

## INTRODUCTION TO DIGITAL IMAGE REPRESENTATION

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### \* Digital image representation :-

- An image may be defined as two dimensional function  $f(x, y)$  where  $x$  and  $y$  are spatial co-ordinates and  $f$  is the intensity (amplitude) at any pair of co-ordinates  $x, y$ .

- The term gray scale or gray level is used to refer to the intensity of monochrome images.

- An image may be continuous with respect to the  $x$  and  $y$  co-ordinates and also in amplitude.

- To convert such image into digital form needs to convert co-ordinates as well as intensity of image.

- Digitalizing the co-ordinates value is called sampling and digitalizing amplitude value is called as quantization.

- Thus, when  $x, y$  and amplitude values of  $f$  are finite, discrete, continuous then we call the image a digital image.

### \* Co-ordinate Conventions :-

- The result of sampling and quantization is a matrix of real numbers.

- Assume that an image  $f(x, y)$  is sampled so that resulting image has  $m$  rows and  $N$  columns.

- We can say that the image is of size  $M \times N$ . The co-ordinates convention is used in the image processing toolbox is given below.

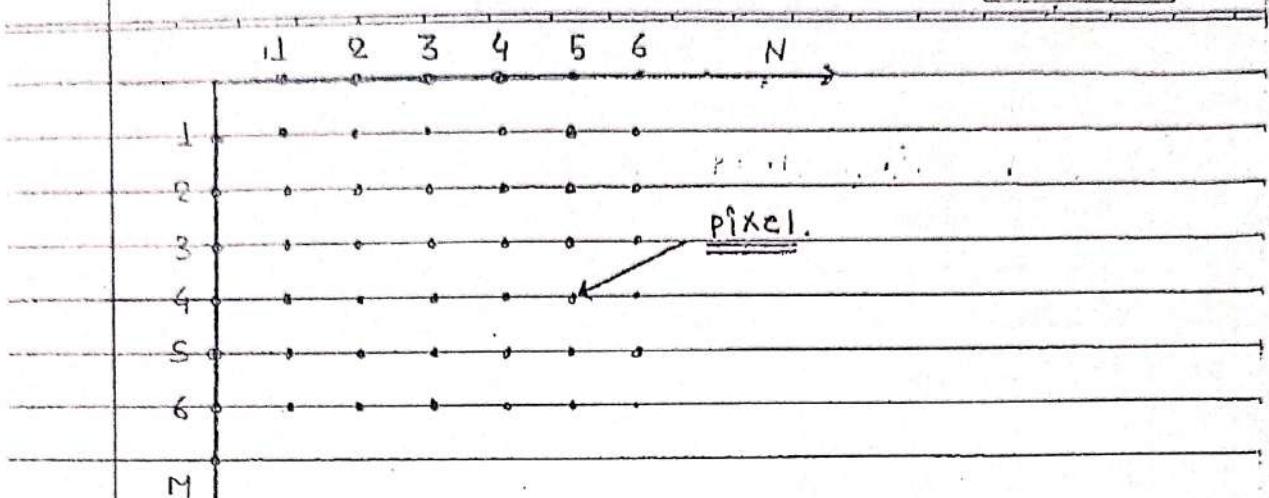


fig :- Co-ordinate conversions used in matlab toolbox.

- The co-ordinate system in above figure represents a matlab matrix as.

	$f(1,1)$	$f(1,2)$	-----	$f(1,n)$	
	$f(2,1)$	$f(2,2)$	-----	$f(2,n)$	
$f =$	$f(3,1)$	$f(3,2)$	-----	$f(3,n)$	
		⋮			
		$f(m,1)$	$f(m,2)$	-----	$f(M,N)$

- Matrix in matlab are stored in variables with names such as a, f, g, h etc.

- Variables must begin with a letter and may contain only letters, numerals and underscores.

## \* Reading , Writing and displaying Images :-

### 1) Reading Images :-

- Images are read into matlab environment using function imread.
- The syntax of imread is  
imread ('filename');
- Here filename is the string containing the complete name of the image file containing extension.

EX :-

>> f = imread ('coins.png');

- Reads the png file into image array f. The semicolon at the end of the statement is used for suppressing the output.

- If a Semicolon is not used, matlab displays the result of operation on screen.

- Following are some of the image graphics formats supported by imread and imwrite.

<u>Format name</u>	<u>Description</u>	<u>Recognized extensions</u>
TIFF	Tagged Image file format	.tif, .tiff,
JPEG	Joint Photographic Experts Group.	.jpg, .jpeg,
PNG	Portable Network Graphics.	.png,
BMP	Bitmap Picture	.bmp,

- Function size gives the row and column dimensions of an image.

Ex :

```
>> size (f)
    246 300
>> [R, C] = size (f)
    R = 246
    C = 300.
```

### 2) Writing Images :-

- Images are written onto the disk using function imwrite.

- The basic syntax of imwrite is:  
imwrite (f, 'filename');

- Where f is the image array containing the filename to be copied and file name specifies the destination file name.

- By using imwrite function, you may change the format of source file.

Ex :

```
>> f = imread ('coins.png');
>> imwrite (f, 'mycoins.jpg');
>> imfinfo coins.png
>> imfinfo mycoins.jpg
```

### 3) Displaying Images :-

- Images are displayed on the matlab desktop using function imshow, which has the basic syntax :-

```
imshow (f, g)
```

- Where  $f$  is an image array and  $G_1$  is the number of intensity levels used to display it.
  - If  $G_1$  is omitted, it defaults to 256
- using syntax :

`imshow(f, [low, high])`

- displays all values less than low as blank and all values greater than high as white.
- The values in between are displayed as intermediate intensity values using the default gray levels.

- Finally, the syntax `imshow(f, [])` sets the variable low to the minimum value of array  $f$  and high to the maximum value of  $f$ .

- This form of `imshow` is useful for displaying images that have a low dynamic range.

Ex :

```
>> f = imread('rice.png');
>> imshow(f)
>> imshow(f, [80, 150])
>> imshow(f, [])
>> imshow(f), figure, imshow(f, [80, 150]);
    figure, imshow(f, []);
```

Ox

```
>> f = imread('rice.png');
>> subplot(1, 3, 1), imshow(f), ;
>> subplot(1, 3, 2), imshow(f, [80, 150])
>> subplot(1, 3, 3), imshow(f, []);
```

## \* Data classes and Image types :-

### Data classes :-

- matlab supports 10 data classes that are listed in the following table.

Data class	Description.
double	<ul style="list-style-type: none"> <li>- It is a double precision floating point numbers whose approximate range is <math>10^{-308}</math> to <math>10^{307}</math>.</li> <li>- This data class assigns 8 bytes per element.</li> </ul>
uint8	<ul style="list-style-type: none"> <li>- It is a unsigned 8 bit integer with range [0, 255]. It allocate 1 byte per element. The default dataclass of an image is uint8.</li> </ul>
uint16	<ul style="list-style-type: none"> <li>- It is unsigned 16 bit integers with range [0, 65535]. It allocate 2 bytes per element.</li> </ul>
uint32	<ul style="list-style-type: none"> <li>- Unsigned 32 bit integers in range [0, 4294967295]. It allocate 4 bytes per element.</li> </ul>
int8	<ul style="list-style-type: none"> <li>- It is signed 8 bit integers in the range [-128, 127]. It assign 1 byte per element.</li> </ul>

int16	- It is signed 16 bit integers in the range [-32768, 32767]. It assigns 2 bytes per element.
int32	- It is signed 32 bit integers in the range [-2147483648, 2147483647]. It assigns 4 bytes per element.
single	- It is single precision floating point numbers with values in approximate range $10^{-38}$ to $10^{37}$ . It assigns 4 byte per element.
logical	- This data class allows logical 0's or logical 1's. It assigns 1 byte per element.
char.	- It is a character datatype allocating 2 bytes per element.

Examples :-

① double :-

$$a = [12.56 \ -19; \ 4.5 \ 98]$$

$$a = \begin{matrix} 12.5600 & -19.0000 \\ 4.5000 & 98.0000 \end{matrix}$$

② uint8 :-

$$b = \text{uint8}([100 \ 908; \ -25 \ 150])$$

$$b = \begin{matrix} 100 & 255 \\ 0 & 150 \end{matrix}$$

(3) uint16 :-

$$c = \text{uint16}([-10000 \ 98; -250 \ 15.70])$$

$$c = 10000 \ 98$$

$$0 \ 16.$$

(4) uint32 :-

$$d = \text{uint32}([-80 \ 12.11; 500 \ 25000])$$

$$d = 0 \ 12$$

$$500 \ 25000.$$

(5) Single :-

$$e = \text{single}([-45 \ 9.8; 122 \ 1000])$$

$$e = -0.0045 \ 0.0010$$

$$0.0122 \ 1.0000$$

(6) int8 :-

$$f = \text{int8}([-100 \ 908; -30 \ 19.14])$$

$$f = 100 \ 127$$

$$-30 \ 19.$$

(7) int16 :-

$$g = \text{int16}([-10000 \ 98; -250 \ 15.70])$$

$$g = 10000 \ 98$$

$$-250 \ 16.$$

(8) int32 :-

$$h = \text{int32}([879 \ 6894; 50.34 \ 1870])$$

$$h = 879 \ 6894$$

$$50 \ 1870.$$

(i) logical :-

T = logical ([ 25 0 -4 ; 1 7.8 5 ])

T = | 0 |

| | | .

(ii) char :-

T = char ( ' COCSIT' )

T = COCSIT ..

## \* Image types :-

- The matlab toolbox supports four types of images:

- 1) Intensity Images.
- 2) Binary Images.
- 3) RGB Images.
- 4) Indexed Images.

### 1) Intensity Images :-

- An intensity image is a data matrix whose values have been scaled to represent intensities.

- When the elements of an intensity image are of data class uint8 or uint16, they have intensity values in the range [0, 255] or [0, 65535] respectively.

- If the image is of class double, the values are floating point numbers in the range [0, 1].

### 2) Binary Images :

- Binary Images have a very specific meaning in matlab.

- A binary image is a logical array of 0's and 1's.

- Thus a binary image is of data class logical.

- You can use 'logical' function to convert any numeric array to logical array.

- If 'A' contains elements other than 0's and 1's, the 'logical' function can be used to convert 'A' to logical array.

### 3) RGB Images :-

- An RGB is a  $m \times n \times 3$  array of color pixels, where each color pixel is a triplet corresponding to the Red, Green and blue components of an RGB image at a specific location.

- The three images forming RGB color image are referred to as the Red, Green and blue component images.

- The dataclass of the component images determines their range of values.

- A typical representation of pixels of RGB image is shown in following figure.

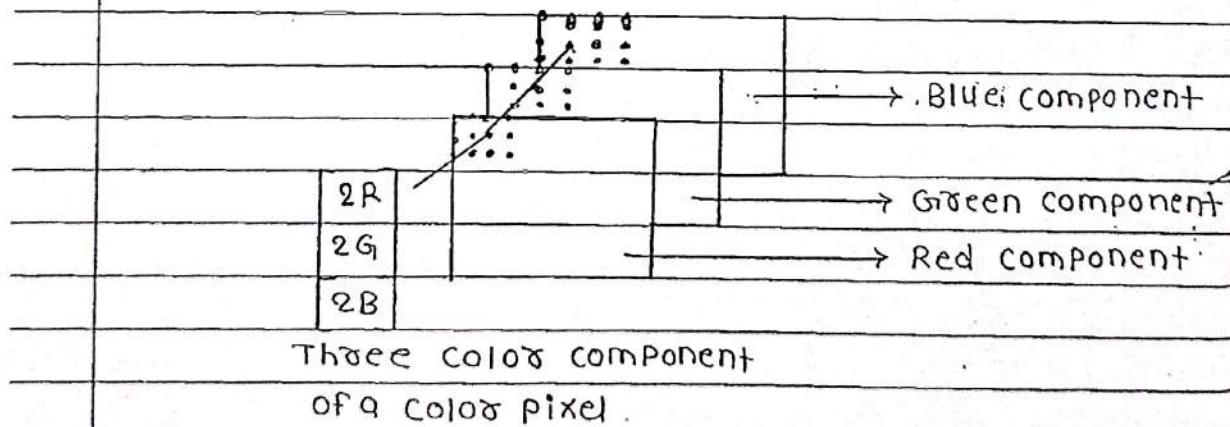


fig : A typical representation of RGB images.

#### 4) Indexed Images :

- An indexed image has two components - A data matrix of integers ('X') and a color map matrix ('map').
- A matrix map is ~~my~~ 3 array of class double containing floating point values in the range 0-1.
- The length 'm' of the map is equal to the number of colors it defines.
- The color of each pixel is determined by using the corresponding values of integer matrix 'X'.

#### \* Practice :

##### % Study of Image Types :

```
>> f = imread('cameraman.png');
>> g = imread('paper.png');
>> h = imread('coins.png');
>> subplot(1, 3, 1), imshow(f)
>> subplot(1, 3, 2), imshow(g)
>> subplot(1, 3, 3), imshow(h)
```

## \* Converting between Data classes and Image Types :

### \* Data classes:

- The toolbox provides specific functions that perform the scaling necessary to convert both image types & data classes.

- To change the data class of any array the syntax is

`B = datatype(a)`

- where a is a variable of any data class and datatype represent the type in which conversion is to be done.

For ex :

`>> a = [-20 10 ; 28.2 40]`

`>> b = uint8(a)`

$$\begin{array}{cc} -20 & 10 \\ 28.2 & 40 \end{array} \quad b = \begin{array}{cc} 0 & 10 \\ 28 & 40 \end{array}$$

`>> c = logical(a)`

$$c = \begin{array}{cc} 1 & 1 \\ 1 & 1 \end{array}$$

## \* Converting between Image Types :

- The IPT (Image Processing Toolbox) in matlab provides following functions for converting b/w image types.

<u>Function Name</u>	<u>Converts input to</u>	<u>valid input image dataclass</u>
im2uint8	uint8	logical , uint8 , uint16 , double .
im2uint16	uint16	uint8 , logical , uint16 , double .
im2double	double	logical , uint8 , uint16 , double .
mat2gray	double([0,1])	double
im2bw	logical	uint8 , uint16 , logical .

I> im2uint8 :

- Function im2uint8 converts an input to uint8 .

- If the input is already of uint8 dataclass , this function returns the same result.

Ex :

```
>> f = imread ('coin.png')
>> g = im2uint8 (f)
>> imshow (f, [ ]) , figure , imshow (g, [ ])
```

e> im2uint16 :

- Function im2uint16 converts an input to uint16 data class.

- values in the output image

are in range [0, 65535].

- If the input is same class no changes are done.

Ex :

```
>> f = imread('rice.png');
```

```
>> g = im2uint16(f);
```

```
>> imshow(f,[ ]); figure, imshow(g,[ ]);
```

s> im2double :

- Function im2double converts an input to class double.

- The values in the output image are adjusted in the range [0,1].

Ex :

```
>> f = imread('rice.png');
```

```
>> g = im2double(f);
```

```
>> imshow(g)
```

u> mat2gray :

An arbitrary array of class double can be converted to class double scaled in the range [0,1] can be accomplished with the function mat2gray.

- The basic syntax of mat2gray is  $\theta =$

```
g = mat2gray(f, [fmin fmax]);
```

- where g is the output image whose values are scaled in the range [0,1].

- The parameters  $f_{\min}$  and  $f_{\max}$  are such that values less than  $f_{\min}$  in  $f$  because 0 in  $g$  and values

ex :

```
>>> f = imread('rice.png');
>> g = matgray(f);
>> imshow(g)
```

s> im2bw:

- Finally the function `im2bw` produces a binary image from an intensity image.

- The syntax is

```
g = im2bw(f, T);
```

- where  $T$  is the threshold value.

- The output image  $g$  has values 0 for all pixels with intensity values less than  $T$  and values 1 for all other pixels.

- Thus the output image will have either 0 or 1 value.

- The default value of  $T$  is

0.5.

Ex :

```
>> f = imread('rice.png');
>> g = im2bw(f);
>> imshow(g)
>> g = im2bw(f, 0.4);
>> imshow(g)
>> g = im2bw(f, 0.7);
>> imshow(g)
```

## \* Introduction to m-function Programming :

- In matlab m-files are created using a texteditor and are saved with a name in form 'filename.m'. such as multi.m or sumprod.m.

- m-functions are also written in texteditors and follow some rules like functions should start with a keyword function and should be saved with function name.

- Following are the components of m-function file.

- 1> The function defn line.
- 2> The H1 line.
- 3> Help Text.
- 4> Function body
- 5> Comments.

### 1> The function defn line :

- The function defn line has the form.

function [output] = functionname ( inputs )

Ex :

function [x,y] = sumprod ( a,b )

- where a, b are the inputs.

- x is used to store sum of (a and b) while y is used to store product of a and b.

- The function defn line should always start with keyword function.

## 2) The H1 Line :

- The H1 line is the first textline.  
- It is a single comment line  
that immediately follows the function defn  
line.

- Blank lines are not allowed  
in both H1 line and function defn line

## 3) Help Text :

- The help text is a text block  
that follows the H1 line without any blank  
lines in between.

- Help text is used to provide  
comments and online help for the function.

- When the user types

`>> help functionname` at the command prompt  
matlab displays all comment lines that appear  
after function defn line.

## 4) Function Body :

- The function body contains  
all the matlab statements that perform  
computation and assigns value to the output  
variable.

## 5) Comments :

- Comments are the lines  
preceded by % which can be added at the  
end of the m-function file.

Ex :-

```
function [x,y] = sumprod(a,b)
% Function to compute sum and product.
% (Multiple comments):
%
x = a+b;
y = a*b;
disp(x)
disp(y)
```

Note :- Save this m-function with name sumprod.

## \* Operators in matlab :-

- matlab operators are grouped into three main categories.

- 1) Arithmetic operators.
- 2) Relational operators
- 3) Logical operators.

### 1) Arithmetic Operators :-

- matlab has two different types of arithmetic operations - matrix arithmetic operation and

- matrix operations are done by following the rules of linear algebra while array operations are done on an element by element basis.

- The dot operator distinguishes array operations from matrix operations.

Ex :

$a*b$  is a matrix multiplication.

$a.*b$  is a array multiplication.

- Following table lists array and matrix arithmetic operators.

Operator	Name	matlab function	Example
+	Array & matrix add	PLUS (a,b)	$\gg c = a+b ; \underline{\underline{o}}$ $\gg c = PLUS(a,b)$
-	Array & matrix sub. fraction	minus (a,b)	$\gg c = a-b ; \underline{\underline{o}}$ $\gg c = minus(a,b)$
.*	Array multiplication	times (a,b)	$\gg c = a.*b ; \underline{\underline{o}}$ $\gg c = times(a,b)$
*	matrix multiplication	mtimes (a,b)	$\gg c = a*b ; \underline{\underline{o}}$ $\gg c = mtimes(a,b)$
.\	Array right division	divide (a,b)	$\gg c = a.\backslash b ; \underline{\underline{o}}$ $\gg c = divide(a,b)$
\	Array left division	ldivide (a,b)	$\gg c = a.\backslash b ; \underline{\underline{o}}$ $\gg c = ldivide(a,b)$