

# 1 Enumerating Arrangements of $k$ items from $n$ objects.

Tips for solving: Look at the simplest cases and try to work out the pseudo code for a recursive algorithm. Some of the functions defined can give clues as to what is to be done.

1 /\* Consider all arrangements of  $k$  items  
2 from  $n$  objects. For  $n=3, k=2$ , they  
3 are 12, 21, 13, 31, 23, 32. The number  
4 of such arrangements is  
5  $nP_k = n(n-1) \cdots (n-k+2)(n-k+1)$ .  
6 Below is a program which when given  $n, k$   
7 as input, prints all arrangements of  $k$   
8 items from  $n$  objects. \*/

9 #include <stdio.h>  
10 #include <stdlib.h>  
11 #include <stdbool.h>  
12 typedef int\*\* PermList;  
13  
14 int count\_arrangements(int n, int k) {  
15 // Problem 1 a.) write a recursive  
16 // function logic here in one line to  
17 // compute the number of all arrangements  
18 // of  $k$  items from  $n$  objects. (2 marks)  
19 }

20  
21 PermList create\_perm\_list(int n,  
22 int k) {  
23 int fn = count\_arrangements(n, k);  
24 PermList pl = malloc(fn \* sizeof(int \*));  
25 for(int i = 0; i < fn; i++) {  
26 pl[i] = malloc(n \* sizeof(int));  
27 }  
28 return pl;  
29 }

30 void destroy\_perm\_list(PermList pl,  
31 int n, int k) {  
32 int fn = count\_arrangements(n, k);  
33 for (int i = 0; i < fn; i++) {  
34 free(pl[i]);  
35 }  
36 free(pl);  
37 }

38 // given a 'small\_row' of size 'size'  
39 // copies it to 'big\_row' which has size  
40 // 'size+1'. Also sets the last position  
41 // in 'big\_row' to 'e'

42 void insert\_and\_copy(int\* small\_row, int size,  
43 int e, int\* big\_row) {  
44 for (int i = 0; i < size; i++) {  
45 big\_row[i] = small\_row[i];  
46 }  
47 big\_row[size] = e;  
48 }

51 // checks if 'e' is in the 'row' of size 'size'  
52 bool find(int e, int\* row, int size) {  
53 for(int i = 0; i < size; i++) {  
54 if (row[i] == e) {  
55 return true;  
56 }  
57 }  
58 return false;  
59 }

60 // find the numbers from {1,...,n}  
61 // that are not in 'row' which is of size 'k'  
62 // and puts them in 'elements'  
63 void find\_elements\_not\_in\_row(int\* row, int n,  
64 int k,  
65 int\* elements) {  
66 int c = 0;  
67 for (int i = 0; i < n; i++) {  
68 if (find(i+1, row, k) == false) {  
69 elements[c++] = i+1;  
70 }  
71 }  
72 }

73  
74 PermList enumerate\_arrangements(  
75 int n, int k) {  
76 PermList B = create\_perm\_list(n, k);  
77 if (k == 1) {  
78 // Problem 1 b.) write code here for base  
79 // case of recursively building list 'B'  
80 // of all arrangements of  $k=1$  items  
81 // from {1,...,n}. (3 marks)  
82 } else {  
83 // Problem 1 c.) write code here for  
84 // recursively building list 'B' of all  
85 // arrangements of  $k$  items from  
86 // {1,...,n}. (5 marks)  
87 }  
88 return B;  
89 }

90 void print\_perm\_list(PermList pl,  
91 int n, int k) {  
92 int fn = count\_arrangements(n, k);  
93 for(int i = 0; i < fn; i++) {  
94 for (int j = 0; j < k; j++) {  
95 printf("%d ", pl[i][j]);  
96 }  
97 printf("\n");  
98 }  
99 }

100  
101 int main() {  
102 int n = 10;  
103 int k = 5;  
104 print\_perm\_list(  
105 enumerate\_arrangements(n, k), n, k);  
106 return 0;  
107 }

## 2 Banking on Structs

```
1  /* Build a program for managing a bank.
2   There should be a database of bank
3   accounts and transactions. We should
4   be able to add new accounts,
5   new transactions (credit/debit) and
6   compute the balance of a account */
7  #include <stdio.h>
8  #include <string.h>
9
10 typedef enum AccountType {
11     Savings,
12     Current
13 } AccountType;
14
15 typedef enum TransactionType {
16     Credit,
17     Debit
18 } TransactionType;
19
20 typedef struct Transaction {
21     TransactionType type;
22     struct BankAccount* account;
23     int amount;
24 } Transaction;
25
26 typedef struct BankAccount {
27     char name[100];
28     int pin;
29     AccountType type;
30     // passbook is an array of transactions
31     // pointers to avoid taking too much memory
32     struct Transaction* passbook[1000];
33     int transactions_count;
34 } BankAccount;
35
36 typedef struct BankDatabase {
37     BankAccount accounts[1000];
38     Transaction transactions[10000];
39     int accounts_count;
40     int transactions_count;
41 } BankDatabase;
42
43 // compute the total amount of money
44 // with the bank amoung all the accounts
45 int compute_money_with_bank(
46     BankDatabase* db) {
47     int sum = 0;
48     for(int i = 0;
49         i < db->transactions_count; i++) {
50         switch(db->transactions[i].type) {
51             case Credit:
52                 sum += db->transactions[i].amount;
53                 break;
54             case Debit:
55                 sum -= db->transactions[i].amount;
56                 break;
57         }
58     }
59     return sum;
60 }
```

```
61 int compute_balance(BankAccount* acc) {
62     // Problem 2 a.) fill in the code to
63     // find the balance of the account
64     // 'acc'. (3 marks)
65 }
66
67 BankAccount* add_bank_account(char* name,
68     int pin, AccountType type,
69     BankDatabase* db) {
70     // Problem 2 b.) fill in the code to add
71     // a new account 'acc' to the bank
72     // database 'db'. The function should
73     // also return a pointer to the bank
74     // account created in 'db'. (3 marks)
75 }
76
77 Transaction* add_transaction(
78     TransactionType type,
79     BankAccount *account,
80     int amount, BankDatabase* db) {
81     // Problem 2 c.) Fill in the code for
82     // adding a transaction to the system.
83     // The logic should be written such
84     // that the all the other functions in
85     // this program continue to work
86     // correctly. (6 marks)
87 }
88
89 int main() {
90
91     BankDatabase db;
92     db.accounts_count = db.transactions_count = 0;
93     BankAccount acc = { .pin = 1234,
94         .transactions_count = 0};
95     strcpy(acc.name, "Ivan");
96     BankAccount* acc_ptr = add_bank_account(
97         acc.name, acc.pin, acc.type, &db);
98     add_transaction(Credit, acc_ptr, 10000, &db);
99     add_transaction(Debit, acc_ptr, 2000, &db);
100    add_transaction(Credit, acc_ptr, 5000, &db);
101
102    // should print 13000
103    printf("Account balance is %d\n",
104        compute_balance(acc_ptr));
105
106    BankAccount acc2 = { .pin = 6897,
107        .transactions_count = 0};
108    strcpy(acc2.name, "Jake");
109    BankAccount* acc_ptr2 = add_bank_account(
110        acc2.name, acc2.pin, acc2.type, &db);
111    add_transaction(Credit, acc_ptr2, 100000, &db);
112    add_transaction(Debit, acc_ptr2, 20000, &db);
113    add_transaction(Credit, acc_ptr2, 50000, &db);
114
115    // should print 130000
116    printf("Account balance is %d\n",
117        compute_balance(acc_ptr2));
118
119    // should print 143000
120    printf("Total Money with bank is %d\n",
121        compute_money_with_bank(&db));
122 }
123
124
125
126
```