

#1

```
import numpy as np
```

```
from scipy import stats
```

```
def variance_test(data1,data2):
```

```
    var1=np.var(data1,ddof=11)
```

```
    var2=np.var(data2,ddof=1)
```

```
    F=var1/var2
```

```
    df1=len(data)-1
```

```
    df2=len(data)-1
```

```
    p_value=1-stats.f.cdf(f,df1,df2)
```

```
    return F,p_value;
```

```
data1=[22,23,44,55,66]
```

```
data2=[34,45,66,89,90]
```

```
F, p_value = variance_ratio_test(data1, data2)
```

```
print(f"F-value: {F}")
```

```
print(f"P-value: {p_value}")
```

```
import numpy as np
```

```
from scipy import stats
```

```
def variance_ratio_test(data1, data2):
```

```
    # Calculate variances of both datasets
```

```
var1 = np.var(data1, ddof=1) # Sample variance (ddof=1 for unbiased estimator)
```

```
var2 = np.var(data2, ddof=1)
```

```
# Calculate the F-statistic
```

```
F = var1 / var2
```

```
# Degrees of freedom
```

```
df1 = len(data1) - 1 # degrees of freedom for the first sample
```

```
df2 = len(data2) - 1 # degrees of freedom for the second sample
```

```
# Calculate the p-value using the F-distribution CDF
```

```
p_value = 1 - stats.f.cdf(F, df1, df2)
```

```
return F, p_value
```

```
# Example data
```

```
data1 = [10, 12, 13, 15, 16, 18]
```

```
data2 = [20, 22, 24, 25, 30]
```

```
# Get F-value and p-value
```

```
F, p_value = variance_ratio_test(data1, data2)
```

```
print(f"F-value: {F}")
```

```
print(f"P-value: {p_value}")
```

Q2. Given a significance level of 0.05 and the degrees of freedom for the numerator and denominator of an

F-distribution, write a Python function that returns the critical F-value for a two-tailed test.

```
from scipy import stats
```

```
def criticle_f_value(alpha,data1,data2):
```

```
    upper_critical_value=stats.f.ppf(1-alpha,data1,data2)
```

```
    lower_critical_value=1/upper_criticle_value
```

```
    return upper_criticle_value,lower_criticle_value
```

```
    alpha=0.05
```

```
    data1=5
```

```
    data2=10
```

```
    lower_critical, upper_critical = critical_f_value(alpha, data1, data2)
```

```
print(f"Lower critical F-value: {upper_critical}")
```

```
print(f"Upper critical F-value: {lower_critical}")
```

```
import numpy as np
```

```
from scipy import stats
```

```
def f_test_for_variances(sample1, sample2):

    # Calculate variances of both datasets

    var1 = np.var(sample1, ddof=1) # Sample variance (ddof=1 for unbiased estimator)

    var2 = np.var(sample2, ddof=1)


    # Calculate the F-statistic (ratio of variances)

    F = var1 / var2 if var1 > var2 else var2 / var1 # Ensure F > 1


    # Degrees of freedom for each sample

    df1 = len(sample1) - 1 # degrees of freedom for the first sample

    df2 = len(sample2) - 1 # degrees of freedom for the second sample


    # Calculate the p-value using the F-distribution CDF

    p_value = 1 - stats.f.cdf(F, df1, df2)


    return F, df1, df2, p_value


# Generate random samples from two normal distributions with known variances

np.random.seed(42) # For reproducibility


# Parameters for the normal distributions: mean, variance, and sample size

mean1, var1, size1 = 10, 4, 30 # mean=10, variance=4, sample size=30

mean2, var2, size2 = 20, 9, 30 # mean=20, variance=9, sample size=30


# Generate the samples using numpy's normal distribution function
```

```
sample1 = np.random.normal(mean1, np.sqrt(var1), size1)
```

```
sample2 = np.random.normal(mean2, np.sqrt(var2), size2)
```

```
# Perform the F-test for variances
```

```
F, df1, df2, p_value = f_test_for_variances(sample1, sample2)
```

```
# Output the results
```

```
print(f"F-value: {F}")
```

```
print(f"Degrees of freedom for sample 1: {df1}")
```

```
print(f"Degrees of freedom for sample 2: {df2}")
```

```
print(f"P-value: {p_value}")
```

```
#4
```

```
import scipy.stats as stats
```

```
# Given values
```

```
var1 = 10 # Variance of first population
```

```
var2 = 15 # Variance of second population
```

```
n1 = 12 # Sample size for population 1
```

```
n2 = 12 # Sample size for population 2
```

```
alpha = 0.05 # Significance level
```

```
# F-statistic calculation
```

```
F = var1 / var2 if var1 > var2 else var2 / var1 # Ensure F > 1
```

Degrees of freedom

df1 = n1 - 1 # Degrees of freedom for sample 1

df2 = n2 - 1 # Degrees of freedom for sample 2

p-value calculation

p_value = 1 - stats.f.cdf(F, df1, df2)

print(f"F-value: {F}")

print(f"Degrees of freedom for sample 1: {df1}")

print(f"Degrees of freedom for sample 2: {df2}")

print(f"P-value: {p_value}")

#5

Given values

claimed_variance = 0.005 # Claim variance

sample_variance = 0.006 # Sample variance

n = 25 # Sample size

alpha = 0.01 # Significance level

F-statistic calculation

F = sample_variance / claimed_variance

Degrees of freedom

df1 = n - 1 # Degrees of freedom for sample

df2 = n - 1 # Degrees of freedom for the population (same as sample)

p-value calculation

p_value = 1 - stats.f.cdf(F, df1, df2)

print(f"F-value: {F}")

print(f"Degrees of freedom: {df1}")

print(f"P-value: {p_value}")

#6

def f_distribution_mean_variance(df1, df2):

if df1 <= 2:

mean = None

else:

mean = df1 / (df1 - 2)

if df2 <= 4:

variance = None

else:

variance = (2 * df2 * (df1 + df2 - 2)) / (df1 * (df2 - 2)2 * (df2 - 4))**

return mean, variance

Example degrees of freedom

df1 = 5

df2 = 10

```
mean, variance = f_distribution_mean_variance(df1, df2)

print(f"Mean of F-distribution: {mean}")

print(f"Variance of F-distribution: {variance}")


#7

# Given values

var1 = 25 # Sample variance for population 1

var2 = 20 # Sample variance for population 2

n1 = 10 # Sample size for population 1

n2 = 15 # Sample size for population 2

alpha = 0.10 # Significance level


# F-statistic calculation

F = var1 / var2 if var1 > var2 else var2 / var1 # Ensure F > 1


# Degrees of freedom

df1 = n1 - 1 # Degrees of freedom for sample 1

df2 = n2 - 1 # Degrees of freedom for sample 2


# p-value calculation

p_value = 1 - stats.f.cdf(F, df1, df2)


print(f"F-value: {F}")

print(f"Degrees of freedom for sample 1: {df1}")
```



```
print(f"Degrees of freedom for sample 2: {df2}")
```

```
print(f"P-value: {p_value}")
```

```
#8
```

```
# Data for restaurants
```

```
restaurant_a = [24, 25, 28, 23, 22, 20, 27]
```

```
restaurant_b = [31, 33, 35, 30, 32, 36]
```

```
# Calculate variances
```

```
var_a = np.var(restaurant_a, ddof=1)
```

```
var_b = np.var(restaurant_b, ddof=1)
```

```
# Sample sizes
```

```
n1 = len(restaurant_a)
```

```
n2 = len(restaurant_b)
```

```
alpha = 0.05 # Significance level
```

```
# F-statistic calculation
```

```
F = var_a / var_b if var_a > var_b else var_b / var_a
```

```
# Degrees of freedom
```

```
df1 = n1 - 1
```

```
df2 = n2 - 1
```

```
# p-value calculation
```

```
p_value = 1 - stats.f.cdf(F, df1, df2)
```

```
print(f"F-value: {F}")
```

```
print(f"Degrees of freedom for sample 1: {df1}")
```

```
print(f"Degrees of freedom for sample 2: {df2}")
```

```
print(f"P-value: {p_value}")
```

```
#9
```

```
# Data for groups
```

```
group_a = [80, 85, 90, 92, 87, 83]
```

```
group_b = [75, 78, 82, 79, 81, 84]
```

```
# Calculate variances
```

```
var_a = np.var(group_a, ddof=1)
```

```
var_b = np.var(group_b, ddof=1)
```

```
# Sample sizes
```

```
n1 = len(group_a)
```

```
n2 = len(group_b)
```

```
alpha = 0.01 # Significance level
```

```
# F-statistic calculation
```

```
F = var_a / var_b if var_a > var_b else var_b / var_a
```

```
# Degrees of freedom
```

```
df1 = n1 - 1
```

```
df2 = n2 - 1
```

```
# p-value calculation
```

```
p_value = 1 - stats.f.cdf(F, df1, df2)
```

```
print(f"F-value: {F}")
```

```
print(f"Degrees of freedom for sample 1: {df1}")
```

```
print(f"Degrees of freedom for sample 2: {df2}")
```

```
print(f"P-value: {p_value}")
```

```
#10
```