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EE3900 - Gate Assignment 3

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Download all latex-tikz codes from

https://github.com/vaishnavi-w/EE3900/blob/main/Gate3/latex3.tex

GATE EC - 2001 Q1.21

If a signal f(t) has energy E, the energy of the signal f(2t) is equal to

- A) E
- B) $\frac{E}{2}$
- C) $\tilde{2}E$
- D) 4E

SOLUTION

The energy of the signal f(t) is given as.

$$E = \int_{-\infty}^{\infty} |f(t)|^2 dt \qquad (0.0.1)$$

The energy of signal f(2t),

$$E' = \int_{-\infty}^{\infty} |f(2t)|^2 dt \qquad (0.0.2)$$

Putting u = 2t,

$$du = 2dt \qquad (0.0.3)$$

$$E' = \int_{-\infty}^{\infty} |f(u)|^2 \frac{du}{2} = \frac{E}{2}$$
 (0.0.4)

Answer: Option B

Example:

Consider a signal

$$f(t) = e^{-t}u(t) (0.0.5)$$

Energy of the signal,

$$E = \int_{-\infty}^{\infty} |e^{-t}u(t)|^2 dt = \int_{0}^{\infty} e^{-2t} dt = \frac{1}{2}$$
 (0.0.6)

Consider a signal,

$$f(2t) = e^{-2t}u(2t) (0.0.7)$$

$$E' = \int_{-\infty}^{\infty} |e^{-2t}u(2t)|^2 dt \qquad (0.0.8)$$

$$= \int_0^\infty e^{-4t} dt \tag{0.0.9}$$

$$=\frac{1}{4} = \frac{E}{2} \tag{0.0.10}$$