

Q.1) From your analysis of the categorical variables from the dataset, what could you infer about their effect on the dependent variable? (3 marks)

When analyzing the effect of **categorical variables** on the **dependent variable**, we consider the following points:

1. Encoding Categorical Variables:

- Categorical features (e.g., gender, product type, region) need to be encoded into numerical values for machine learning algorithms.
- Common encoding methods include one-hot encoding, label encoding, or using dummy variables.

2. Inference from Coefficients:

- In linear models (e.g., linear regression), the coefficients associated with categorical variables provide insights.
- A positive coefficient indicates that an increase in that category positively affects the dependent variable.
- A negative coefficient suggests the opposite.

3. Interaction Effects:

- Consider interactions between categorical variables and other features.
- For example, the effect of a product type might vary based on the region.

Q.2) Why is it important to use `drop_first=True` during dummy variable creation

The **`drop_first=True`** parameter is essential during **dummy variable creation** (using methods like `pd.get_dummies()` in pandas) for the following reasons:

1. Multicollinearity Reduction:

- When creating dummy variables, we convert categorical features into binary columns (0 or 1) to represent different categories.
- By setting `drop_first=True`, we exclude one category (usually the first) from the dummy variables.
- This helps reduce multicollinearity (correlation) among the dummy features.
- Without dropping the first category, the model might encounter linear dependencies between the dummy variables, violating assumptions for linear regression.
- **`drop_first=True`** ensures better model behavior by reducing dimensionality and handling multicollinearity.

Q.3) Looking at the pair-plot among the numerical variables, which one has the highest correlation with the target variable?

- In the pair-plot among the numerical variables, the feature with the **highest correlation** to the **target variable** is typically the one that exhibits the strongest linear relationship.
- To determine this, you can calculate the correlation coefficients between each numerical feature and the target variable.
- The feature with the highest absolute correlation value (closest to 1) is the most influential.
- If you have access to the correlation matrix or the actual data, you can compute the correlations directly.
- Otherwise, you can use statistical tools or libraries (such as pandas in Python) to find the most correlated feature.

Q.4) How did you validate the assumptions of Linear Regression after building the model on the training set?

After building a **linear regression model** on the training set, it's crucial to validate the assumptions to ensure the reliability of the results. Here are the key steps for validating these assumptions:

1. Linear Relationship:

- Assumption: There exists a linear relationship between the independent variable (x) and the dependent variable (y).
- Validation:
 - Create a scatter plot of (x) vs. (y).
 - Visually inspect whether the points roughly fall along a straight line.
 - If linear, this assumption is met; otherwise, consider nonlinear transformations or additional variables.

2. Independence of Residuals:

- Assumption: Residuals (errors) are independent.
- Validation:
 - Examine a residual time series plot (residuals vs. time).
 - Ideally, most residual autocorrelations should fall within the 95% confidence bands around zero.
 - Lack of patterns among consecutive residuals indicates independence.

3. Homoscedasticity (Constant Variance):

- Assumption: Residuals have constant variance at every level of (x).
- Validation:
 - Plot residuals vs. predicted values.
 - Look for consistent spread of residuals across the range of predictions.
 - Heteroscedasticity (varying spread) suggests violation of this assumption.

4. Normality of Residuals:

- Assumption: Residuals follow a normal distribution.
- Validation:
 - Create a histogram or Q-Q plot of residuals.
 - Check if they resemble a normal distribution.
 - Consider transformations if residuals deviate significantly from normality.

Remember that addressing violations of these assumptions can improve model accuracy and reliability.

Q.5) Based on the final model, which are the top 3 features contributing significantly towards explaining the demand of the shared bikes?

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General Subjective Questions

Q.1) Explain the linear regression algorithm in detail.

- **Linear Regression-**
 - Linear regression is a supervised machine learning algorithm that models the relationship between a dependent variable (target) and one or more independent features (predictors).
 - It aims to find the best-fitting linear equation that predicts the target variable based on the input features.
- **Types of Linear Regression:**
 - Simple Linear Regression:
 - Involves a single independent feature (e.g., predicting house price based on square footage).
 - Multiple Linear Regression:
 - Utilizes multiple independent features (e.g., predicting house price using area, age, and location).

- **How It Works:**

- Linear regression fits a line (or hyperplane in higher dimensions) to the data using the least squares method.
- The goal is to minimize the sum of squared errors between predicted and actual values.
- The linear equation takes the form:
$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n + \epsilon$$
 - y is the predicted output.
 - (x_1, x_2, \dots, x_n) are input features.
 - $(\beta_0, \beta_1, \dots, \beta_n)$ are coefficients (weights).
 - (ϵ) represents the error term.

- **Why Linear Regression Matters:**

- Interpretability: Linear regression provides clear coefficients, aiding understanding of feature impact.
- Simplicity: It's transparent and foundational for more complex algorithms.

Q.2) Explain the Anscombe's quartet in detail.

Anscombe's quartet is a fascinating concept in machine learning that highlights the importance of data visualization and the limitations of relying solely on summary statistics. Let's dive into the details:

1. Anscombe's Quartet-

- Anscombe's quartet consists of four datasets, each containing eleven (x, y) pairs.
- Surprisingly, these datasets share identical summary statistics in terms of means, variances, correlations, and linear regression lines.
- However, when we plot them, they reveal distinctive patterns and different relationships between x and y .

2. Purpose and Significance:

- Anscombe's quartet serves several purposes:
- Visualizing Data: It emphasizes the importance of exploratory data analysis through visual inspection.
- Challenging Assumptions: Summary statistics alone can be misleading; visual examination is crucial.
- Outliers and Trends: Data visualization helps spot outliers, trends, and nuances not evident from statistics alone.

3. Practical Example:

- Let's explore Anscombe's quartet with a practical implementation:
- Import the necessary libraries (e.g., NumPy, Pandas, Matplotlib).
- Load the quartet dataset (which contains four sets of (x, y) values).
- Calculate descriptive statistics (mean, standard deviation, correlations, etc.) for each dataset.
- Visualize the data using scatter plots to see the unique patterns.

Q.3) What is Pearson's R?. What is scaling?

1. Pearson's R (Correlation Coefficient):

- Pearson's Correlation Coefficient (often denoted as r) measures the strength and direction of a linear relationship between two continuous variables.
 - It ranges from -1 to 1:
 - ($r = 1$): Perfect positive correlation (as one variable increases, the other increases).
 - ($r = -1$): Perfect negative correlation (as one variable increases, the other decreases).
 - ($r = 0$): No linear correlation.
- **Use cases:**
 - Feature Selection: Widely employed in machine learning for selecting important variables.
 - Understanding Relationships: Helps understand how inputs relate to outputs.

2. Scaling in Machine Learning:

- Feature Scaling is crucial during data preprocessing to handle varying magnitudes or units of features.
- Why use feature scaling?
- Ensures all features are on a comparable scale.
- Prevents larger-scale features from dominating the learning process.
- Enhances algorithm performance and stability.
- **Methods:**
 - Min-Max Scaling: Scales features to a range (usually 0 to 1).
 - Standardization (Z-score normalization): Centers features around mean and scales by standard deviation.
 - Absolute Maximum Scaling: Divides each entry by the maximum absolute value in the column.

- **Benefits:**
 - Helps algorithms understand relative relationships better.
 - Prevents numerical instability due to scale disparities.

Q.4) Why is scaling performed? What is the difference between normalized scaling and standardized scaling?

1. Why Is Scaling Performed?

- Scaling is a crucial step in data preprocessing to ensure that all features (variables) have the same scale or magnitude.
- Reasons for scaling:
 - Varying Magnitudes: Features often have different units and ranges, making direct comparisons challenging.
 - Algorithm Sensitivity: Some algorithms (e.g., k-nearest neighbors, gradient descent) are sensitive to feature scales.
 - Convergence and Stability: Scaling aids faster convergence during optimization.

2. Normalized Scaling (Min-Max Scaling):

- Objective: Bring all feature values within the range of 0 to 1.
- Formula:
 - Normalize each feature (x) using:

$$x_{\text{normalized}} = \frac{\max(x) - \min(x)}{\max(x) - \min(x)} x - \min(x)$$
- Pros:
 - Preserves the shape of the distribution.
 - Useful when features have different ranges.
- Cons:
 - Loses some information, especially about outliers.

3. Standardized Scaling (Z-score normalization):

- Objective: Transform data to have a mean of 0 and a standard deviation of 1.
- Formula:
 - Standardize each feature (x) using:

$$x_{\text{standardized}} = \frac{\text{std}(x)}{\text{std}(x)} x - \text{mean}(x)$$
- Pros:
 - Retains information about outliers.
 - Suitable for algorithms relying on Euclidean distance or gradient descent.
- Cons:
 - Does not enforce a specific range (values can be negative or positive).

Normalized scaling compresses data into the $[0, 1]$ range, while standardized scaling centers data around a mean of 0 with a standard deviation of 1.

Q.5 You might have observed that sometimes the value of VIF is infinite. Why does this happen?

The occurrence of **infinite values** in the **Variance Inflation Factor (VIF)** is related to a phenomenon called **perfect multicollinearity**.

1. Variance Inflation Factor (VIF):

- VIF measures the degree of multicollinearity (correlation) between independent variables in a regression model.
- It quantifies how much the variance of a coefficient is inflated due to correlations with other predictors.
- High VIF values indicate strong interdependencies among features.

2. Perfect Multicollinearity:

- Perfect multicollinearity occurs when two or more independent variables are perfectly linearly dependent.
- In other words, one variable can be entirely predicted by a combination of other variables.
- When this happens, the correlation between these variables is perfect (usually $R^2 = 1$).
- The VIF formula involves dividing by $(1 - R^2)$, which leads to an infinite value (since $1 - 1 = 0$).

3. Solution:

- To address perfect multicollinearity, remove one of the correlated variables from the dataset.
- Dropping one of the variables ensures that the model remains stable and interpretable.

VIF helps us identify problematic correlations, but infinite VIF values signal a need for variable removal.