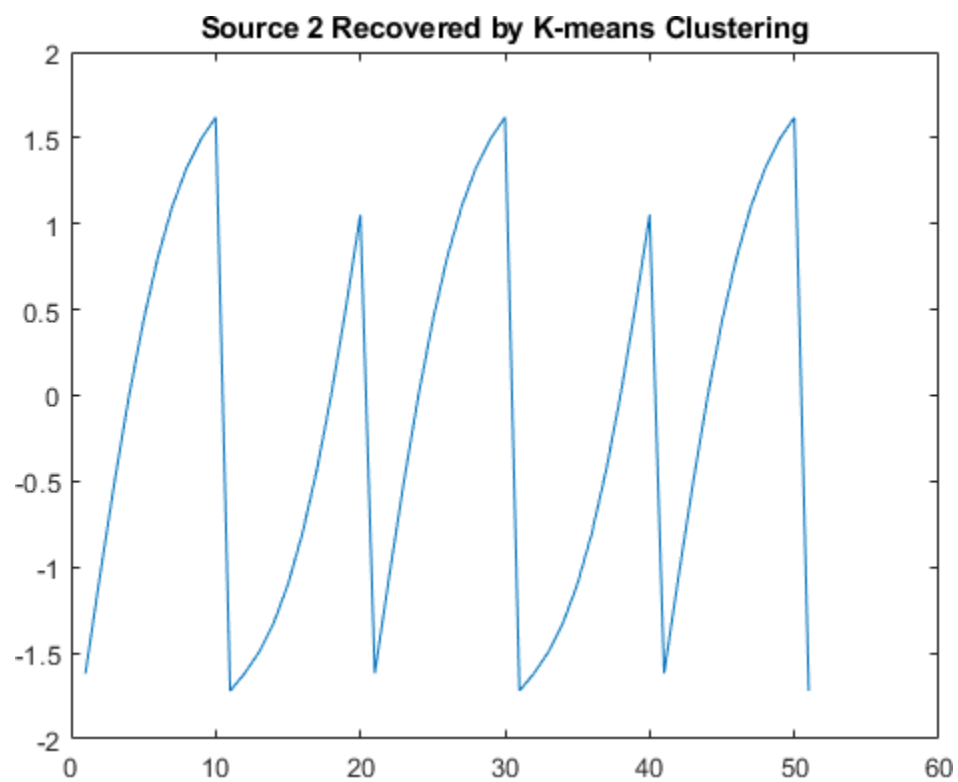
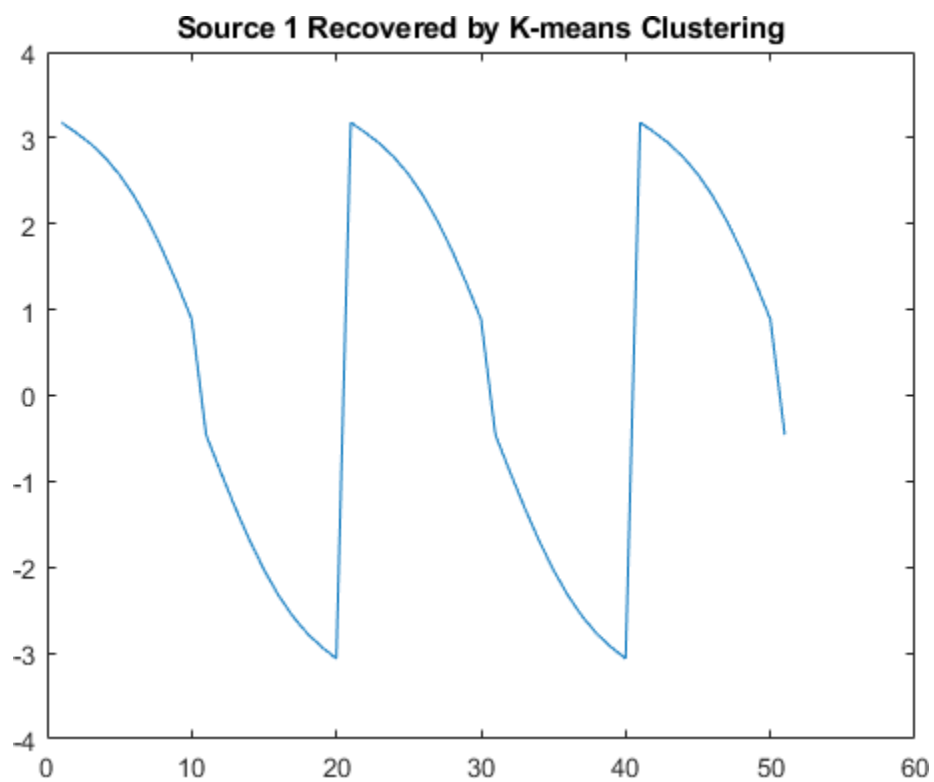
S_12_mean = S2_mean(2,:);
figure, plot(S_12_mean),title('Source 2 Recovered by K-means
Clustering');

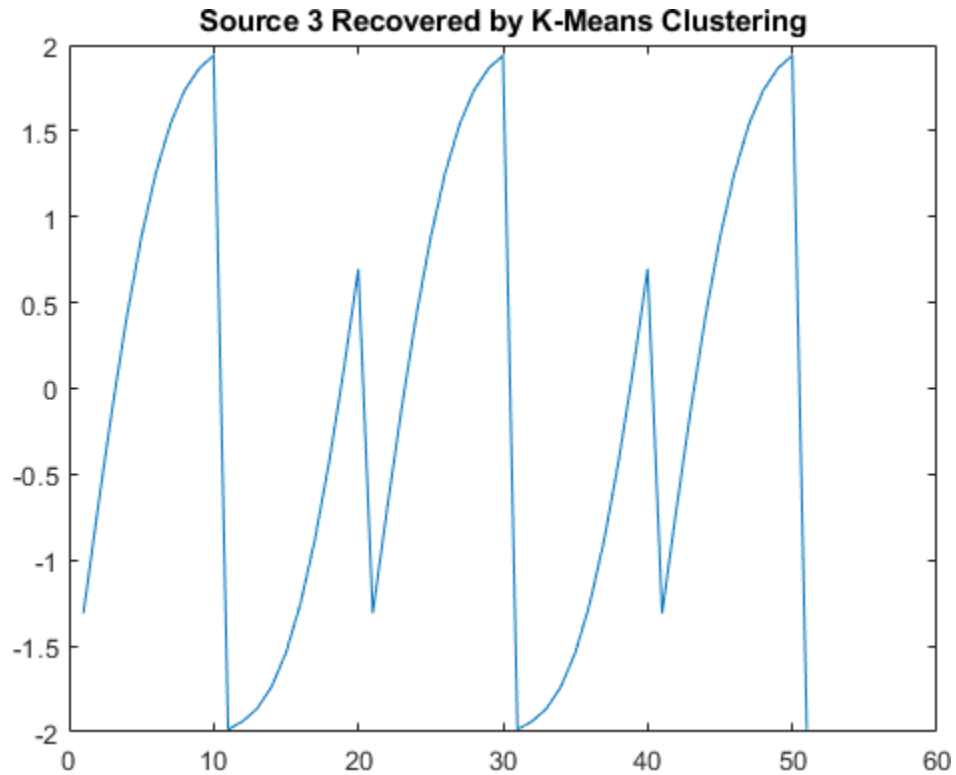
S_13_mean = S2_mean(3,:);
figure, plot(S_13_mean),title('Source 3 Recovered by K-Means
Clustering');

```

1.5631







## K-medoids Clustering

```
% Taking transpose of mixture x1
x1 = x1_bar';
% Taking transpose of mixture x2
x2 = x2_bar';

% All classification of mixture x1 are represented by the vector
idx_medoid
[idx_medoid, C_medoid] = kmedoids(x1,3);
% All classification of mixture x2 are represented by the vector
idx2_medoid
[idx2_medoid, C2_medoid] = kmedoids(x2,3);

% Plotting cluster of mixture x1
figure;
gscatter(x1(:,1),idx_medoid),title('Clusters of mixture 1');
% Plotting cluster of mixture x2
figure;
gscatter(x2(:,1),idx2_medoid),title('Clusters of mixture 2');

% Initializing frequencies of clusters in mixture x1
p1_medoid = 0;
p2_medoid = 0;
```

```

p3_medoid = 0;

for i=1:51
    if idx_medoid(i,1)==1
        p1_medoid = p1_medoid+1; % Calculating frequency of cluster 1
        in mixture x1
    elseif idx_medoid(i,1)==2
        p2_medoid = p2_medoid+1; % Calculating frequency of cluster 2
        in mixture x1
    else
        p3_medoid = p3_medoid+1; % Calculating frequency of cluster 3
        in mixture x1
    end
end

% Calculating posterior probabilities using the frequency of each
cluster
% in the mixture x1
posterior11_medoid = p1_medoid/51;
posterior21_medoid = p2_medoid/51;
posterior31_medoid = p3_medoid/51;

% Initializing frequencies of clusters in mixture x2
p11_medoid = 0;
p22_medoid = 0;
p33_medoid = 0;

for i=1:51
    if idx2_medoid(i,1)==1
        p11_medoid = p11_medoid+1; % Calculating frequency of cluster
        1 in mixture x2
    elseif idx2_medoid(i,1)==2
        p22_medoid = p22_medoid+1; % Calculating frequency of cluster
        2 in mixture x2
    else
        p33_medoid = p33_medoid+1; % Calculating frequency of cluster
        3 in mixture x2
    end
end

% Calculating posterior probabilities using the frequency of each
cluster
% in the mixture x2
posterior12_medoid = p11_medoid/51;
posterior22_medoid = p22_medoid/51;
posterior32_medoid = p33_medoid/51;

% Finding mixing matrix A from obtained posterior values after
clustering
A1 = [posterior11_medoid, posterior21_medoid, posterior31_medoid ;
      posterior12_medoid, posterior22_medoid, posterior32_medoid];

% Scaling matrix L
L = [0.5, 0, 0 ; 0, 0.5, 0 ; 0, 0, 1];

```

```

% Permutation matrix
P = eye(3);

% Approximation matrix of A1
B_medoid = A1*P*L;
E_medoid = B_medoid-A;
error_medoid = norm(E_medoid);
disp(error_medoid);

% Pseudoinverse of B has been used to approximate the source
S2_medoid = pinv(B_medoid)*X;

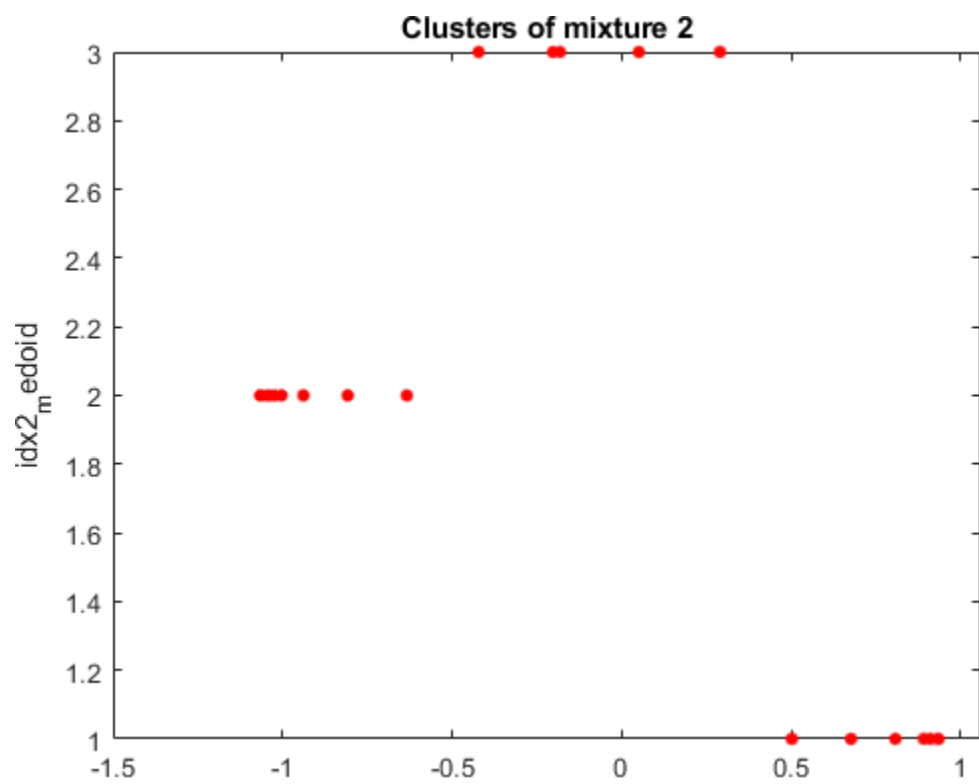
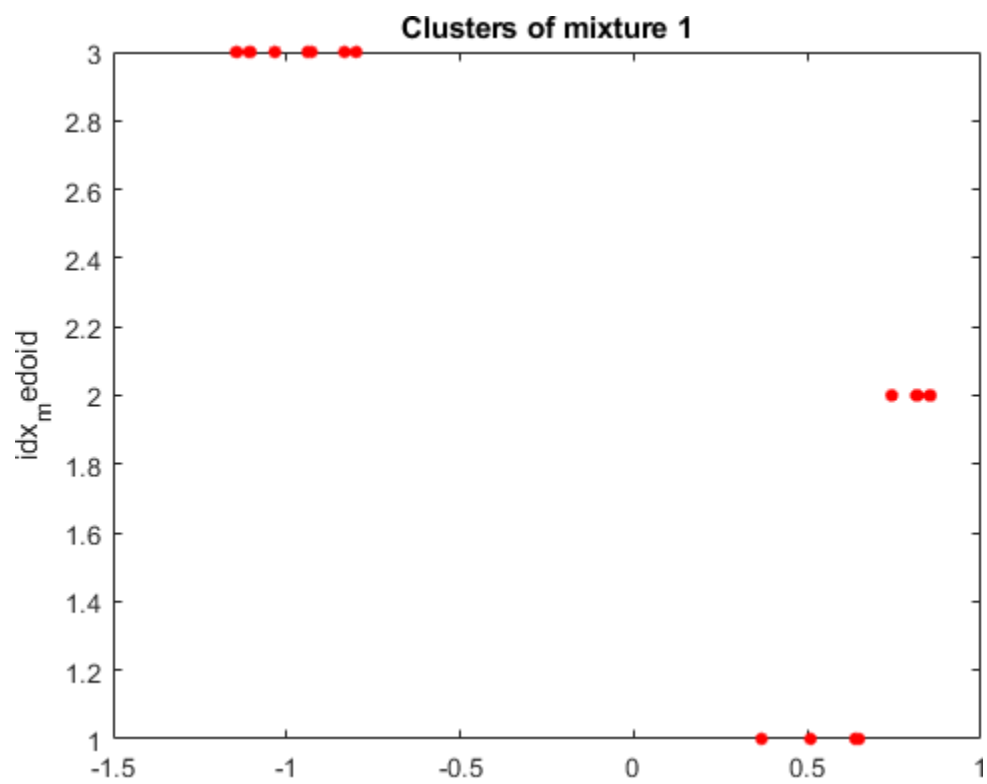
% Plotting the obtained source signals
S_11_medoid = S2_medoid(1,:);
figure, plot(S_11_medoid),title('Source 1 Recovered by K-medoids
Clustering');

S_12_medoid = S2_medoid(2,:);
figure, plot(S_12_medoid),title('Source 2 Recovered by K-medoids
Clustering');

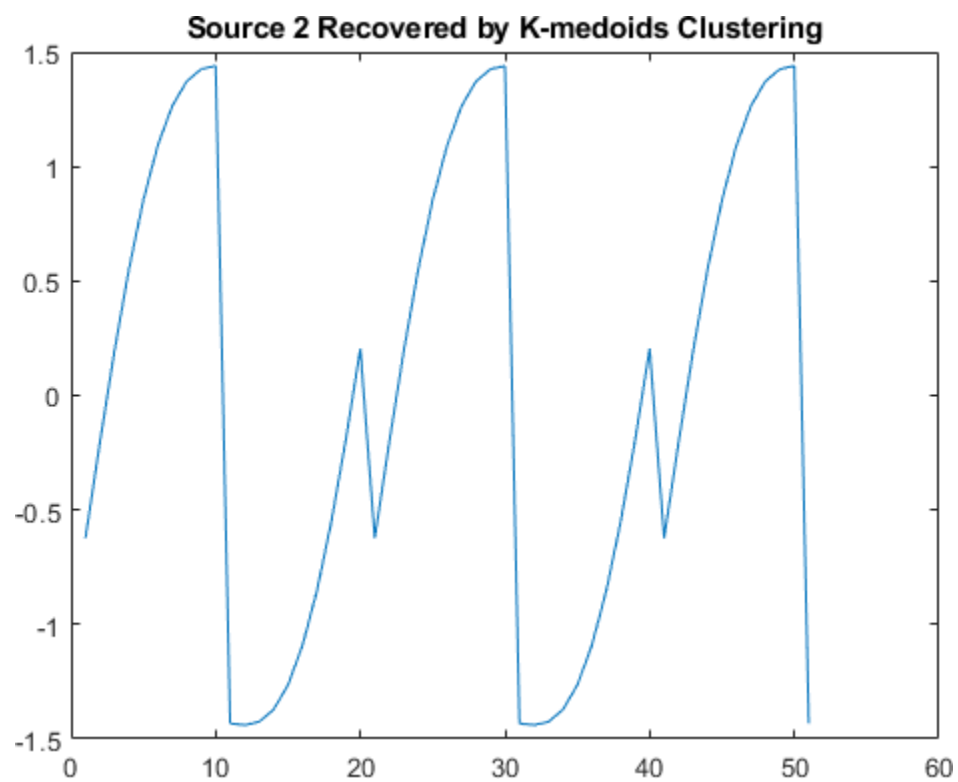
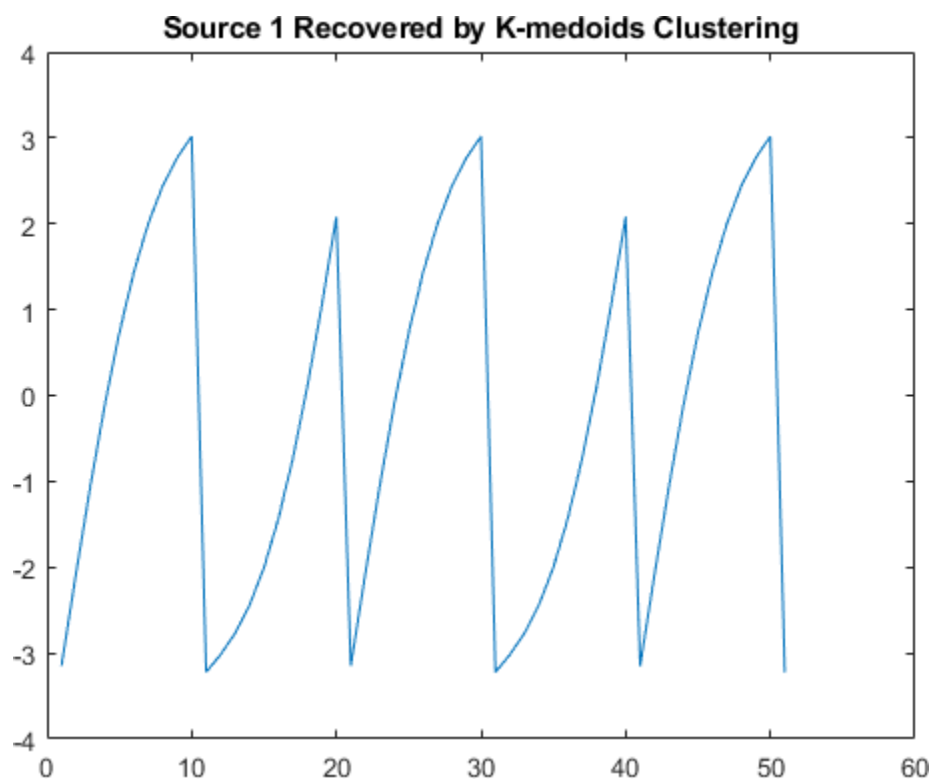
S_13_medoid = S2_medoid(3,:);
figure, plot(S_13_medoid),title('Source 3 Recovered by K-medoids
Clustering');

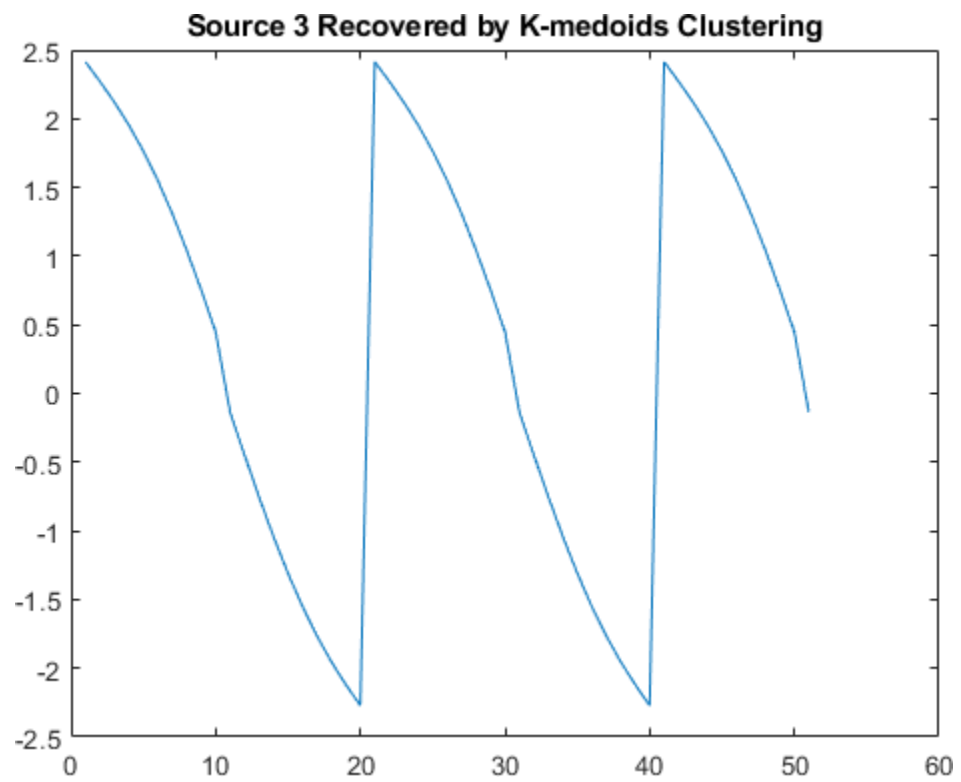
```

1.5496









*Published with MATLAB® R2018a*

# Executing the code 1000 times to determine the winning algorithm

```
error_a = []; % empty matrix to store error in In-Paper algorithm (in
1000 iterations)
error_mean_a = []; % empty matrix to store error in inbuilt K means
algorithm (in 1000 iterations)
error_medoid_a = []; % empty matrix to store error in inbuilt K medoid
algorithm (in 1000 iterations)
for i = 1:1000 % loop for 1000 iterations

% Defining the time period and frequency for the signals.
    tp = 0:0.1:5;
    freq = 0.5;

% Genrating 3 signals. Three types of waveforms have been used -
% Sine, Sawtooth and Square
    signal1 = sin(2*pi*freq*tp);
    signal2 = sawtooth(2*pi*freq*tp);
    signal3 = square(2*pi*freq*tp);

% Generating two mixtures of signals by multiplying each signal with a
% random number and adding them up.
    x1 = rand(1)*signal1 + rand(1)*signal2 + rand(1)*signal3;
    x1 = x1/max(x1);
    x2 = rand(1)*signal1 + rand(1)*signal2 + rand(1)*signal3;
    x2 = x2/max(x2);
    x1_bar = x1 - mean(x1);
    x2_bar = x2 - mean(x2);

% Combining the mixtures into a matrix
    X = [x1 ; x2];

% Combining the sources into a matrix
    S = [signal1 ; signal2 ; signal3];
% Obtaining Signals back from given Mixtures

% A has been initialised with the values suggested in the paper
% Columns of A i.e ai = (cos(alphai), sin(alphai)) with alpha between
% 0 and pi.
    alpha1 = pi/4;
    alpha2 = pi/2;
    alpha3 = 3*pi/4;
    A = [cos(alpha1), cos(alpha2), cos(alpha3); -cos(alpha1), -
cos(alpha2), sin(alpha3)];

% Initializing Weights(Neurons) as suggested in the paper

    w1 = [cos(alpha1)];
    w_1 = [-cos(alpha1)];
    w2 = [cos(alpha2)];
```

```

w_2 = [-cos(alpha2)];
w3 = [cos(alpha3)];
w_3 = [sin(alpha3)];

% Learning rate
n = 0.5;

% There are a total of 6 weights in the mixing matrix and each weight
% has been updated 50 times to obtain suitable values of weights for
further
% calculations.
% Pie function as mentioned in the paper has been used.

for i= 2:51 % Updation of weight 1 for x1
    y = pie(x1_bar(1,1:i-1));
    a = w1 + n * pie(-1*y-w1);
    w1 = [1/3 pie(a)];
end
w1_f = w1(1,51);

for i= 2:51 % Updation of weight 1 for x1
    y = pie(x1_bar(1,1:i-1));
    a = w2 + n * pie(y-w2);
    w2 = [2/3 pie(a)];
end
w2_f = w2(1,51);

for i= 2:51 % Updation of weight 3 for x1
    y = pie(x1_bar(1,1:i-1));
    a = w3 + n * pie(-1*y-w3);
    e1 = i-1;
    if(isnan(a))
        break;
    end
    w3 = [1 pie(a)];
end

if(e1 == 50)
    w3_f = w3(1,51);
else
    w3_f = w3(1,e1);
end

for i= 2:51 % Updation of weight 1 for x2
    y = pie(x2_bar(1,1:i-1));
    a = w_1 + n * pie(y-w_1);
    w_1 = [-1/3 pie(a)];
end
w_1_f = w_1(1,51);

for i= 2:51 % Updation of weight 2 for x2
    y = pie(x2_bar(1,1:i-1));
    a = w_2 + n * pie(y-w_2);
    w_2 = [-2/3 pie(a)];
end

```

```

w_2_f = w_2(1,51);

for i= 2:51 % Updation of weight 3 for x2
    y = pie(x2_bar(1,1:i-1));
    a = w_3 + n * pie(-1*y-w_3);
    e2 = i-1;
    if(isnan(a))
        break;
    end
    w_3 = [-1 pie(a)];
end
if(e2 == 50)
w_3_f = w_3(1,51);
else
w_3_f = w_3(1,e2);
end

%Final mixing matrix has been obtained after getting updated weights
A_obtained = [w1_f, w2_f, w3_f ; w_1_f, w_2_f, w_3_f];

%Scaling matrix L has been initialised
L = [0.5, 0, 0 ; 0, 0.5, 0 ; 0, 0, 1];

%Permuation matrix
P = eye(3);

%Approximation matrix of A
B = A_obtained*P*L;
E = B-A;
error = norm(E);
error_a = [error_a, error];
%disp(error);

%Psuedo inverse of B has been used to find the source
S_pred = pinv(B)*X;

% K means Clustering

% Taking transpose of mixture x1
x1 = x1_bar';
% Taking transpose of mixture x2
x2 = x2_bar';

% All classification of mixture x1 are represented my the vector
idx_mean
[idx_mean, C_mean] = kmeans(x1,3);
% All classification of mixture x2 are represented my the vector
idx2_mean
[idx2_mean, C2_mean] = kmeans(x2,3);

% Initializing frequencies of clusters in mixture x1
p1_mean = 0;
p2_mean = 0;
p3_mean = 0;

```

```

        for i=1:51
            if idx_mean(i,1)==1
                p1_mean = p1_mean+1; % Calculating frequency of cluster 1
in mixture x1
            elseif idx_mean(i,1)==2
                p2_mean = p2_mean+1; % Calculating frequency of cluster 2
in mixture x1
            else
                p3_mean = p3_mean+1; % Calculating frequency of cluster 3
in mixture x1
            end
        end
    end

% Calculating posterior probabilities using the frequency of each
cluster
% in the mixture x1
    posterior11_mean = p1_mean/51;
    posterior21_mean = p2_mean/51;
    posterior31_mean = p3_mean/51;

% Initializing frequencies of clusters in mixture x2
    p11_mean = 0;
    p22_mean = 0;
    p33_mean = 0;

    for i=1:51
        if idx2_mean(i,1)==1
            p11_mean = p11_mean+1; % Calculating frequency of cluster
1 in mixture x2
        elseif idx2_mean(i,1)==2
            p22_mean = p22_mean+1; % Calculating frequency of cluster
2 in mixture x2
        else
            p33_mean = p33_mean+1; % Calculating frequency of cluster
3 in mixture x2
        end
    end

% Calculating posterior probabilities using the frequency of each
cluster
% in the mixture x2
    posterior12_mean = p11_mean/51;
    posterior22_mean = p22_mean/51;
    posterior32_mean = p33_mean/51;

% Finding mixing matrix A from obtained posterior values after
clustering
    A1 = [posterior11_mean, posterior21_mean, posterior31_mean ;
posterior12_mean, posterior22_mean, posterior32_mean];

% Scaling matrix L
    L = [0.5, 0, 0 ; 0, 0.5, 0 ; 0, 0, 1];

```

```

% Permuation matrix
P = eye(3);

% Approximation matrix of A1
B_mean = A1*P*L;
E_mean = B_mean-A;
error_mean = norm(E_mean);
error_mean_a = [error_mean_a , error_mean];
%disp(error_mean);

% Pseudoinverse of B has been used to approximate the source
S2_mean = pinv(B_mean)*X;

% K-medoids Clustering

% Taking transpose of mixture x1
x1 = x1_bar';
% Taking transpose of mixture x2
x2 = x2_bar';

% All classification of mixture x1 are represented my the vector
idx_medoid
[idx_medoid, C_medoid] = kmedoids(x1,3);
% All classification of mixture x2 are represented my the vector
idx2_medoid
[idx2_medoid, C2_medoid] = kmedoids(x2,3);

% Initializing frequencies of clusters in mixture x1
p1_medoid = 0;
p2_medoid = 0;
p3_medoid = 0;

for i=1:51
    if idx_medoid(i,1)==1
        p1_medoid = p1_medoid+1; % Calculating frequency of
cluster 1 in mixture x1
    elseif idx_medoid(i,1)==2
        p2_medoid = p2_medoid+1; % Calculating frequency of
cluster 2 in mixture x1
    else
        p3_medoid = p3_medoid+1; % Calculating frequency of
cluster 3 in mixture x1
    end
end

% Calculating posterior probabilities using the frequency of each
cluster
% in the mixture x1
posterior11_medoid = p1_medoid/51;
posterior21_medoid = p2_medoid/51;
posterior31_medoid = p3_medoid/51;

% Initializing frequencies of clusters in mixture x2
p11_medoid = 0;

```

```

p22_medoid = 0;
p33_medoid = 0;

for i=1:51
    if idx2_medoid(i,1)==1
        p11_medoid = p11_medoid+1; % Calculating frequency of
cluster 1 in mixture x2
    elseif idx2_medoid(i,1)==2
        p22_medoid = p22_medoid+1; % Calculating frequency of
cluster 2 in mixture x2
    else
        p33_medoid = p33_medoid+1; % Calculating frequency of
cluster 3 in mixture x2
    end
end

% Calculating posterior probabilities using the frequency of each
cluster
% in the mixture x2
posterior12_medoid = p11_medoid/51;
posterior22_medoid = p22_medoid/51;
posterior32_medoid = p33_medoid/51;

% Finding mixing matrix A from obtained posterior values after
clustering
A1 = [posterior11_medoid, posterior21_medoid, posterior31_medoid ;
posterior12_medoid, posterior22_medoid, posterior32_medoid];

% Scaling matrix L
L = [0.5, 0, 0 ; 0, 0.5, 0 ; 0, 0, 1];

% Permutation matrix
P = eye(3);

% Approximation matrix of A1
B_medoid = A1*P*L;
E_medoid = B_medoid-A;
error_medoid = norm(E_medoid);
error_medoid_a = [error_medoid_a, error_medoid];
%disp(error_medoid);

% Pseudoinverse of B has been used to approximate the source
S2_medoid = pinv(B_medoid)*X;

end

algo_count = 0; % initializing the count to track how many times the
In-Paper Algo wins
mean_count = 0; % initializing the count to track how many times k
means wins
medoid_count = 0; % initializing the count to track how many times K
medoids wins
for i=1:1000 % logic to find the least error obtained in one
particular iteration and doing the same for 1000 iterations

```



```

        if(error_a(1,i) <= error_mean_a(1,i) && error_a(1,i) <=
error_medoid_a(1,i))
            algo_count = algo_count+1;
        elseif(error_mean_a(1,i) <= error_a(1,i) && error_mean_a(1,i) <=
error_medoid_a(1,i))
            mean_count = mean_count+1;
        elseif(error_medoid_a(1,i) <= error_a(1,i) && error_medoid_a(1,i)
<= error_mean_a(1,i))
            medoid_count = medoid_count+1;
        end
    end
end

% Calculating the Probability of how many times each algorithm wins
p_algo = (algo_count)/1000;
p_mean = (mean_count)/1000;
p_medoid = (medoid_count)/1000;

% Printing the obtained probabilities
fprintf('Probability with which the In-Paper algorithm gives the least
error : %0.3f\n\n', p_algo);
fprintf('Probability with which K-means algorithm gives the least
error : %0.3f\n\n', p_mean);
fprintf('Probability with which K-medoid algorithm gives the least
error : %0.3f\n\n', p_medoid);

Probability with which the In-Paper algorithm gives the least error :
0.441

Probability with which K-means algorithm gives the least error : 0.267

Probability with which K-medoid algorithm gives the least error :
0.292

```

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