## Unit Vector Perpendicular

## 1 $12^{th}$ Maths - Chapter 10

This is Problem-4 from Exercise 10.4

1. Show that 
$$(\overrightarrow{a} - \overrightarrow{b})X(\overrightarrow{a} + \overrightarrow{b}) = 2(\overrightarrow{a}X\overrightarrow{b})$$

## 2 Solution

Let us assume that

$$\mathbf{a} = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}, \mathbf{b} = \begin{pmatrix} 3 \\ 2 \\ 1 \end{pmatrix} \tag{1}$$

$$\mathbf{a} + \mathbf{b} = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} + \begin{pmatrix} 3 \\ 2 \\ 1 \end{pmatrix} = \begin{pmatrix} 4 \\ 4 \\ 4 \end{pmatrix} \tag{2}$$

$$\mathbf{a} - \mathbf{b} = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} - \begin{pmatrix} 3 \\ 2 \\ 1 \end{pmatrix} = \begin{pmatrix} -2 \\ 0 \\ 2 \end{pmatrix} \tag{3}$$

by using vector product

$$\mathbf{aXb} = \begin{pmatrix} -4\\8\\-4 \end{pmatrix} \tag{4}$$

$$2(\mathbf{aXb}) = \begin{pmatrix} -8\\16\\-8 \end{pmatrix} \tag{5}$$

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$$(5)$$

$$(\mathbf{a} - \mathbf{b})X(\mathbf{a} + \mathbf{b}) = \begin{pmatrix} -8\\16\\-8 \end{pmatrix}$$

$$(6)$$

we can clearly see that (5) is equal to (6)  $(\overrightarrow{a} - \overrightarrow{b})X(\overrightarrow{a} + \overrightarrow{b}) = 2(\overrightarrow{a}X\overrightarrow{b})$