Advanced Algorithm Mini Project Report

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Project Title: Sudoku Solver

3		6	5		8	4		
5	2							
	8	7					3	1
		3		1			8	
9			8	6	3			5
	5			9		6		
1	3					2	5	
							7	4
		5	2		6	3		

Given a partially filled grid of size 9×9, goal is to assign numbers from 1 to 9 to the empty cells such that every row, every column and every sub grid of size 3×3 contains exactly one instance of numbers from 1 to 9

This game has become popular now in large number of countries and many developers have tried to generate more complicated and interesting puzzles

Solving Sudoku helps to improve concentration, reduce anxiety and stress, promotes a healthy competition and improves problem-solving skills

There are 3 methods of implementing Sudoku solver –

1. Brute Force

This approach is used to generate all possible configurations of numbers from 1 to 9 to fill the empty cells. Try every configuration one by one until the correct configuration is found. After filling all the unassigned positions check if the matrix is safe or not. If safe print else recurs for other cases

bruteforce.c

```
int solveSudoku(int N,int grid[N][N],int row,int col)
    if(row == N - 1 && col == N)
    if(col == N)
        row++;
        col = 0;
    if(grid[row][col] > 0)
        return solveSudoku(N,grid,row,col + 1);
    for(int num = 1;num <= N;num++)</pre>
        if(isSafe(N,grid,row,col,num))
            grid[row][col] = num;
            if(solveSudoku(N,grid,row,col + 1))
                return 1;
        grid[row][col] = 0;
    return 0;
void printGrid(int N,int arr[N][N])
    for(int i = 0; i < N; i++)
        for(int j = 0; j < N; j++)
            printf("%d\t",arr[i][j]);
        printf("\n");
```

```
int main()
   int N = 9;
   int grid[9][9] = \{\{3, 0, 6, 5, 0, 8, 4, 0, 0\},
                      { 5, 2, 0, 0, 0, 0, 0, 0, 0 },
                      \{0, 8, 7, 0, 0, 0, 0, 3, 1\},\
                      { 0, 0, 3, 0, 1, 0, 0, 8, 0 },
                      \{9, 0, 0, 8, 6, 3, 0, 0, 5\},\
                      { 0, 5, 0, 0, 9, 0, 6, 0, 0 },
                      \{1, 3, 0, 0, 0, 0, 2, 5, 0\},\
                      { 0, 0, 0, 0, 0, 0, 0, 7, 4 },
                      { 0, 0, 5, 2, 0, 6, 3, 0, 0 }};
   if(solveSudoku(N,grid,0,0))
       printGrid(N,grid);
   else
       printf("No solution exists");
   return 0;
```

2. Backtracking

Before assigning a number check whether it is safe to assign. After checking for safety assign that number and recursively check whether this assignment leads to a solution or not. If the assignment does not lead to a solution, try next number for the current empty cell. And if none of the numbers from 1 to 9 leads to a solution, then print no solution exists

backtracking.c

```
#include <stdio.h>
int findUnassignedLocation(int N,int grid[N][N],int *row,int *col)
    int j;
    for(i = 0; i < N; i++)
        for(j = 0; j < N; j++)
            if(grid[i][j] == 0)
                 *row = i;
                *col = j;
                return 1;
    *row = i;
    *col = j;
    return 0;
int usedInRow(int N,int grid[N][N],int row,int num)
    for(int col = 0;col < N;col++)</pre>
        if (grid[row][col] == num)
            return 1;
    return 0;
```

```
int solveSudoku(int N,int grid[N][N])
    int row;
    int col;
    if (!findUnassignedLocation(N,grid,&row,&col))
    for(int num = 1;num <= N;num++)</pre>
        if(isSafe(N,grid,row,col,num))
            grid[row][col] = num;
            if(solveSudoku(N,grid))
                 return 1;
            grid[row][col] = 0;
    return 0;
void printGrid(int N,int grid[N][N])
    for(int row = 0;row < N;row++)</pre>
        for(int col = 0;col < N;col++)</pre>
            printf("%d\t",grid[row][col]);
        printf("\n");
```

3. Bit Masks

This method is a slight optimization to the above 2 methods. For each row or column or box create a bitmask and for each element in the grid set the bit at position 'value' to 1 in the corresponding bitmasks

bitmasks.c

```
int solveSudoku(int grid[N][N],int i,int j,int *seted)
    if(!*seted)
        *seted = 1;
        setInitialValues(grid);
    if(i == N-1 \&\& j == N)
    if(j == N)
        j = 0;
        i++;
    if(grid[i][j])
        return solveSudoku(grid,i,j + 1,seted);
    for(int nr = 1;nr <= N;nr++)</pre>
        if(isSafe(i,j,nr))
            grid[i][j] = nr;
            row[i] |= 1 << nr;
            col[j] |= 1 << nr;
            box[getBox(i, j)] |= 1 << nr;</pre>
            if(solveSudoku(grid,i,j + 1,seted))
                return 1;
            row[i] &= ~(1 << nr);
            col[j] &= ~(1 << nr);
            box[getBox(i, j)] &= \sim(1 << nr);
        grid[i][j] = 0;
    return 0;
```

Brute Force Technique of Solving Sudoku

- create a function that checks if the given matrix is a valid sudoku or not. Keep hashmap for the row, column and boxes. If any number has frequency greater than 1 in the hashmap return false else return true
- create a recursive function that takes grid, current row and column index
- check for some base cases
 - if index is at i = N 1 and j = N, then check if the grid is safe or not. If safe print grid and return true else return false
 - if j = N, then do i++ and j = 0
- if the current index is not assigned then fill elements from 1 to 9 and recur for all 9 cases with index of next element. If the recursive call returns true then break the loop and return true
- if the current index is assigned then call the recursive function with the index of the next element
- since for every unassigned index there are 9 possible options, so time complexity is $O(9^{\wedge}(N^{\wedge}2))$
- since for storing the output array a matrix is needed, so space complexity is $O(N^2)$

C:\U	sers\dell	\Desktop	\advance	d algori	ithms>gco	brutefo	orce.c		
C:\U	sers\dell	\Desktop	\advance	d algori	ithms>a				
3	1	6	5	7	8	4	9	2	
5	2	9	1	3	4	7	6	8	
4	8	7	6	2	9	5	3	1	
2	6	3	4	1	5	9	8	7	
9	7	4	8	6	3	1	2	5	
8	5	1	7	9	2	6	4	3	
1	3	8	9	4	7	2	5	6	
6	9	2	3	5	1	8	7	4	
7	4	5	2	8	6	3	1	9	

Backtracking Technique of Solving Sudoku

- create a function that checks after assigning the current index if grid becomes unsafe or not. Keep hashmap for row, column and boxes. If any number has frequency greater than 1 in the hashmap return false else return true. hashmap can be avoided by using loops
- create a recursive function that takes a grid
- check for any unassigned location
 - if present then assign a number from 1 to 9
 - check if assigning the number to current index makes the grid unsafe or not
 - if safe then recursively call the function for all safe cases from 0 to 9
 - if any recursive call returns true end the loop and return true. If no recursive call returns true then return false
- if there is no unassigned location then return true
- since for every unassigned index there are 9 possible options, so time complexity is $O(9^{(N^2)})$. The time complexity remains same but there will be some early pruning so time taken will be much less than the brute approach, but upper bound time complexity remains same
- since for storing the output array a matrix is needed, so space complexity is $O(N^2)$

c \	\		V 1						
C:\Us	ers\dell	L\Desktop	\advance	ed algori	Lthms>gc	c backtra	acking.c		
c \	\								
C:\Us	sers (dell	L\Desktop	\advance	ed algori	L⊤nms>a				
3	1	6	5	7	8	4	9	2	
5	2	9	1	3	4	7	6	8	
4	8	7	6	2	9	5	3	1	
2	6	3	4	1	5	9	8	7	
9	7	4	8	6	3	1	2	5	
8	5	1	7	9	2	6	4	3	
1	3	8	9	4	7	2	5	6	
6	9	2	3	5	1	8	7	4	
7	4	5	2	8	6	3	1	9	

Bit Masks Technique of Solving Sudoku

- create 3 arrays each one for rows, columns and boxes of size N
- boxes are indexed from 0 to 8. In order to find the box index use this formula: row / 3*3+ column / 3
- map the initial values of grid
- each time we add an element to the grid or remove an element from the grid set the bit to 1 or 0 accordingly to the corresponding bitmasks
- since for every unassigned index there are 9 possible options, so time complexity is $O(9^{\circ}(N^{\circ}2))$. Time complexity remains the same but checking if a number is safe to use is much faster as it takes O(1)
- since for storing the output array a matrix is needed and 3 extra arrays of size N are required for bitmasks, so space complexity is $O(N^2)$

C:\Us	sers\dell	l\Desktop	\advance	ed algor:	ithms>gc	bitmas	KS.C		
C:\Us	sers\del]	L\Desktor	\advance	ed algor:	ithms>a				
3	1	6	5	7	8	4	9	2	
5	2	9	1	3	4	7	6	8	
4	8	7	6	2	9	5	3	1	
2	6	3	4	1	5	9	8	7	
9	7	4	8	6	3	1	2	5	
8	5	1	7	9	2	6	4	3	
1	3	8	9	4	7	2	5	6	
6	9	2	3	5	1	8	7	4	
7	4	5	2	8	6	3	1	9	

Sudoku game developed using brute force approach

sudoku_server.c

```
#include<stdio.h>
#include<stdlib.h>
#include "sudoku header.h"
int **createPuzzle()
    int **puzzle;
    int arrayPuzzle[9][9] = {{ 3, 0, 6, 5, 0, 8, 4, 0, 0 },
                             { 5, 2, 0, 0, 0, 0, 0, 0, 0 },
                             \{ 0, 8, 7, 0, 0, 0, 0, 3, 1 \},
                             { 0, 0, 3, 0, 1, 0, 0, 8, 0 },
                             { 9, 0, 0, 8, 6, 3, 0, 0, 5 },
                             \{0, 5, 0, 0, 9, 0, 6, 0, 0\},\
                             { 0, 0, 0, 0, 0, 0, 0, 7, 4 },
   puzzle = (int**)malloc(sizeof(int*) * 9);
    for(int i = 0; i < 9; i++)
       puzzle[i] = (int*)malloc(sizeof(int) * 9);
       for(int j = 0; j < 9; j++)
            puzzle[i][j] = arrayPuzzle[i][j];
   return puzzle;
```

```
void printPuzzle(int **puzzle)
   printf("\n");
   printf("0 | 1 2 3 | 4 5 6 | 7 8 9 | X\n");
   printf("
   for(int i = 0, a = 1; i < 9; i++, a++)
        for(int j = 0; j < 9; j++)
            if(j == 0)
              printf(" %d |", a);
            else if(j\%3 == 0)
               printf("|");
            printf(" %d ", puzzle[i][j]);
if(j == 8)
                printf("|");
       printf("\n");
       if((i + 1) \% 3 == 0)
            printf("
   printf(" Y\n");
```

```
int solvePuzzle(int **puzzle)
   int j;
   if(!checkAvailable(puzzle,&i,&j))
   for(int val = 1;val < 10;val++)</pre>
        if(checkBox(puzzle,i,j,val))
            puzzle[i][j] = val;
            if(solvePuzzle(puzzle))
                puzzle[i][j] = 0;
   return 0;
int **copyPuzzle(int **puzzle)
   int **newPuzzle;
   newPuzzle = (int**)malloc(sizeof(int*) * 9);
   for (int i = 0; i < 9; i++)
       newPuzzle[i] = (int*)malloc(sizeof(int) * 9);
        for(int j = 0; j < 9; j++)
            newPuzzle[i][j] = puzzle[i][j];
   return newPuzzle;
```

```
oid userChoice(int **userPuzzle,int **tempPuzzle)
  int positionX;
  int positionY;
  int userVal;
  int j;
      if(!checkAvailable(userPuzzle,&i,&j))
          printf("\nsuccessfully solved the puzzle!\n");
      while(1)
          printf("\npress enter to continue or press q to quit\n");
          c = getchar();
              getchar();
              solvePuzzle(userPuzzle);
              printf("\nsolved puzzle:\n");
              printPuzzle(userPuzzle);
          else if((c != '\n') && (c != 'q'))
              getchar();
      printf("\nenter coordinate for the square to insert value as X Y:\n");
      scanf("%d %d",&positionX,&positionY);
      while(1)
```

```
for(int i = 0;i < 9;i++)
{
    for(int j = 0;j < 9;j++)
        tempPuzzle[i][j] = userPuzzle[i][j];
}
if(!solvePuzzle(tempPuzzle))
{
    printf("\nvalue entered is not leading to the solution, so try again\n",positionX + 1,positionY + 1);
    userPuzzle[positionY][positionX] = 0;
}
getchar();
printPuzzle(userPuzzle);
}
return;
}</pre>
```

```
#include<stdio.h>
#include<stdlib.h>
#include"sudoku header.h"
int main()
    int **puzzle = createPuzzle();
    int **userPuzzle = copyPuzzle(puzzle);
    int **tempPuzzle = copyPuzzle(puzzle);
    printf("Rules-\n\n");
    printf("The objective of sudoku is to fill a 9x9 grid made of squares such that each row,
    each column and each full 3x3 squares use numbers from 1 to 9 only one time\n");
    printf("Insert numbers in the squares having value 0\n");
   printf("To check solved puzzle press q key\n\n");
    printf("Let's start the game!\n");
    printPuzzle(userPuzzle);
    userChoice(userPuzzle,tempPuzzle);
    free(puzzle);
    free(userPuzzle);
    free(tempPuzzle);
```

sudoku_header.h

```
int **createPuzzle();
void printPuzzle(int **puzzle);
int checkAvailable(int **puzzle,int *row,int *column);
int checkBox(int **puzzle,int row,int column,int val);
int solvePuzzle(int **puzzle);
int **copyPuzzle(int **puzzle);
void userChoice(int **userPuzzle,int **tempPuzzle);
```

```
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```

```
enter coordinate for the square to insert value as X Y:
0 3
7 10
can't insert value to this coordinate, so enter new coordinate
 an't insert value to this coordinate, so enter new coordinate
2 1
enter value from 1 to 9
value entered is already present in that row or column or box, so try again
 0 | 1 2 3 | 4 5 6 | 7 8 9 | X
   | 3 0 6 | 5 0 8 | 4 0 0 |
| 5 2 0 | 0 0 0 0 0 0 0 0
| 0 8 7 | 0 0 0 0 0 3 1 |
 1 |
 3 | 0
           3 | 0 1 0 | 0 8 0 |
0 | 8 6 3 | 0 0 5 |
0 | 0 9 0 | 6 0 0 |
         3 0 | 0 0 0 | 2 5 0 |
            0 | 0 0
5 | 2 0
                        0 | 0 7
6 | 3 0
8 | 0
9 | 0
```

```
press enter to continue or press q to quit
enter coordinate for the square to insert value as X Y:
5 1
enter value from 1 to 9
0 | 1 2 3 | 4 5 6 | 7 8 9 | X
1 | 3 1 6 | 5 7 8 | 4 0 0 |
2 | 5 2 0 | 0 0 0 | 0 0 0 |
 3 | 0 8 7 | 0 0 0 | 0 3 1 |
4 | 0 0 3 | 0 1 0 | 0 8 0 |
  9 0 0 8 6 3 0
 5
                         0 5
 6 | 0 5 0 | 0 9 0 | 6
                         0
                            0
  | 1 3 0 | 0 0 0 | 2 5 0
8 | 0 0 0 | 0 0 0 | 0 7 4
9 | 0 0 5 | 2 0 6 | 3 0 0 |
```