

# AI1103-Assignment 2

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Download all python codes from

[https://github.com/vaishnavi-w/AI1103/blob/main/Assignment\\_2/code\\_assign2.py](https://github.com/vaishnavi-w/AI1103/blob/main/Assignment_2/code_assign2.py)

and latex-tikz codes from

[https://github.com/vaishnavi-w/AI1103/blob/main/Assignment\\_2/latex\\_assign2.tex](https://github.com/vaishnavi-w/AI1103/blob/main/Assignment_2/latex_assign2.tex)

That gives,

$$\Pr(Y = 0|X = 1) = \Pr(Y = 1|X = 0) = \frac{7}{8} \quad (0.0.5)$$

Let E denote the event that bit is transmitted incorrectly. Probability of error,  $\Pr(E)$

$$\Pr(E) = \Pr(X = 0) \Pr(Y = 1|X = 0) + \Pr(X = 1) \Pr(Y = 0|X = 1) \quad (0.0.6)$$

On substituting the values,

$$\Pr(E) = \frac{9}{10} \times \frac{7}{8} + \frac{1}{10} \times \frac{7}{8} \quad (0.0.7)$$

$$= \frac{63}{80} + \frac{7}{80} \quad (0.0.8)$$

$$= \frac{7}{8} \quad (0.0.9)$$

Answer: No option matches

## QUESTION

A binary symmetric channel (BSC) has a transition probability of  $1/8$ . If the binary transmit symbol  $X$  is such that  $\Pr(X = 0) = 9/10$ , then the probability of error for an optimum receiver

- A)  $\frac{7}{80}$
- B)  $\frac{63}{80}$
- C)  $\frac{9}{10}$
- D)  $\frac{1}{10}$

## SOLUTION

Let random variables,  $X \in \{0, 1\}$  denote the bit transmitted and  $Y \in \{0, 1\}$  denote the output bit received.

From the given information,

$$\Pr(X = 0) = \frac{9}{10} \quad (0.0.1)$$

$$\Pr(X = 1) = 1 - \Pr(X = 0) = \frac{1}{10} \quad (0.0.2)$$

Also given, transition probability  $= \frac{1}{8}$ . Transition probability is the probability with which the bit is transmitted correctly. That gives,

$$\Pr(Y = 1|X = 1) = \Pr(Y = 0|X = 0) = \frac{1}{8} \quad (0.0.3)$$

Probability that the bit is not transmitted correctly  
= 1-transition probability

$$= 1 - \frac{1}{8} = \frac{7}{8} \quad (0.0.4)$$