## STAT 46700/ CS 5900 Topics in Data Science Spring 2025 Lab 3 [Vaishak Balachandra]

**Q.N. 1**) The gross domestic product (GDP) of the United States in trillions of dollars from 1950-2013 are provided in the link below

http://media.pearsoncmg.com/aw/aw\_sharpe\_business\_3/datasets/txt/GDP\_2013.txt

- a) Display the data using a scatterplot.
- b) Fit a simple linear regression model
- c) Add the fitted line to the scatter plot.
- d) Determine the coefficient of determination.
- e) Analyze the residual plots. Is your model questionable?
- f) Perform the Box-Cox transformation to improve the model.

```
> ####### LAB 3
> # Q1
> 01 <- read.table("https://media.pearsoncmg.com/aw/aw_sharpe_business_3/datasets/txt/GDP_2013.txt"</pre>
 header = T, sep = "\t")
> head(Q1,5)
 Year GDP...T.
1 2013
        13.75
2 2012
         13.67
3 2011
        13.44
4 2010
        13.18
5 2009
        12.87
> dim(Q1)
[1] 64 2
> names(Q1) = c("Year", "GDP")
> head(Q1,5)
 Year
1 2013 13.75
2 2012 13.67
3 2011 13.44
4 2010 13.18
5 2009 12.87
> attach(Q1)
> plot(Year, GDP, main = "Scatterplot: GDP against Year", pch = 17, cex = 1.2, col.main = "orange",
col.lab = "purple", col = "green")
> # b
> model = lm(GDP~Year)
> model
Call:
lm(formula = GDP ~ Year)
Coefficients:
(Intercept)
                  Year
  -387.8433
                0.1993
> cat("Fitted Model:
+ GDP = -387.8433 + 0.1993* Year"
Fitted Model:
```

```
GDP = -387.8433 + 0.1993 * Year
> # c
> abline(model, lwd = 2, col = "red")
> # d
> summary(model)
lm(formula = GDP ~ Year)
Residuals:
               10 Median
                                 30
     Min
-1.23604 -0.63427 -0.07458 0.51860 1.35054
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -3.878e+02 9.217e+00 -42.08 <2e-16 ***
             1.993e-01 4.651e-03 42.84 <2e-16 ***
Year
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.6874 on 62 degrees of freedom
Multiple R-squared: 0.9673, Adjusted R-squared: 0.9668
F-statistic: 1835 on 1 and 62 DF, p-value: < 2.2e-16
> cat("R-squared value: 96.73%")
R-squared value: 96.73%
> # e
> plot(model,1)
> cat("Residual plot is not soo good!! - > as it has a clear structure(parabolic). Thus, needs some
transformation!!")
Residual plot is not soo good!! - > as it has a clear structure(parabolic). Thus, needs some transf
ormation!!
> # f
> install.packages("MASS")
> library(MASS)
> b = boxcox(model)
> b = boxcox(model, lambda = seq(-1,1))
> y1 = GDP^0.25
> new_model = lm(y1~Year)
> summary(new_model)
Call:
lm(formula = y1 \sim Year)
Residuals:
      Min
                 1Q
                      Median
                                     3Q
-0.039953 -0.010020 -0.000066 0.010955 0.028132
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -2.266e+01 2.015e-01 -112.5 <2e-16 ***
Year 1.224e-02 1.017e-04 120.3 <2e-16 ***
                                           <2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.01503 on 62 degrees of freedom
Multiple R-squared: 0.9957, Adjusted R-squared: 0.9957
F-statistic: 1.448e+04 on 1 and 62 DF, p-value: < 2.2e-16
> new_model
lm(formula = y1 ~ Year)
```

```
Coefficients:
(Intercept)
                    Year
  -22.66422
                 0.01224
> cat("New Fitted Model:
+ GDP^0.2 =
               -22.66422 + 0.01224*Year")
New Fitted Model:
GDP^0.2 =
            -22.66422 + 0.01224*Year
> cat("R-squared value: 99.57%")
R-squared value: 99.57%
> plot(new_model,1)
> cat("Residual plot has no clear structure, hence a better model!!")
Residual plot has no clear structure, hence a better model!!
```









