Lending Club Data Analysis

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Dataset details: The lending club dataset is a collection of installment loan records, including credit grid data (e.g. FICO, revolving balance, etc.) and loan performance (e.g. loan status).

The data is stored in a postgres database on AWS. Please use the below information to connect to the database with your tool of choice to access the data (R, Python, SQL, etc.)

There are 4 tables for you to use: . lending_club_2007_2011 . lending_club_2012_2013 . lending_club_2014 . lending_club_2015

```
## Loading tidyverse: ggplot2
## Loading tidyverse: tibble
## Loading tidyverse: tidyr
## Loading tidyverse: readr
## Loading tidyverse: purrr
## Loading tidyverse: dplyr
## Conflicts with tidy packages ------
## filter(): dplyr, stats
## lag():
            dplyr, stats
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
      as.Date, as.Date.numeric
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
      select
## Loading required package: gplots
##
## Attaching package: 'gplots'
##
  The following object is masked from 'package:stats':
##
##
      lowess
## Loading required package: Matrix
## Attaching package: 'Matrix'
## The following object is masked from 'package:tidyr':
##
##
      expand
## Loading required package: foreach
```

```
##
## Attaching package: 'foreach'
## The following objects are masked from 'package:purrr':
##
       accumulate, when
## Loaded glmnet 2.0-5
## randomForest 4.6-12
## Type rfNews() to see new features/changes/bug fixes.
## Attaching package: 'randomForest'
## The following object is masked from 'package:dplyr':
##
##
       combine
## The following object is masked from 'package:ggplot2':
##
       margin
## Loading required package: RPostgreSQL
## Loading required package: DBI
dim(lending_club_consolidated)
summary(lending_club_consolidated)
Based on the summary, cleaning consolidated lending dataset
#Deleting row containing Memberid as NA (all columns are NA for this observation)
lending_club_consolidated <- lending_club_consolidated[!is.na(</pre>
  lending_club_consolidated$member_id),]
#Converting id to numeric datatype
lending_club_consolidated$id = as.numeric(lending_club_consolidated$id)
#Creating a new column from issue_d as a date datatype
lending_club_consolidated\sissue_date<-as.Date(as.yearmon(lending_club_consolidated\sissue_d,
                                                            format = \frac{\text{''}}{b} - \frac{\text{''}}{Y}'')
#Creating a new column from earliest_cr_line as a date datatype
lending_club_consolidated$earliest_cr_line_date<-</pre>
  as.Date(as.yearmon(lending_club_consolidated$earliest_cr_line, format = "%b-%Y"))
#Converting interest rate to numeric datatype
lending_club_consolidated$int_rate = as.numeric(gsub("\\\", "",
                                                        lending_club_consolidated$int_rate))
#Converting revol_util to numeric datatype
lending_club_consolidated$revol_util = as.numeric(gsub("\\\", "",
                                                          lending_club_consolidated$revol_util))
#Converting term to numeric datatype
lending_club_consolidated$term <- as.numeric(substr</pre>
                                               (lending_club_consolidated$term,0,3))
```

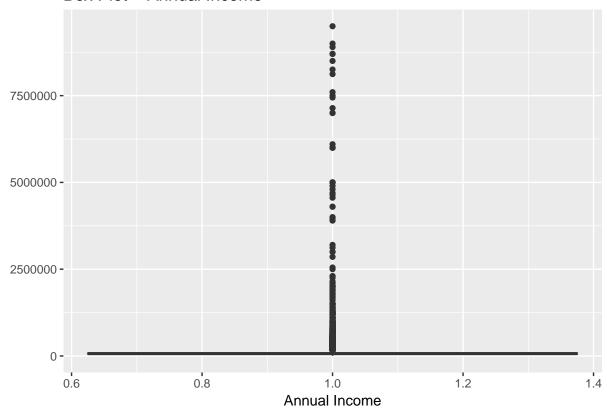
Below are two sections of data questions relating to the Lending Club dataset and another question that is not related to it. Please try and answer all the questions. Quality is much more important than quantity.

Going through the dataset we can understand that Lending club dataset contains information about loan given out to people who have number of different purposes. The information has been captured from 2007 to 2015. There are 111 different columns. Some of the key columns with regards to below analysis are loan_amnt, grade, term, issue_d, loan_status, etc.

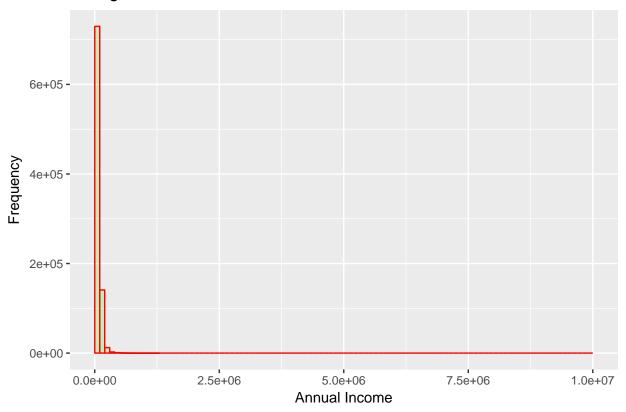
1. Does the data have any outliers?

Outliers are observations that are abnormally out of range of the other values for a random sample from the population. To find out outliers I looked at the summary of the consolidated lending dataset. This helped understand that mostly none of the features had such abnormal observations, except for a couple of important ones like annual_inc and tot_hi_cred_lim.

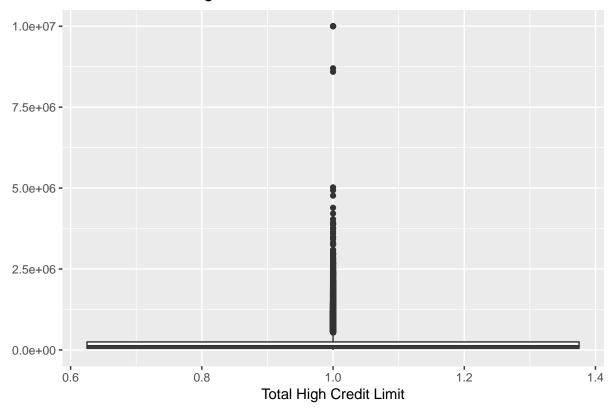
Box Plot - Annual Income



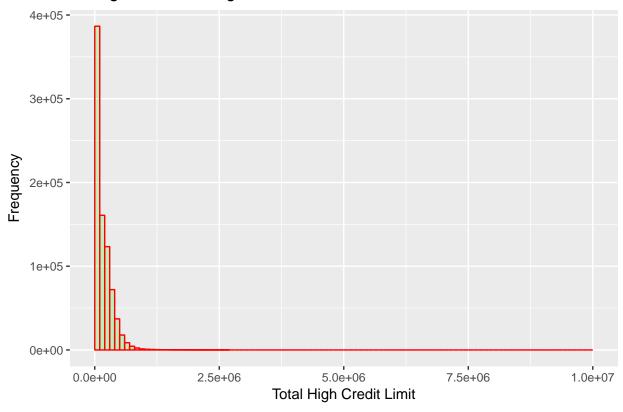
Histogram - Annual Income



Box Plot - Total High Credit Limit



Histogram - Total High Credit Limit

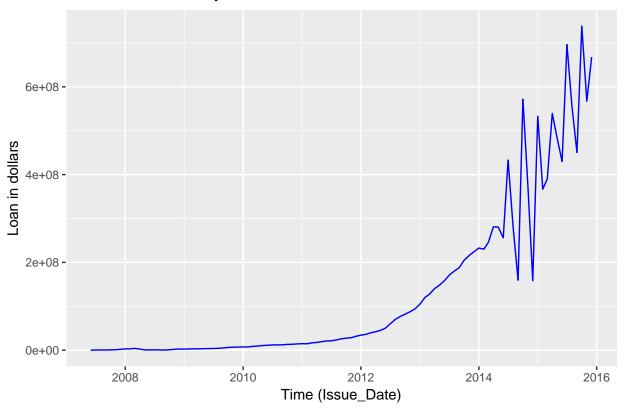


From the above graphics we can see that some of the observations for annual_inc and tot_hi_cred_lim are outliers. This becomes very evident from the box plot where the 1st and 3rd quartiles are very near to the baseline and other values are abnormally higher. Logically, an annual income of \$9500000 is abnormally high for a person applying for a loan. It also is clear from 3rd quartile value being almost 100 times lesser. Similarly for a credit limit of \$9999999, is abnormally high when compared to 3rd quartile values is around \$250000. Thus there are some outliers in the dataset which may have been captured due to wrong entry by the loan applicant.

2. What is the monthly total loan volume by dollars and by average loan size?

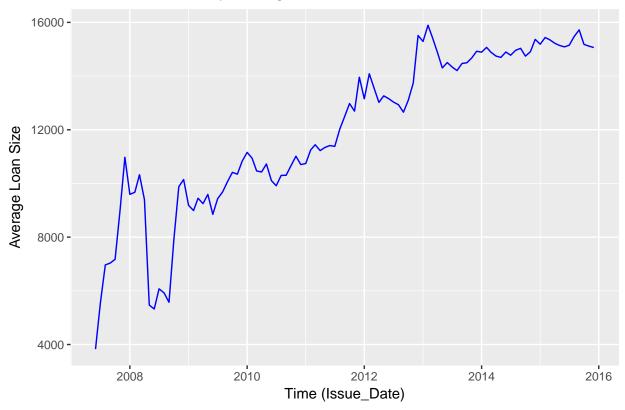
For us to look at the monthly trend of loan volume, we need group together loans issued in individual months. Following on that we can calculate monthly total loan volume by dollars and monthly total loan volume by average loan size.

Total loan volume by dollars



From the above graphic we can see that the total loan issued per month was almost constant in the period from 2007-12, but after that there is a steep rise until mid of 2014 after which it has been quite fluctuating.

Total loan volume by average loan size



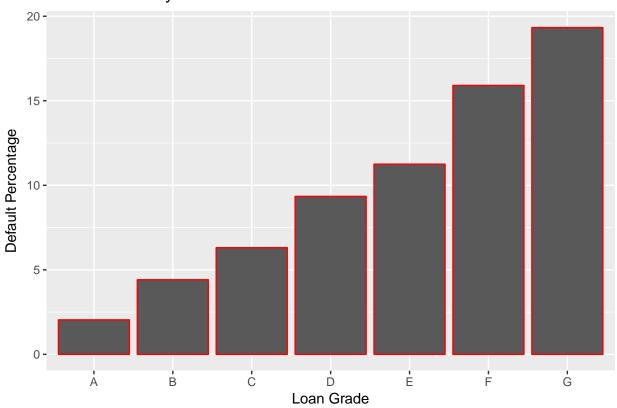
From above graphic we can see that total loan volume by average loan size has been steadily increaseing over the years although a dip is seen in the period between 2008-09. This dip may be on account of the 2008 financial crisis where the average loan issued took a hit.

3. What are the default rates by Loan Grade?

To calculate the default rates, we use the loan_status column which identifies the current status of the loan. As per my knowledge, the status of the loan changes from current to late to default to charged off, if the loan is not payed before due date. Thus in order to calculate the percentage of default in each grade, I have also considered loans which were charged off. I am considering charged of loans because at some stage these loans were in default stage and due to no payment from the loan applicant the status have been moved to charged off.

```
#Plotting Default rates by Loan Grade
ggplot(default_prop_by_grade, aes(x = grade, y= DefaultPercentage)) +
   geom_bar(stat = "identity", colour="red") +
   labs(title = "Default Rates by Loan Grade", x = "Loan Grade", y = "Default Percentage")
```

Default Rates by Loan Grade

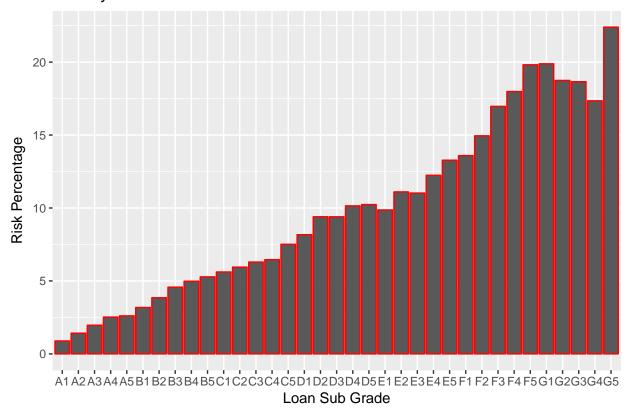


The bar plot shows the sum of default percentages per grade. We can see that the default percentages increase from grade A through G. This is expected as per lending club website because grade A is more risk free than grades through G.

4. Are we charging an appropriate rate for risk?

To answer this question we need to have a measure for risk. Assuming that we consider the likelihood of a loan getting "Charged off", "Default" or "Late" as the risk, we can calculate percentage of loans having such status per subgrade. Using this risk measure we can make plot of subgrade vs. risk. We can also find the correlation between risk and mean interest rate per subgrade, to answer our quastion more appropriately

Risk by Loan Sub Grade



#Finding correlation between Risk and Mean Interest rate per sub grade cor(risk_int_rate_df\$Risk, risk_int_rate_df\$Mean_Interest_Rate)

[1] 0.976253

The correlation between Risk and Mean Interest rate is as high as 0.976. Thus we can say that we are actually charging appropriate rate for the risk. With increase in risk there is an increase in interest rate charged to the customers. From the graphic of Risk by Loan Sub Grade, it is expected that risk percentage should increase as we move from sub grades A1-A5 through G1-G5. This is very much the case, except for ris being less for G2, G3 and G4 than G1 and F5. Thus it could be case of miss categorizing customers to wrong sub

grades. But overall, I would say we are charging an appropriate rate for risk.

5. What are the top 5 predictors of default rate by order of importance? Explain the model that you used and discuss how you validated it.

As assumed in the above questions, default on loan is followed by charged off, thus considering charged off status as also default, I am creating a new variable on the dataset which is a categorical variable indicating 1 for default and 0 for not default.

As we discovered there are some outliers in our data, I would like to assume that these have been introduced due to human error and thus can removed from the dataset. For annual income, as the 3rd quartile is \$90000, I would like to ignore values beyond \$1,50,000, this is keeping in mind any person having an annual salary greater than \$1,50,000 is less likely to apply for loan of 500 to 30000 dollars. Another outlier found was in tot_hi_cred_lim. The 3rd quartile value is \$247777, thus a value of \$500000 sounds reasonable for an upper limit.

Now to create a model to predict default rate, I plan to logically cut down the features to 20-25 as many of the features in the dataset arent very useful for prediction. The required subset of features according to my understanding are captured into the new dataframe as below:

NA values hinder in building an efficient model and since there are only small portion rows containing NA's, I am ignoring them.

As we are trying to predict a qualitative variable, if there is a default or not on a loan, I plan to use Logistic regression for building the model. Firsty, setting the seed as to achieve same result on each run and avoid different random sampling on each iteration. Secondly, segregating dataset into train and test. Thirdly,

running glm function for logistic regression.

Note: Due to computational restrictions, I am reducing the size of dataset to 10% of the actual lending_club_model_df.

```
set.seed(1)
#Reducing size of the dataset because of computational restrictions
reduced_population_size <- sample(nrow(lending_club_model_df),</pre>
                                  nrow(lending_club_model_df)*0.1)
reduced_lending_club_model_df <- lending_club_model_df [reduced_population_size, ]</pre>
#Segregating training and test data
train <- sample(nrow(reduced_lending_club_model_df),</pre>
                nrow(reduced_lending_club_model_df)*0.7)
lending_club_model_df.train <- reduced_lending_club_model_df[train, ]</pre>
lending_club_model_df.test <- reduced_lending_club_model_df[-train, ]</pre>
#Fitting logistic regression model
logit.fit <- glm ( default_category ~ .,</pre>
                  data = lending_club_model_df.train , family = "binomial" )
summary(logit.fit)
##
## Call:
## glm(formula = default_category ~ ., family = "binomial", data = lending_club_model_df.train)
## Deviance Residuals:
       Min
                 10
                      Median
                                   30
                                           Max
## -1.5154 -0.3529 -0.2275 -0.1472
                                         3.3735
## Coefficients: (6 not defined because of singularities)
##
                                        Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                                              21.781 < 2e-16
                                       4.140e+01 1.901e+00
## loan_amnt
                                      -9.204e-06 1.917e-05
                                                              -0.480 0.631098
## int_rate_percent
                                      -1.511e-02 3.473e-02 -0.435 0.663594
                                                               3.453 0.000554
## gradeB
                                       1.443e+00 4.180e-01
## gradeC
                                       1.838e+00 4.874e-01
                                                               3.771 0.000163
## gradeD
                                       2.444e+00 5.714e-01
                                                               4.278 1.88e-05
## gradeE
                                       2.915e+00 6.713e-01
                                                              4.342 1.41e-05
                                                               4.033 5.50e-05
                                       3.133e+00 7.768e-01
## gradeF
## gradeG
                                       3.338e+00 9.204e-01
                                                               3.627 0.000286
                                       3.481e-01 4.206e-01
                                                               0.828 0.407864
## sub_gradeA2
                                       4.681e-01 4.038e-01
## sub_gradeA3
                                                               1.159 0.246334
                                       2.758e-01 3.827e-01
## sub gradeA4
                                                               0.721 0.471124
## sub gradeA5
                                       7.174e-01 3.680e-01
                                                               1.950 0.051230
## sub_gradeB1
                                      -2.940e-01 1.967e-01 -1.495 0.134978
## sub_gradeB2
                                      -4.479e-01 1.718e-01
                                                              -2.606 0.009151
                                      -1.441e-01 1.451e-01
                                                              -0.993 0.320612
## sub_gradeB3
## sub_gradeB4
                                      -1.266e-01 1.342e-01
                                                              -0.943 0.345428
## sub_gradeB5
                                              NA
                                                          NA
                                                                  NA
                                                              -2.165 0.030410
## sub_gradeC1
                                      -3.319e-01 1.533e-01
## sub_gradeC2
                                      -1.421e-01 1.377e-01
                                                              -1.032 0.302072
                                       4.102e-02 1.249e-01
                                                               0.328 0.742601
## sub_gradeC3
## sub_gradeC4
                                       1.574e-02 1.204e-01
                                                             0.131 0.896039
```

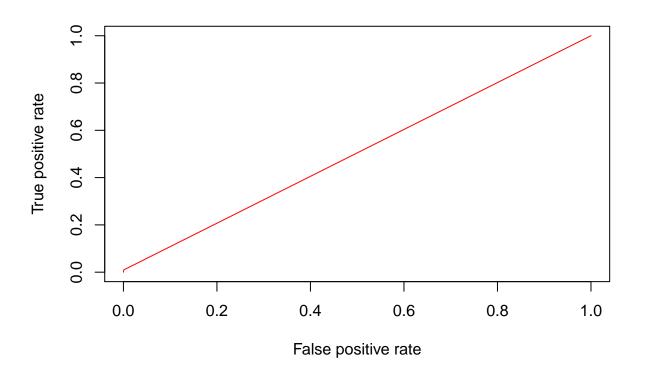
```
## sub_gradeC5
                                                   1.542e-01
                                                               -2.129 0.033282
## sub_gradeD1
                                       -3.283e-01
## sub gradeD2
                                       -1.833e-01
                                                   1.465e-01
                                                               -1.251 0.210997
## sub_gradeD3
                                       -1.869e-01
                                                   1.426e-01
                                                               -1.311 0.189934
## sub gradeD4
                                       -6.079e-02
                                                   1.374e-01
                                                               -0.442 0.658177
## sub gradeD5
                                               NA
                                                           NA
                                                                   NΑ
## sub gradeE1
                                                   1.935e-01
                                                               -2.480 0.013140
                                       -4.798e-01
## sub_gradeE2
                                       -2.246e-01
                                                   1.781e-01
                                                               -1.261 0.207344
## sub_gradeE3
                                       -2.887e-01
                                                   1.794e-01
                                                               -1.609 0.107655
## sub_gradeE4
                                       -3.942e-01
                                                   1.865e-01
                                                               -2.114 0.034517
## sub_gradeE5
                                               NA
                                                           NA
                                                                   NA
                                                                             NA
                                       -4.763e-01
                                                   2.873e-01
                                                               -1.658 0.097363
## sub_gradeF1
## sub_gradeF2
                                       -3.955e-01
                                                   2.956e-01
                                                               -1.338 0.180948
## sub_gradeF3
                                        1.584e-02
                                                   2.867e-01
                                                                0.055 0.955950
                                                               -0.284 0.776085
## sub_gradeF4
                                       -8.655e-02
                                                   3.043e-01
## sub_gradeF5
                                               NA
                                                           NA
                                                                   NA
                                                                             NA
                                                               -0.427 0.669293
## sub_gradeG1
                                       -2.394e-01
                                                   5.604e-01
## sub gradeG2
                                        3.722e-01
                                                   5.491e-01
                                                                0.678 0.497953
## sub_gradeG3
                                       -8.440e-02
                                                   6.103e-01
                                                               -0.138 0.890015
## sub gradeG4
                                       -7.772e-01
                                                   7.285e-01
                                                               -1.067 0.286083
## sub_gradeG5
                                               NA
                                                           NA
                                                                   NA
                                                                            NΔ
## annual inc
                                       -8.036e-06
                                                   1.054e-06
                                                               -7.626 2.43e-14
## verification_statusSource Verified 1.045e-01
                                                   5.683e-02
                                                                1.839 0.065850
## verification statusVerified
                                                                0.887 0.375006
                                        4.891e-02
                                                   5.513e-02
## term_in_months
                                        1.125e-03
                                                  4.911e-03
                                                                0.229 0.818793
## dti
                                        1.073e-02
                                                   2.913e-03
                                                                3.683 0.000231
## earliest_cr_line_date
                                                   8.745e-06
                                                                3.775 0.000160
                                        3.301e-05
## inq_last_6mths
                                        9.576e-02
                                                   1.965e-02
                                                                4.874 1.09e-06
                                                   5.692e-03
## open_acc
                                        7.575e-04
                                                                0.133 0.894118
                                       -6.944e-02
## pub_rec
                                                   4.483e-02
                                                               -1.549 0.121417
## revol_bal
                                        4.648e-07
                                                   1.984e-06
                                                                0.234 0.814744
## revol_util_percent
                                       -1.114e-03
                                                   1.048e-03
                                                               -1.063 0.287604
## total_acc
                                        4.259e-03
                                                   2.550e-03
                                                                1.670 0.094867
                                                   4.352e-02
## initial_list_statusw
                                       -7.343e-03
                                                               -0.169 0.865993
## application_typeJOINT
                                       -1.075e+01
                                                   1.883e+02
                                                               -0.057 0.954488
                                                   3.051e-01
## acc_now_deling
                                       -1.448e-01
                                                               -0.474 0.635215
## deling 2yrs
                                       -2.148e-03
                                                   2.439e-02
                                                               -0.088 0.929835
## installment
                                       7.007e-04
                                                   5.908e-04
                                                                1.186 0.235592
## addr stateAL
                                       -8.113e-03
                                                   4.679e-01
                                                               -0.017 0.986165
                                                   5.031e-01
## addr_stateAR
                                       -1.436e-01
                                                               -0.285 0.775295
## addr stateAZ
                                        2.822e-01
                                                   4.511e-01
                                                                0.626 0.531585
## addr_stateCA
                                        2.761e-01
                                                   4.357e-01
                                                                0.634 0.526350
## addr stateCO
                                        1.655e-02
                                                  4.578e-01
                                                                0.036 0.971172
## addr_stateCT
                                       -7.450e-02
                                                   4.699e-01
                                                               -0.159 0.874034
## addr_stateDC
                                        1.469e-01
                                                   6.470e-01
                                                                0.227 0.820333
## addr_stateDE
                                                   5.421e-01
                                                                1.256 0.209171
                                        6.808e-01
                                        3.918e-01
## addr_stateFL
                                                   4.383e-01
                                                                0.894 0.371390
## addr_stateGA
                                        5.231e-02
                                                   4.490e-01
                                                                0.116 0.907260
                                                   4.896e-01
                                                                1.335 0.182034
## addr_stateHI
                                        6.533e-01
## addr_stateID
                                       -1.075e+01
                                                   6.211e+02
                                                               -0.017 0.986192
## addr_stateIL
                                        5.052e-02
                                                   4.460e-01
                                                                0.113 0.909798
## addr stateIN
                                       2.648e-01
                                                   4.585e-01
                                                                0.577 0.563614
                                       1.823e-01 4.801e-01
## addr stateKS
                                                                0.380 0.704193
## addr stateKY
                                        1.245e-01 4.805e-01
                                                                0.259 0.795596
```

```
## addr stateLA
                                        4.774e-01 4.634e-01
                                                                1.030 0.302938
                                        3.092e-01 4.515e-01
## addr_stateMA
                                                                0.685 0.493517
## addr stateMD
                                        3.319e-01
                                                   4.505e-01
                                                                0.737 0.461273
## addr_stateME
                                       -1.026e+01
                                                   1.246e+02
                                                               -0.082 0.934380
## addr stateMI
                                        6.456e-02
                                                   4.512e-01
                                                                0.143 0.886216
## addr stateMN
                                        3.753e-02 4.595e-01
                                                                0.082 0.934915
## addr stateMO
                                        2.615e-01
                                                   4.566e-01
                                                                0.573 0.566785
## addr_stateMS
                                       -2.159e-01
                                                   5.851e-01
                                                               -0.369 0.712112
## addr stateMT
                                       -5.518e-01
                                                   6.723e-01
                                                               -0.821 0.411853
## addr_stateNC
                                       9.923e-02
                                                  4.492e-01
                                                                0.221 0.825165
## addr_stateND
                                       -1.010e+01
                                                  1.762e+02
                                                               -0.057 0.954272
## addr_stateNE
                                                               -0.171 0.864432
                                       -1.877e-01
                                                   1.099e+00
## addr_stateNH
                                       -4.426e-01
                                                   5.845e-01
                                                               -0.757 0.448886
## addr_stateNJ
                                        1.905e-01
                                                   4.463e-01
                                                                0.427 0.669426
                                                   4.940e-01
                                                                1.059 0.289506
## addr_stateNM
                                        5.232e-01
## addr_stateNV
                                        4.331e-01
                                                   4.554e-01
                                                                0.951 0.341599
## addr_stateNY
                                        3.448e-01
                                                   4.378e-01
                                                                0.788 0.430967
## addr stateOH
                                        9.028e-02
                                                   4.463e-01
                                                                0.202 0.839674
                                                   4.731e-01
                                                                0.801 0.423387
## addr_stateOK
                                        3.787e-01
## addr stateOR
                                        2.459e-01
                                                   4.644e-01
                                                                0.530 0.596410
## addr_statePA
                                        2.799e-01
                                                  4.445e-01
                                                                0.630 0.528908
## addr stateRI
                                                   5.079e-01
                                                                0.473 0.636255
                                        2.402e-01
## addr_stateSC
                                                               -0.923 0.356021
                                       -4.538e-01
                                                   4.917e-01
## addr stateSD
                                                   6.384e-01
                                       -1.143e-01
                                                               -0.179 0.857957
## addr stateTN
                                        4.183e-01
                                                   4.556e-01
                                                                0.918 0.358533
## addr stateTX
                                        9.984e-02 4.386e-01
                                                                0.228 0.819928
## addr_stateUT
                                        2.351e-01
                                                   4.876e-01
                                                                0.482 0.629654
## addr_stateVA
                                        3.085e-01
                                                   4.471e-01
                                                                0.690 0.490162
                                                   5.766e-01
## addr_stateVT
                                        4.688e-01
                                                                0.813 0.416157
## addr_stateWA
                                        1.086e-01
                                                   4.541e-01
                                                                0.239 0.811037
## addr_stateWI
                                       -1.088e-01
                                                   4.718e-01
                                                               -0.231 0.817694
## addr_stateWV
                                       -1.829e-01
                                                   5.362e-01
                                                               -0.341 0.733073
## addr_stateWY
                                       -1.532e-01
                                                   6.103e-01
                                                              -0.251 0.801787
                                       -2.862e-03 1.033e-04 -27.706 < 2e-16
## issue_date
##
## (Intercept)
                                       ***
## loan amnt
## int_rate_percent
## gradeB
                                       ***
## gradeC
                                       ***
## gradeD
## gradeE
                                       ***
## gradeF
                                       ***
## gradeG
                                       ***
## sub_gradeA2
## sub_gradeA3
## sub_gradeA4
## sub_gradeA5
## sub_gradeB1
## sub_gradeB2
## sub_gradeB3
## sub_gradeB4
## sub_gradeB5
## sub gradeC1
```

```
## sub_gradeC2
## sub_gradeC3
## sub_gradeC4
## sub_gradeC5
## sub_gradeD1
## sub_gradeD2
## sub_gradeD3
## sub_gradeD4
## sub_gradeD5
## sub_gradeE1
## sub_gradeE2
## sub_gradeE3
## sub_gradeE4
## sub_gradeE5
## sub_gradeF1
## sub_gradeF2
## sub_gradeF3
## sub_gradeF4
## sub_gradeF5
## sub_gradeG1
## sub_gradeG2
## sub_gradeG3
## sub_gradeG4
## sub_gradeG5
## annual_inc
                                       ***
## verification_statusSource Verified .
## verification_statusVerified
## term_in_months
## dti
                                       ***
## earliest_cr_line_date
                                       ***
## inq_last_6mths
                                       ***
## open_acc
## pub_rec
## revol_bal
## revol_util_percent
## total_acc
## initial_list_statusw
## application_typeJOINT
## acc_now_deling
## delinq_2yrs
## installment
## addr_stateAL
## addr_stateAR
## addr_stateAZ
## addr_stateCA
## addr_stateCO
## addr_stateCT
## addr_stateDC
## addr_stateDE
## addr_stateFL
## addr_stateGA
## addr_stateHI
## addr_stateID
## addr_stateIL
```

```
## addr_stateIN
## addr_stateKS
## addr stateKY
## addr_stateLA
## addr_stateMA
## addr stateMD
## addr stateME
## addr_stateMI
## addr_stateMN
## addr_stateMO
## addr_stateMS
## addr_stateMT
## addr_stateNC
## addr_stateND
## addr_stateNE
## addr_stateNH
## addr_stateNJ
## addr_stateNM
## addr_stateNV
## addr_stateNY
## addr_stateOH
## addr_stateOK
## addr_stateOR
## addr statePA
## addr_stateRI
## addr_stateSC
## addr_stateSD
## addr_stateTN
## addr_stateTX
## addr_stateUT
## addr_stateVA
## addr_stateVT
## addr_stateWA
## addr_stateWI
## addr_stateWV
## addr_stateWY
## issue date
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
   (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 22649 on 52396 degrees of freedom
## Residual deviance: 19118 on 52293 degrees of freedom
## AIC: 19326
##
## Number of Fisher Scoring iterations: 13
#Predicting on test data
logit.probs <- predict(logit.fit, newdata = lending_club_model_df.test, type = "response")</pre>
## Warning in predict.lm(object, newdata, se.fit, scale = 1, type =
## ifelse(type == : prediction from a rank-deficient fit may be misleading
```

```
logit.probs <- ifelse(logit.probs > 0.5, 1, 0)
#Confusion Matrix
confmatrix_default_category<- table(lending_club_model_df.test$default_category,</pre>
                                     logit.probs)
confmatrix_default_category
##
      logit.probs
##
           0
     0 21186
                 14
##
     1 1245
##
                 12
#Accuracy of the model
sum(diag(confmatrix_default_category))/sum(confmatrix_default_category)
## [1] 0.9439373
#Checking performance of the model by plotting ROC curve
pr <- prediction(logit.probs, lending_club_model_df.test$default_category)</pre>
prf <- performance(pr, measure = "tpr", x.measure = "fpr")</pre>
plot(prf, col=rainbow(5))
```



```
#Area under the curve
auc <- performance(pr, measure = "auc")
auc <- auc@y.values[[1]]
auc</pre>
```

[1] 0.5044431

From the model generated, there are some variables which have little statistical significance as the pvalue is greater than 0.05. Thus these can be ignored while building the final model. Now, to understand the accuracy and performance of the model, we can look at the confusion matrix. It has a very good accuracy level though there are 1245 falsepositive and 14 Falsenegatives which are misclassified. To understand the performance of the model, we look at the ROC curve. As the AUC is very small, the performance of the model is not great. High performing models have ROC curve touching the top left orner and covering more area. Thus addition of deletion of features are required for the model. We can also look at AIC which is a measure of goodness of fit and can be used for model selection.

Now to reduce the number of features and select the best set of features, we can choose between backward subset selection method or lasso regression. In backward stepwise selection, a model with all features is considered initially and then based on performance of the model one or more features are removed and the process is continued untill we get the best mode.

In case of Lasso, the coefficients of the features which are not as significant are reduced to zero.

revol_bal + revol_util_percent + total_acc + initial_list_status +

application type + acc now deling + deling 2yrs + installment +

```
##
## Step: AIC=19326.03
## default_category ~ loan_amnt + int_rate_percent + sub_grade +
## annual_inc + verification_status + term_in_months + dti +
## earliest_cr_line_date + inq_last_6mths + open_acc + pub_rec +
## revol_bal + revol_util_percent + total_acc + initial_list_status +
## application_type + acc_now_delinq + delinq_2yrs + installment +
## addr_state + issue_date
```

```
##
##
                            Df Deviance
                                           AIC
                                  19194 19304
## - addr_state
                            49
## - sub_grade
                            34
                                  19176 19316
## - deling 2yrs
                             1
                                  19118 19324
                                  19118 19324
## - open acc
                             1
## - initial list status
                             1
                                  19118 19324
## - term_in_months
                             1
                                  19118 19324
## - revol bal
                             1
                                  19118 19324
## - int_rate_percent
                             1
                                  19118 19324
## - loan amnt
                             1
                                  19118 19324
## - acc_now_deling
                             1
                                  19118 19324
## - application_type
                             1
                                  19119 19325
## - revol_util_percent
                             1
                                  19119 19325
## - installment
                             1
                                  19119 19325
## - verification_status
                             2
                                  19122 19326
## <none>
                                  19118 19326
## - pub_rec
                                  19121 19327
                             1
## - total_acc
                                  19121 19327
```

addr_state + issue_date

##

##

##

##

```
19132 19338
## - dti
## - earliest_cr_line_date 1
                               19133 19339
## - ing last 6mths
                           1
                               19141 19347
## - annual_inc
                               19179 19385
                           1
## - issue date
                           1
                               19824 20030
##
## Step: AIC=19303.69
## default_category ~ loan_amnt + int_rate_percent + sub_grade +
##
      annual inc + verification status + term in months + dti +
##
      earliest_cr_line_date + inq_last_6mths + open_acc + pub_rec +
##
      revol_bal + revol_util_percent + total_acc + initial_list_status +
##
      application_type + acc_now_deling + deling_2yrs + installment +
##
      issue_date
##
##
                          Df Deviance
## - sub_grade
                          34
                               19253 19295
## - deling_2yrs
                               19194 19302
                          1
## - initial list status
                          1 19194 19302
## - term_in_months
                          1 19194 19302
## - open acc
                           1
                              19194 19302
## - revol_bal
                          1 19194 19302
## - int_rate_percent
                          1 19194 19302
## - acc_now_deling
                          1 19194 19302
## - loan amnt
                           1 19194 19302
                           1 19195 19303
## - application_type
## - revol_util_percent
                           1 19195 19303
## - verification_status
                           2 19197 19303
                               19195 19303
## - installment
                           1
                               19196 19304
## - total_acc
                           1
## <none>
                               19194 19304
## - pub_rec
                               19197 19305
## - dti
                           1
                               19206 19314
## - earliest_cr_line_date 1
                               19210 19318
                               19215 19323
## - inq_last_6mths
                           1
## - annual inc
                           1
                               19253 19361
## - issue date
                           1
                               19912 20020
##
## Step: AIC=19295.39
## default_category ~ loan_amnt + int_rate_percent + annual_inc +
##
      verification_status + term_in_months + dti + earliest_cr_line_date +
##
      ing last 6mths + open acc + pub rec + revol bal + revol util percent +
##
      total_acc + initial_list_status + application_type + acc_now_deling +
      delinq_2yrs + installment + issue_date
##
##
                          Df Deviance
                               19253 19293
## - loan_amnt
                           1
## - delinq_2yrs
                           1
                               19253 19293
                           1 19253 19293
## - term_in_months
## - initial_list_status
                           1 19253 19293
## - revol_bal
                           1 19253 19293
                              19254 19294
## - open_acc
                           1
                          1 19254 19294
## - acc_now_delinq
## - revol_util_percent
                          1 19254 19294
## - installment
                           1 19254 19294
```

```
## - application_type
                          1
                               19254 19294
## - total_acc
                               19255 19295
                               19253 19295
## <none>
## - verification_status
                               19258 19296
                           2
## - pub_rec
                           1
                               19256 19296
## - dti
                               19268 19308
                           1
## - earliest cr line date 1 19271 19311
## - inq last 6mths
                               19277 19317
                           1
## - annual_inc
                           1
                               19317 19357
## - int_rate_percent
                               19605 19645
                           1
## - issue_date
                           1
                               20762 20802
##
## Step: AIC=19293.39
## default_category ~ int_rate_percent + annual_inc + verification_status +
      term_in_months + dti + earliest_cr_line_date + inq_last_6mths +
##
      open_acc + pub_rec + revol_bal + revol_util_percent + total_acc +
##
      initial_list_status + application_type + acc_now_deling +
##
      delinq_2yrs + installment + issue_date
##
                          Df Deviance AIC
##
## - delinq_2yrs
                           1
                               19253 19291
## - initial_list_status
                               19253 19291
                               19253 19291
## - revol_bal
                           1
## - term_in_months
                          1
                               19254 19292
## - open acc
                          1 19254 19292
## - acc_now_deling
                           1 19254 19292
## - revol_util_percent
                           1 19254 19292
## - application_type
                               19254 19292
                           1
                           1 19255 19293
## - total_acc
                              19253 19293
## <none>
                           2 19258 19294
## - verification_status
## - pub_rec
                           1
                               19256 19294
## - installment
                           1 19267 19305
## - dti
                               19268 19306
                           1
## - earliest_cr_line_date 1
                               19271 19309
## - inq_last_6mths
                           1
                               19277 19315
## - annual inc
                           1 19318 19356
## - int_rate_percent
                          1 19759 19797
## - issue date
                           1
                               20762 20800
##
## Step: AIC=19291.41
## default_category ~ int_rate_percent + annual_inc + verification_status +
      term_in_months + dti + earliest_cr_line_date + inq_last_6mths +
##
      open_acc + pub_rec + revol_bal + revol_util_percent + total_acc +
##
      initial_list_status + application_type + acc_now_delinq +
##
      installment + issue_date
##
##
                          Df Deviance
                                       AIC
## - initial_list_status
                           1
                               19253 19289
## - revol_bal
                           1
                               19253 19289
## - open_acc
                               19254 19290
                          1
                          1 19254 19290
## - term in months
## - acc_now_delinq
                          1 19254 19290
## - revol util percent
                           1 19254 19290
```

```
## - application_type
                           1
                               19254 19290
## - total_acc
                               19255 19291
## <none>
                               19253 19291
## - verification_status
                               19258 19292
                           2
## - pub_rec
                           1
                               19256 19292
## - installment
                               19268 19304
                           1
## - dti
                             19268 19304
                           1
## - earliest_cr_line_date 1
                               19271 19307
## - inq_last_6mths
                           1
                               19277 19313
                               19318 19354
## - annual_inc
                           1
## - int_rate_percent
                           1
                               19763 19799
                                20767 20803
## - issue_date
                           1
## Step: AIC=19289.43
## default_category ~ int_rate_percent + annual_inc + verification_status +
##
      term_in_months + dti + earliest_cr_line_date + inq_last_6mths +
##
      open_acc + pub_rec + revol_bal + revol_util_percent + total_acc +
##
      application_type + acc_now_delinq + installment + issue_date
##
                          Df Deviance AIC
##
## - revol_bal
                           1
                               19254 19288
## - open acc
                                19254 19288
                               19254 19288
## - term_in_months
                           1
## - acc now deling
                               19254 19288
                           1
                           1 19254 19288
## - revol_util_percent
## - application_type
                           1
                               19254 19288
## - total_acc
                               19255 19289
                           1
                               19253 19289
## <none>
                           2 19258 19290
## - verification_status
                           1 19256 19290
## - pub_rec
## - installment
                           1 19268 19302
## - dti
                           1
                               19268 19302
## - earliest_cr_line_date 1
                               19271 19305
## - inq_last_6mths
                               19277 19311
                           1
## - annual inc
                           1
                                19318 19352
                           1
                               19767 19801
## - int_rate_percent
## - issue date
                           1
                                20885 20919
##
## Step: AIC=19287.46
## default_category ~ int_rate_percent + annual_inc + verification_status +
      term_in_months + dti + earliest_cr_line_date + inq_last_6mths +
##
      open_acc + pub_rec + revol_util_percent + total_acc + application_type +
      acc_now_delinq + installment + issue_date
##
##
                          Df Deviance
                                19254 19286
## - term_in_months
                           1
                                19254 19286
## - open_acc
                           1
                               19254 19286
## - acc_now_deling
## - revol_util_percent
                           1
                               19254 19286
## - application_type
                           1
                                19254 19286
## - total_acc
                                19255 19287
                           1
## <none>
                               19254 19288
## - verification_status
                           2 19258 19288
                                19256 19288
## - pub_rec
```

```
## - installment 1
                                19268 19300
## - dti
                                19269 19301
                           1
## - earliest cr line date 1
                               19271 19303
## - inq_last_6mths
                                19277 19309
                           1
## - annual inc
                           1
                                19320 19352
                                19779 19811
## - int rate percent
                           1
## - issue date
                                20886 20918
                           1
##
## Step: AIC=19285.59
## default_category ~ int_rate_percent + annual_inc + verification_status +
      dti + earliest_cr_line_date + inq_last_6mths + open_acc +
##
      pub_rec + revol_util_percent + total_acc + application_type +
##
      acc_now_delinq + installment + issue_date
##
##
                          Df Deviance
## - open_acc
                           1
                                19254 19284
                                19254 19284
## - acc_now_deling
                           1
## - revol_util_percent
                           1 19254 19284
## - application_type
                              19255 19285
                           1
## - total acc
                           1
                                19255 19285
## - verification_status
                                19258 19286
                           2
## <none>
                                19254 19286
## - pub_rec
                              19256 19286
                           1
## - installment
                                19269 19299
                           1
## - dti
                               19269 19299
                           1
## - earliest_cr_line_date 1
                               19271 19301
## - inq_last_6mths
                                19279 19309
                           1
                                19323 19353
## - annual_inc
                           1
## - int_rate_percent
                          1
                               19908 19938
                                20919 20949
## - issue_date
                           1
##
## Step: AIC=19283.76
## default_category ~ int_rate_percent + annual_inc + verification_status +
##
      dti + earliest_cr_line_date + inq_last_6mths + pub_rec +
##
      revol_util_percent + total_acc + application_type + acc_now_delinq +
##
      installment + issue_date
##
##
                          Df Deviance
                                      AIC
## - acc_now_delinq
                           1
                               19254 19282
## - revol_util_percent
                                19254 19282
                           1
## - application_type
                               19255 19283
                           1
## - verification_status
                           2
                                19258 19284
                                19254 19284
## <none>
## - pub_rec
                               19256 19284
                           1
## - total_acc
                              19257 19285
                           1
                               19269 19297
## - installment
                           1
## - dti
                           1
                               19270 19298
## - earliest_cr_line_date 1 19272 19300
## - inq_last_6mths
                           1
                               19279 19307
## - annual_inc
                           1
                                19323 19351
## - int_rate_percent
                               19910 19938
                          1
                                20919 20947
## - issue_date
                           1
##
## Step: AIC=19281.99
```

```
## default_category ~ int_rate_percent + annual_inc + verification_status +
##
      dti + earliest_cr_line_date + inq_last_6mths + pub_rec +
##
      revol_util_percent + total_acc + application_type + installment +
##
      issue_date
##
##
                          Df Deviance
                                      AIC
## - revol util percent
                           1 19255 19281
## - application_type
                                19255 19281
                           1
## - verification_status
                           2
                                19258 19282
                                19254 19282
## <none>
## - pub_rec
                           1
                                19256 19282
## - total acc
                                19257 19283
                           1
## - installment
                           1
                                19269 19295
## - dti
                              19270 19296
                           1
## - earliest_cr_line_date 1
                              19272 19298
## - inq_last_6mths
                           1
                                19279 19305
## - annual_inc
                                19323 19349
                           1
## - int rate percent
                           1
                                19911 19937
## - issue date
                           1
                                20920 20946
## Step: AIC=19280.46
## default_category ~ int_rate_percent + annual_inc + verification_status +
      dti + earliest_cr_line_date + inq_last_6mths + pub_rec +
##
##
      total_acc + application_type + installment + issue_date
##
                          Df Deviance AIC
## - application_type
                           1
                                19255 19279
## - verification_status
                                19258 19280
                                19255 19281
## <none>
## - pub_rec
                              19257 19281
                           1
## - total_acc
                           1
                                19258 19282
## - installment
                           1
                               19269 19293
## - dti
                           1 19271 19295
## - earliest_cr_line_date 1
                                19273 19297
## - ing last 6mths
                           1
                                19281 19305
## - annual_inc
                           1
                                19327 19351
## - int rate percent
                           1
                                19949 19973
## - issue_date
                           1
                                20942 20966
##
## Step: AIC=19279.43
## default_category ~ int_rate_percent + annual_inc + verification_status +
##
      dti + earliest_cr_line_date + inq_last_6mths + pub_rec +
##
      total_acc + installment + issue_date
##
                          Df Deviance
                                19259 19279
## - verification_status
                                19255 19279
## <none>
## - pub_rec
                                19258 19280
                           1
## - total_acc
                           1
                                19259 19281
## - installment
                           1
                                19270 19292
## - dti
                                19271 19293
                           1
## - earliest_cr_line_date 1 19274 19296
## - inq_last_6mths
                           1 19282 19304
## - annual_inc
                                19328 19350
                           1
```

```
## - int_rate_percent
                           1
                                 19950 19972
## - issue date
                                 20945 20967
                            1
##
## Step: AIC=19279.4
## default_category ~ int_rate_percent + annual_inc + dti + earliest_cr_line_date +
       inq_last_6mths + pub_rec + total_acc + installment + issue_date
##
##
                           Df Deviance AIC
## - pub_rec
                                 19261 19279
                                 19259 19279
## <none>
## - total_acc
                                 19263 19281
                            1
                                 19276 19294
## - dti
                            1
## - installment
                            1
                                 19277 19295
## - earliest_cr_line_date 1
                                19278 19296
## - inq_last_6mths
                                19286 19304
                            1
## - annual_inc
                            1
                                 19331 19349
                            1
                                 19988 20006
## - int_rate_percent
## - issue date
                            1
                                 20987 21005
##
## Step: AIC=19279.36
## default_category ~ int_rate_percent + annual_inc + dti + earliest_cr_line_date +
       inq_last_6mths + total_acc + installment + issue_date
##
##
                           Df Deviance
## <none>
                                 19261 19279
## - total acc
                            1
                                 19265 19281
## - dti
                                 19279 19295
                            1
## - installment
                                 19280 19296
                            1
## - earliest_cr_line_date 1
                                19281 19297
## - inq_last_6mths
                            1
                               19288 19304
## - annual_inc
                            1
                                 19332 19348
## - int_rate_percent
                            1
                                 19988 20004
## - issue_date
                                 21037 21053
                            1
## Call: glm(formula = default category ~ int rate percent + annual inc +
       dti + earliest_cr_line_date + inq_last_6mths + total_acc +
##
       installment + issue_date, family = "binomial", data = lending_club_model_df.train)
##
## Coefficients:
##
            (Intercept)
                               int rate percent
                                                            annual inc
##
               3.597e+01
                                      1.285e-01
                                                            -8.181e-06
##
                     dti earliest cr line date
                                                        inq_last_6mths
##
               1.138e-02
                                      3.725e-05
                                                             9.822e-02
##
               total_acc
                                    installment
                                                            issue_date
##
               3.740e-03
                                      4.346e-04
                                                            -2.537e-03
## Degrees of Freedom: 52396 Total (i.e. Null); 52388 Residual
## Null Deviance:
                       22650
## Residual Deviance: 19260
                                AIC: 19280
#Creating matrix for Lasso
X <- model.matrix(default_category ~., data = lending_club_model_df.train)[,-1]</pre>
lending_club_model_df.train$default_category =
```

```
as.numeric(lending_club_model_df.train$default_category)
#Applying logistic regression using glmnet, which gives same result as glm
#when used with alpha = 1
fit <- glmnet(X, lending_club_model_df.train$default_category, alpha = 1,family="binomial")
#Cross validating to find best lambda which will reduce insignificant coefficients to zero
cv.out <- cv.glmnet(X, lending_club_model_df.train$default_category, alpha = 1)</pre>
bestlambda <- cv.out$lambda.min</pre>
bestlambda
## [1] 0.0008946991
#Using best lambda and fitting logistic to find optimum fit model
fit_best <- glmnet(X, lending_club_model_df.train$default_category, lambda = bestlambda)</pre>
coef(fit best)
## 110 x 1 sparse Matrix of class "dgCMatrix"
## (Intercept)
                                        3.199098e+00
## loan_amnt
                                        5.657190e-03
## int_rate_percent
                                       -5.037203e-03
## gradeB
## gradeC
                                       -4.396063e-03
## gradeD
## gradeE
                                        3.614005e-03
## gradeF
## gradeG
                                        1.679783e-02
## sub_gradeA2
                                        1.667884e-03
## sub gradeA3
                                       -2.337108e-03
## sub_gradeA4
## sub_gradeA5
## sub_gradeB1
                                        4.055671e-03
## sub gradeB2
                                       -1.527932e-03
## sub gradeB3
## sub_gradeB4
                                       -1.788586e-03
## sub_gradeB5
                                       -2.580882e-04
## sub_gradeC1
                                       -1.921257e-03
## sub_gradeC2
## sub_gradeC3
## sub_gradeC4
## sub_gradeC5
                                       -4.452849e-03
## sub_gradeD1
## sub_gradeD2
## sub_gradeD3
## sub_gradeD4
                                        2.093182e-03
## sub gradeD5
## sub_gradeE1
## sub_gradeE2
                                        1.247702e-02
## sub_gradeE3
## sub_gradeE4
                                        2.032347e-02
## sub gradeE5
## sub_gradeF1
## sub_gradeF2
## sub_gradeF3
                                        4.084290e-02
                                        1.848990e-02
## sub_gradeF4
```

```
## sub_gradeF5
                                       2.519920e-02
## sub_gradeG1
                                       6.313056e-02
## sub_gradeG2
## sub_gradeG3
## sub_gradeG4
                                      -1.707109e-02
## sub_gradeG5
## annual inc
                                      -2.347851e-07
## verification_statusSource Verified .
## verification_statusVerified
                                       1.385440e-03
## term_in_months
## dti
                                       4.672844e-04
## earliest_cr_line_date
                                       1.109377e-06
## inq_last_6mths
                                       5.735032e-03
## open_acc
                                       3.457467e-05
## pub_rec
                                      -2.408653e-03
## revol_bal
## revol_util_percent
## total_acc
## initial_list_statusw
## application_typeJOINT
## acc_now_delinq
## delinq_2yrs
## installment
                                       1.003812e-05
## addr stateAL
                                      -2.145068e-03
## addr_stateAR
                                      -5.331795e-03
## addr_stateAZ
                                      9.153944e-04
## addr_stateCA
                                       2.269143e-03
                                      -2.363550e-03
## addr_stateCO
## addr_stateCT
                                      -4.851382e-03
## addr_stateDC
## addr_stateDE
                                       1.163719e-02
## addr_stateFL
                                       8.728791e-03
## addr_stateGA
                                      -2.954301e-03
                                       1.664913e-02
## addr_stateHI
## addr_stateID
## addr_stateIL
                                      -1.854261e-03
## addr stateIN
## addr_stateKS
## addr_stateKY
## addr_stateLA
                                       8.664641e-03
## addr stateMA
                                       8.527192e-04
## addr_stateMD
                                       2.106628e-03
## addr_stateME
                                      -2.008754e-04
## addr_stateMI
## addr_stateMN
                                      -1.223701e-03
## addr_stateMO
                                      -1.154355e-03
## addr_stateMS
## addr_stateMT
                                      -1.244104e-02
## addr_stateNC
## addr_stateND
## addr_stateNE
## addr_stateNH
                                      -8.906811e-03
## addr_stateNJ
## addr_stateNM
                                       4.019218e-03
```

```
## addr stateNV
                                        5.898851e-03
                                        4.510388e-03
## addr stateNY
## addr stateOH
                                       -3.990656e-04
## addr_stateOK
                                        2.927416e-03
## addr stateOR
## addr statePA
## addr stateRI
## addr stateSC
                                       -1.592442e-02
## addr stateSD
## addr_stateTN
                                        3.199969e-03
## addr_stateTX
                                       -6.876407e-04
## addr_stateUT
## addr_stateVA
                                        1.801897e-03
## addr_stateVT
## addr_stateWA
## addr_stateWI
                                       -4.536945e-03
## addr_stateWV
                                       -6.368572e-03
## addr stateWY
                                       -7.415899e-04
                                       -1.364127e-04
## issue_date
```

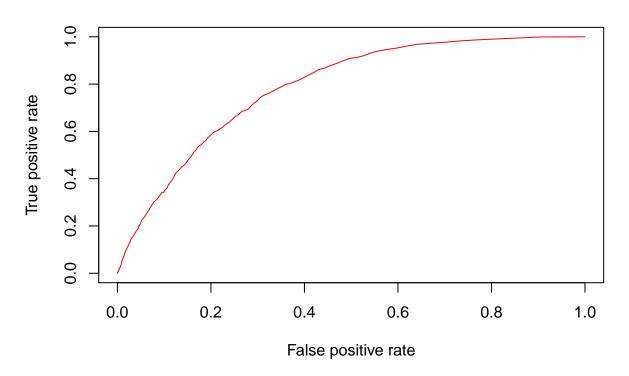
Though the model coefficients vary between backward stepwise selection model and lasso model, we are able to find the best features required for predicting default category of the loan. Depending the coefficients magnitude though we can gauge the importance of the predictors, but it wont be completely correct.

As we havent found a sufficiently satisfactory model, I would like to fit random forest to predict default category.

```
lending club model df.train$grade <- as.factor(lending club model df.train$grade)</pre>
lending club model df.test$grade <- as.factor(lending club model df.test$grade)</pre>
lending_club_model_df.train$default_category =
  as.factor(lending_club_model_df.train$default_category)
#Fitting Random Forest
rf.fit <- randomForest(default_category ~ loan_amnt +
                          int_rate_percent+grade+annual_inc+term_in_months+dti+
                          inq_last_6mths+revol_util_percent+total_acc+issue_date+
                      installment+earliest_cr_line_date,
                        data = lending_club_model_df.train)
#Predicting using random forest model
rf.probs <- predict(rf.fit, newdata = lending_club_model_df.test)</pre>
#Calculating Accuracy using confusion matrix
confmatrix_rf_new<-table(rf.probs,lending_club_model_df.test$default_category)</pre>
confmatrix_rf_new
## rf.probs
                0
                       1
##
          1 21192 1253
##
                8
sum(diag(confmatrix_rf_new))/sum(confmatrix_rf_new)
## [1] 0.9438482
#Plotting performance of model using ROC curve
probRF <- predict(rf.fit, newdata = lending_club_model_df.test, type='prob')</pre>
```

```
predRF <- prediction(probRF[,2],lending_club_model_df.test$default_category)
perfRF <- performance(predRF, measure = "tpr", x.measure = "fpr")
plot(perfRF, col=rainbow(5),main = "ROC for Random Forest")</pre>
```

ROC for Random Forest

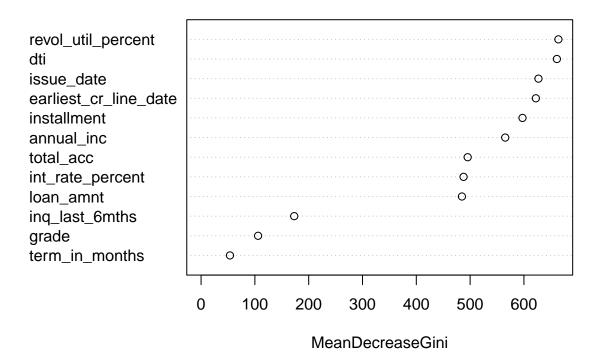


#Finding importance of variables in the model importance(rf.fit)

```
##
                         MeanDecreaseGini
## loan_amnt
                                484.79778
## int_rate_percent
                                487.79333
## grade
                                105.98319
## annual inc
                                565.24821
## term_in_months
                                 53.71374
                                 661.23778
## dti
## inq_last_6mths
                                173.10591
## revol_util_percent
                                664.02851
## total_acc
                                 495.46609
## issue_date
                                 626.97326
## installment
                                597.32102
## earliest_cr_line_date
                                622.16026
```

#Plotting importance of variables in the model
varImpPlot(rf.fit,main = "Variable Importance")

Variable Importance



From the model generated by fitting random forest, the accuracy of the predictions is quite comparable to the Logistic model but performance of this model is far better. This can be seen in the graphic as the ROC curve covers larger area. Moving on to the importance of the predictors, the top five predictors according to variable importance plot based on the random forest model are revol_util_percent, dti, issue_date, earliest_cr_line_date and installment.

- 6. Expain Logistic Regression to:
- a. someone with significant mathematical experience

The outcomes of many of the experiments/research are qualitative or categorical and they can be predicted or categorized into classes using methods like Logistic Regression. Thus logistic regression is used to predict a variable which has discrete values and is not continuous. Logistic regression approach calculates the probability of each of the categories of the response variable. This probability is then used to categorize the response variable Y. The function used to predict qualitative variables has to have outputs between 0 and 1. Thus we use logistic function,

$$p(X) = e^{\beta 0 + \beta 1 * X} / 1 + e^{\beta 0 + \beta 1 * X}$$

 $\beta 0$ and $\beta 1$ are the unknown coefficients. To evaluate these coefficients we can estimate based on available training data using methods like Maximum likelihood. The idea behind finding estimates is that we find estimates for $\beta 0$ and $\beta 1$ such that the predicted probability $p(x_i)$ is as close indicative of the class that the response belongs to. For example, if we consider a scenario where we are predicting a default on a loan payment as in the above examples. The estimates calculated for $\beta 0$ and $\beta 1$ once put in above equation should give a response

closer to 1 for defaultors and close to 0 for individuals who did not default. The maximum likelihood function used to evaluate $\beta 0$ and $\beta 1$ is as below:

$$l(\beta 0, \beta 1) = \pi_{i,j=1} p(x_i) * \pi_{i',j'=0} p(1 - x_{i'})$$

The $\beta 0$ and $\beta 1$ are calculated by maximizing the above function. Once the estimates are calculated, we an use them to classify new test observations by calculating the p(X).

Logistic function will always produce an S shaped curve which would swiftly move from one category represented by 0 to another category represented by 1 for bimodal categorical variables. Some manipulation of logistic function leads to below formula:

$$p(X)/1 - p(X) = e^{\beta 0 + \beta 1 * X}$$

The equation on the left hand side is called the odds and they can range from 0 to infinity. From the above example odd close to 0 indicate lwould mean ow probability of default and high probability of default for odds nearing infinity. Another important concept to know about logistic regression is that log-odds are linear in X. Log-odds is also known as logit.

$$log(p(X)/1 - p(X)) = \beta 0 + \beta 1 * X$$

Thus interpreting the above result we can say that a unit change in X causes the log odds to change by $\beta 1$. Thus in conclusion we can say that there is no linear relationship between p(X) and X. An increase or decrease in X will cause p(X) to increase or decrease depending on the sign of $\beta 1$.

b. someone with little mathematical experience.

As one starts with a research project, there are number of instances when the response variable is qualitative or categorical. The prediction of qualitative response variable involves segreagating responses into different classes and this is achieved by many different methods of which one is logistic regression. For the basis of classification, logistic regression predicts the probability of each of the categories of a qualitative variable. A simple example of classification which can be solved using logistic regression is of classifying if the email recieved by a person is a spam or not. To classify this email, we use the data from previous emails as training observations. The data that can be useful could like the subject line, specific words in email, domain of email sender, etc. Using this data a model is developed which has an output between 0 and 1. Lets assume according to our model we considered 0 as no spam and 1 as spam. Using any new email as a test observation, if the model outputs a value greater than 0.5, we can classify the email as spam or else not a spam. Logistic regression can be applied to classify response variables where there are more than two classes, though in industry some of the other methods like discriminant analysis are preferred.