

HW #2 of OPERATING SYSTEMS

Spring 2025

Name: VAISHAK BALACHANDRA (021) (0037831852)

1. Using Banker's Algorithm for deadlock avoidance in the following example:

5 processes P_0 through P_4 ;

3 resource types:

A (10 instances), B (5 instances), and C (7 instances)

Snapshot at time T_0 :

	Allocation	Max	Available
	A B C	A B C	A B C
P_0	0 1 0	7 5 3	3 3 2
P_1	2 0 0	3 2 2	
P_2	3 0 2	9 0 2	
P_3	2 1 1	2 2 2	
P_4	0 0 2	4 3 3	

1.1) Exam at time T_0 whether the system is in a safe state or not.

To examine, whether system is in a safe state or not, we need first

Need matrix := $(0 \ 1 \ 0) + (2 \ 0 \ 0) + (3 \ 0 \ 2) + (2 \ 1 \ 1) + (0 \ 0 \ 2) =$

$$\boxed{\text{Need} = \text{Max} - \text{Allocation.}}$$

	Allocation			Max			Need			Available		
	A	B	C	A	B	C	A	B	C	A	B	C
P_0	0	1	0	7	5	3	7	4	3	3	3	2
P_1	2	0	0	3	2	2	1	2	2			
P_2	3	0	2	9	0	2	6	0	0			
P_3	2	1	1	2	2	2	0	1	1			
P_4	0	0	2	4	3	3	4	3	1			

Available
resources,

$A = 3$

$B = 3$

$C = 2$

Step 1: Initialize : work = (3 3 2)

finish [i] = False [i = 0, 1, 2, 3, 4]

Step 2 & 3:check Request \leq NeedRequest \leq Available

(150)

$P_0: (7, 4, 3) \not\leq (3, 3, 2) \Rightarrow$ Need to wait!
 $\text{finish}[0] = \text{false}.$

$P_1: (1, 2, 2) \leq (3, 3, 2) \Rightarrow$ Update work
 $\text{work} = (3, 3, 2) + (1, 2, 2) \Rightarrow (5, 3, 2)$ ✓
 $\text{finish}[1] = \text{true}$

$P_2: (6, 0, 0) \not\leq (5, 3, 2) \Rightarrow$ Need to wait!
 $\text{finish}[2] = \text{false}$

$P_3: (0, 1, 1) \leq (5, 3, 2) \Rightarrow$ update work
 $\text{work} = (5, 3, 2) + (0, 1, 1) \Rightarrow (7, 4, 3)$ ✓
 $\text{finish}[3] = \text{true}$

$P_4: (4, 3, 1) \leq (7, 4, 3) \Rightarrow$ update work
 $\text{work} = (7, 4, 3) + (0, 0, 2) \Rightarrow (7, 4, 5)$ ✓
 $\text{finish}[4] = \text{true}$

$P_0: (7, 4, 3) \leq (7, 4, 5) \Rightarrow$ Update work
 $\text{work} = (7, 4, 5) + (0, 1, 0) \Rightarrow (7, 5, 5)$ ✓
 $\text{finish}[0] = \text{true}$

$P_2: (6, 0, 0) \leq (7, 5, 5) \Rightarrow$ update work
 $\text{work} = (7, 5, 5) + (3, 0, 2) \Rightarrow (10, 5, 7)$ ✓
 $\text{finish}[2] = \text{true}$

System Sequence: $[P_1 \rightarrow P_3 \rightarrow P_4 \rightarrow P_0 \rightarrow P_2]$

\therefore The system is in Safe state !!

1.2) Can request for (1,0,2) by P_1 be granted?

To check, if P_1 's request can be granted \rightarrow it need to

- check if request exceeds P_1 's Need or not.
- check if there are enough Available resources or not.
- check if granting request leaves system in safe state or not.

Here, Request = (1, 0, 2) | Available = (3, 3, 2)
For P_1 :- Need $_{P_1}$ = (1, 2, 2)

i) Here $(1, 0, 2) \leq (1, 2, 2)$ i.e. Request \leq Need $_{P_1}$

Thus request is less than or equal to Need of $P_1 \Rightarrow$ Good \checkmark

ii) Here $(1, 0, 2) \leq (3, 3, 2)$ i.e. Request \leq Available.

Thus request is less than or equal to Available at that time to \Rightarrow Good \checkmark

iii) Update Data Structure

new-Available = Available - Request = (3 3 2) - (1 0 2)

$\boxed{\text{new-available} = (2 \ 3 \ 0)}$

new-Allocation $_{P_1}$ = Allocation $_{P_1}$ + Request = (2 0 0) + (1 0 2)

$\boxed{\text{new-allocation}_{P_1} = (3 \ 0 \ 2)}$

new-Need $_{P_1}$ = Need $_{P_1}$ - Request = (1 2 2) - (1 0 2)

$\boxed{\text{New-Need}_{P_1} = (0, 2, 0)}$

Initialize : work = new-available = (2 3 0)
finish[i] = False, $i = 0, 1, 2, 3, 4$.

Repeat ; check request \leq Need
 request \leq Available.

P₀: $(7, 4, 3) \not\leq (2, 3, 0) \Rightarrow$ Need to wait!!
finish[0] = false.

P₁: $(0, 2, 0) \leq (2, 3, 0) \Rightarrow$ update work P₁ ✓
work = $(2, 3, 0) + (0, 2, 0) \Rightarrow (5, 3, 2)$
finish[1] = true.

P₂: $(0, 0, 0) \not\leq (5, 3, 2) \Rightarrow$ Need to wait!!
finish[2] = false.

P₃: $(0, 1, 1) \leq (5, 3, 2) \Rightarrow$ update work P₃ ✓
work = $(5, 3, 2) + (0, 1, 1) \Rightarrow (7, 4, 3)$
finish[3] = true.

P₄: $(4, 3, 1) \leq (7, 4, 3) \Rightarrow$ update work P₄ ✓
work = $(7, 4, 3) + (0, 0, 2) \Rightarrow (7, 4, 5)$
finish[4] = true.

P₀: $(7, 4, 3) \leq (7, 4, 5) \Rightarrow$ update work P₀ ✓
work = $(7, 4, 5) + (0, 1, 0) \Rightarrow (7, 5, 5)$
finish[0] = true.

P₂: $(6, 2, 0) \leq (7, 5, 5) \Rightarrow$ update work P₂ ✓
work = $(7, 5, 5) + (3, 0, 2) \Rightarrow (10, 5, 7)$
finish[2] = true.

System Sequence: $[P_1 \rightarrow P_3 \rightarrow P_4 \rightarrow P_0 \rightarrow P_2]$

Thus still system is in safe state!!

\Rightarrow Thus satisfies all 3 cases.

\therefore Request of $(1, 0, 2)$ for P₁ can
be granted !!

2. Reference String:

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1 9 8 3

Using diagram to show the step-by-step page replacement processing of the following, indicate each page fault and count the total page fault numbers:

1) Frame number = 3; Using a queue and a pointer to implement the FIFO algorithm.

pages frames	7	0	1	2	0	3	0	4	2	3	0	3	2	1	2	0	1	7	0	1	9	8	3
f ₁	7	7	7	2	2	2	2	4	4	4	0	0	0	0	0	0	0	7	7	7	9	9	9
f ₂		0	0	0	0	3	3	3	2	2	2	2	2	1	1	1	1	0	0	0	8	8	8
f ₃			1	1	1	0	0	0	3	3	3	3	3	2	2	2	2	2	1	1	1	3	3
hit(x)/miss(x)	X	X	X	X	✓	X	X	X	X	X	X	✓	✓	X	X	✓	✓	X	X	X	X	X	X

Here,

X → Page Fault/
Miss

✓ → Page Hit

$$\begin{aligned} \# \text{ Faults/Miss} &= 18 \Rightarrow \text{Miss rate/ratio} = 18/23 = 0.7826 // \\ \# \text{ Hits} &= 5 \Rightarrow \text{Hit rate/ratio} = 5/23 = 0.21739 // \\ \text{Total} &= 23 \end{aligned}$$

[* Used pointer (→) to indicate next Hit.]

2) Frame number = 5; Using a stack to implement the LRU algorithm.

pages frames	7	0	1	2	0	3	0	4	2	3	0	3	2	1	2	0	1	7	0	1	9	8	3
f ₁	7	0	1	2	0	3	0	4	2	3	0	3	2	1	2	0	1	7	0	1	9	8	3
f ₂		7	0	1	2	0	3	0	4	2	3	0	3	2	1	2	0	1	7	0	1	9	8
f ₃			7	0	1	2	2	3	0	4	2	2	0	3	3	1	2	0	1	7	0	1	9
f ₄				7	7	1	1	2	3	0	4	4	4	0	0	3	3	2	2	2	7	0	1
f ₅					7	7	1	1	1	1	1	1	4	4	4	4	3	3	3	2	7	0	
✓/X	X	X	X	X	✓	X	✓	X	✓	✓	✓	✓	✓	✓	✓	✓	✓	X	✓	✓	X	X	X

Recently
Accessed

Acting as
a stack

Least
recently
accessed

✓ → Hit

X → Miss/Fault

$$\Rightarrow \text{Miss rate/ratio} = 10/23 = 0.4347 //$$

$$\Rightarrow \text{Hit rate/ratio} = 13/23 = 0.5651 //$$

$$\# \text{ Faults/Miss} = 10$$

$$\# \text{ Hits} = 13$$

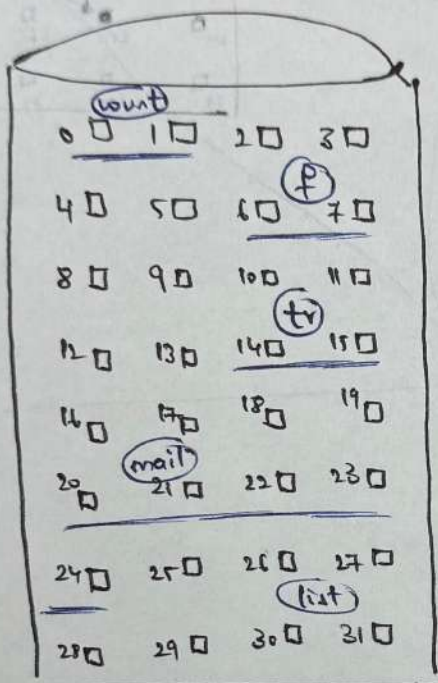
$$\text{Total} = 23$$

3. Using diagrams to show directory tables and blocks allocated in disk for the three allocation methods for files.

⇒ Contiguous Allocation: Mapping from logical to physical.

Directory:

File	Start	Length
wout	0	2
tr	14	3
mail	19	6
list	28	4
f	6	2



Block

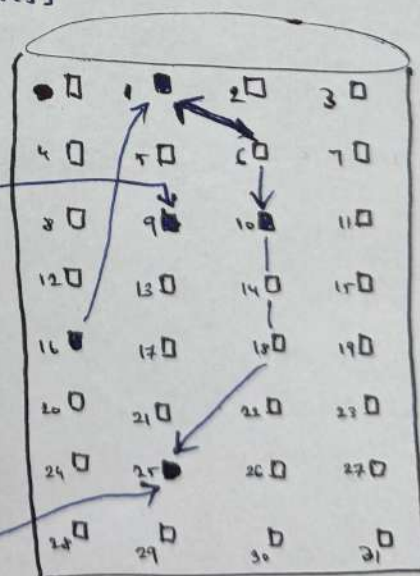
— Block to be accessed = $Q + \text{Starting Address}$

— Displacement into block = R .

⇒ Linked Allocation:

Directory:-

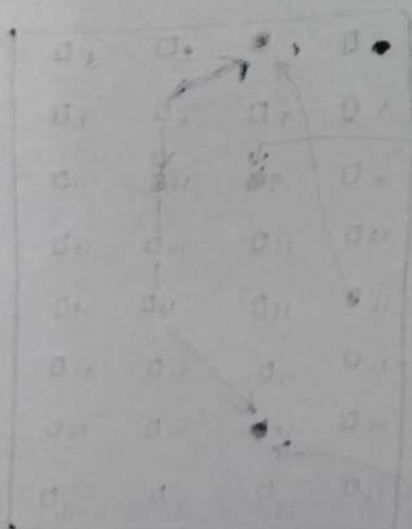
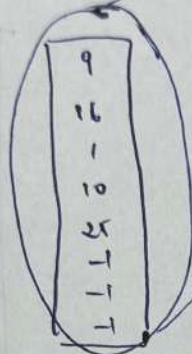
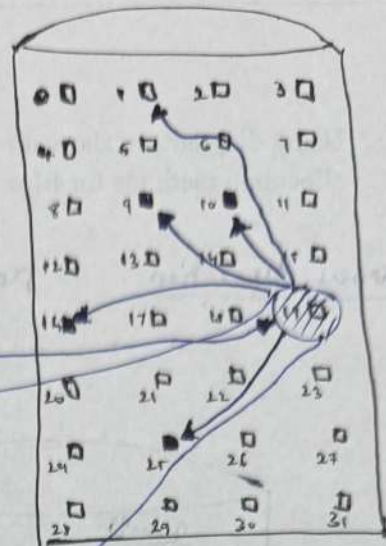
file	start	end
Jeep	9	25



⇒ Indexed Allocation :

Directory :

File	Index - Block
Jup	19



File	Index - Block
Jup	19