

(3 Hours)

[Total Marks : 100]

- N.B. :** (1) Question No. 1 is **compulsory**.
 (2) Attempt any **four** questions from remaining **six** questions.
 (3) Draw **suitable** diagrams wherever **necessary**.
 (4) Assume **suitable** data, if **necessary**.

Q1. (a) Explain different types of machines and state at least one application of each (10)

(b) Let G be the grammar. Find the leftmost derivation, rightmost derivation and parse (10)

tree for the string 00110101

$G: S \rightarrow 0B \mid 1A$

$A \rightarrow 0 \mid 0S \mid 1AA$

$B \rightarrow 1 \mid 1S \mid 0BB$

Q2. (a) Design a DFA to accept (10)

- (i) a set of all strings with odd number of ones followed by even number of zeros
 (ii) a set of all strings with which begin and end with different letters $\Sigma = \{x, y, z\}$

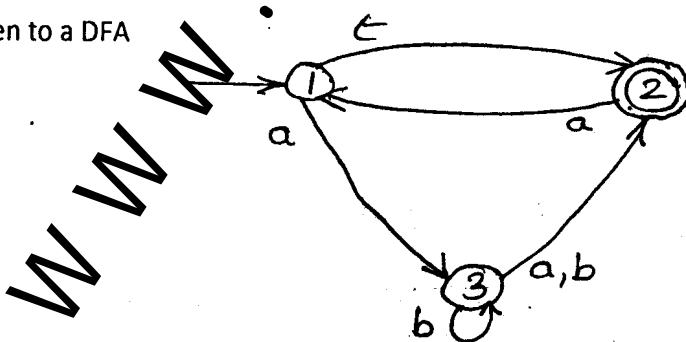
(b) What is a regular expression? Give formal definition of a regular expression. Design a (10)

DFA corresponding to the regular expression $(a+b)^* aba(a+b)^*$

Q3. (a) Design a Moore and Mealy machine to convert each occurrence of a substring abb by aba (10)

(b) Convert the following NFA with epsilon moves to an NFA without epsilon moves and (10)

then to a DFA



Q4. (a) Using pumping lemma prove that the following languages are not regular (10)

(i) $L_1 = \{ ww \mid w \in \{0, 1\}^* \}$

(ii) $L_2 = \{ 0^i 1^i \mid i \geq 1 \}$

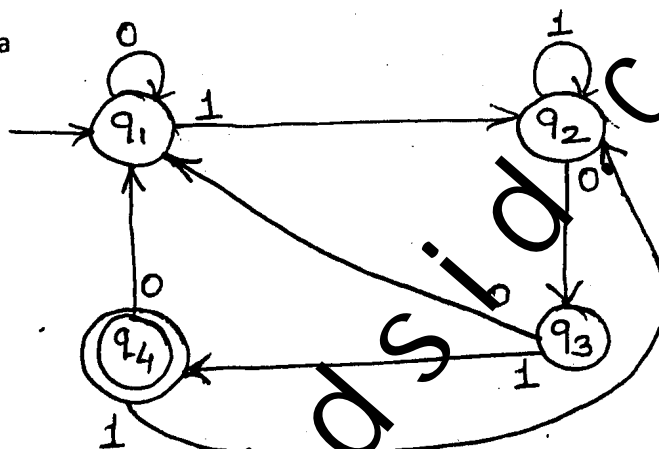
(b) Design a Turing machine to generate the language given by a regular expression (10)

$0(0+1)^*11$

[TURN OVER]

Q5. (a) List and explain decision properties of regular languages. Explain the test for checking emptiness of a regular language (10)

(b) State Arden's theorem and use it to construct a regular expression corresponding to the following automata (10)



Q6 (a) (i) Convert the following CFG to CNF (05)

$$S \rightarrow bA \mid aB$$

$$A \rightarrow bAA \mid aS \mid a$$

$$B \rightarrow aBB \mid bS \mid b$$

(ii) Construct a PDA accepting the following language $L = \{a^n b^m a^n \mid m, n \geq 1\}$ (05)

(b) Explain the rules for simplification of a context free grammar (10)

Q7. Write short notes on (any three) (20)

(a) Variants of a Turing Machine

(b) Post Correspondence Problem

(c) Chomsky Hierarchy

(d) Intractable Problems

(e) Recursive and recursively enumerable languages