### In [2]:

```
import pandas as pd
import numpy as np
from gurobipy import *
import math
import os
import matplotlib.pyplot as plt
```

### In [3]:

```
table = pd.read_csv("C:/Users/NGDRS-1/Downloads/Adjusted.csv", encoding = "ISO-8859-1", eng
table['Date'] = table.Date.apply(lambda x: pd.to_datetime(x).strftime('%d/%m/%Y'))
#table = table.iloc[::-1]
table = table.set_index('Date')
l = list(a for a in range(50))
data = table.iloc[:,1]
table = data.loc['22/11/2018':'20/11/2020']
```

### In [4]:

```
returns_daily = table.pct_change()
for column in returns_daily:
    returns_daily[column] = returns_daily[column].mask(returns_daily[column]<-0.475, np.nan
avg = returns_daily.mean() * 250/4
cov_daily = returns_daily.cov()
cov = cov_daily * 250/4
#std_daily = returns_daily.std()
#std = std_daily * math.sqrt(125/2)</pre>
```

#### In [5]:

cov

#### Out[5]:

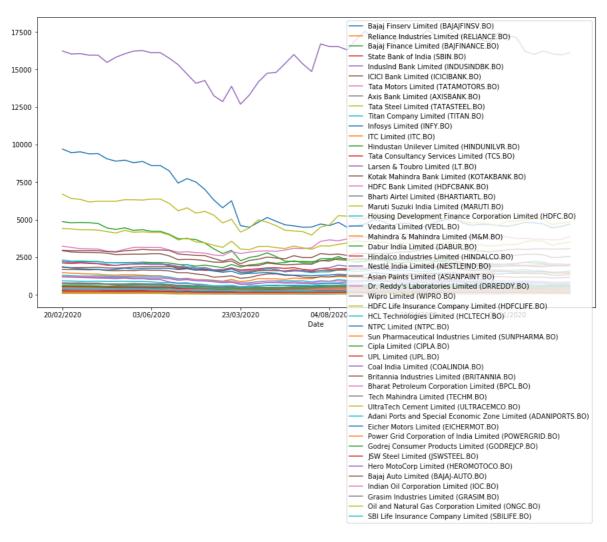
	Bajaj Finserv Limited (BAJAJFINSV.BO)	Reliance Industries Limited (RELIANCE.BO)	Bajaj Finance Limited (BAJFINANCE.BO)	State Bank of India (SBIN.BO)	IndusInd Bank Limited (INDUSINDBK.BO)	(ICIC
Bajaj Finserv Limited (BAJAJFINSV.BO)	0.049449	0.017487	0.047125	0.027874	0.040995	
Reliance Industries Limited (RELIANCE.BO)	0.017487	0.035990	0.017833	0.016079	0.017074	
Bajaj Finance Limited (BAJFINANCE.BO)	0.047125	0.017833	0.060500	0.029923	0.043995	
State Bank of India	0.027874	0.016079	0.029923	0.043528	0.036125	<b>*</b>

### In [51]:

```
tb1 = data.loc['20/02/2020':'20/05/2020']
tb1.plot(figsize=(15,8))
```

### Out[51]:

<matplotlib.axes.\_subplots.AxesSubplot at 0x1b36c8eb188>



### In [6]:

```
def ann_risk_return(table):
    summary = table.agg(["mean","std"]).T
    summary.columns = ["Returns","Risk"]
    summary.Returns = summary.Returns*250
    summary.Risk = summary.Risk*np.sqrt(250)
    return summary
```

### In [7]:

```
ret=table.pct_change().dropna()
```

## In [8]:

summary=ann\_risk\_return(table)

## In [9]:

summary

## Out[9]:

	Returns	Risk
Bajaj Finserv Limited (BAJAJFINSV.BO)	1.766661e+06	22679.307790
Reliance Industries Limited (RELIANCE.BO)	3.709570e+05	5445.133800
Bajaj Finance Limited (BAJFINANCE.BO)	8.220306e+05	10940.176710
State Bank of India (SBIN.BO)	6.675036e+04	965.083893
IndusInd Bank Limited (INDUSINDBK.BO)	2.818815e+05	7368.675261
ICICI Bank Limited (ICICIBANK.BO)	1.020523e+05	1024.635169
Tata Motors Limited (TATAMOTORS.BO)	3.649165e+04	585.336676
Axis Bank Limited (AXISBANK.BO)	1.546971e+05	2238.742989
Tata Steel Limited (TATASTEEL.BO)	1.013505e+05	1155.706337
Titan Company Limited (TITAN.BO)	2.743519e+05	2049.542919
Infosys Limited (INFY.BO)	1.884470e+05	2095.341230
ITC Limited (ITC.BO)	5.584915e+04	629.607689
Hindustan Unilever Limited (HINDUNILVR.BO)	4.842769e+05	3223.337062
Tata Consultancy Services Limited (TCS.BO)	5.209220e+05	3658.911975
Larsen & Toubro Limited (LT.BO)	2.902661e+05	3353.891007
Kotak Mahindra Bank Limited (KOTAKBANK.BO)	3.563117e+05	2645.075129
HDFC Bank Limited (HDFCBANK.BO)	2.807021e+05	1827.692643
Bharti Airtel Limited (BHARTIARTL.BO)	1.038833e+05	1528.719477
Maruti Suzuki India Limited (MARUTI.BO)	1.625847e+06	11704.639404
Housing Development Finance Corporation Limited (HDFC.BO)	4.921693e+05	3510.090808
Vedanta Limited (VEDL.BO)	3.128401e+04	454.283601
Mahindra & Mahindra Limited (M&M.BO)	1.436750e+05	1587.738939
Dabur India Limited (DABUR.BO)	1.123094e+05	633.620179
Hindalco Industries Limited (HINDALCO.BO)	4.547397e+04	476.507291
Nestlé India Limited (NESTLEIND.BO)	3.411875e+06	40760.287768
Asian Paints Limited (ASIANPAINT.BO)	4.104834e+05	3745.795375
Dr. Reddy's Laboratories Limited (DRREDDY.BO)	8.139513e+05	12940.206667
Wipro Limited (WIPRO.BO)	6.424140e+04	617.223139
HDFC Life Insurance Company Limited (HDFCLIFE.BO)	1.270195e+05	1409.268331
HCL Technologies Limited (HCLTECH.BO)	1.426039e+05	1649.041965
NTPC Limited (NTPC.BO)	2.584179e+04	223.365274
Sun Pharmaceutical Industries Limited (SUNPHARMA.BO)	1.105473e+05	690.060256
Cipla Limited (CIPLA.BO)	1.392229e+05	1703.180744
UPL Limited (UPL.BO)	1.298048e+05	1373.368177

	Returns	Risk
Coal India Limited (COALINDIA.BO)	4.100109e+04	560.031185
Britannia Industries Limited (BRITANNIA.BO)	7.640300e+05	6072.812368
Bharat Petroleum Corporation Limited (BPCL.BO)	9.299511e+04	968.973295
Tech Mahindra Limited (TECHM.BO)	1.716117e+05	1408.776755
UltraTech Cement Limited (ULTRACEMCO.BO)	1.016297e+06	5984.290714
Adani Ports and Special Economic Zone Limited (ADANIPORTS.BO)	8.914556e+04	584.108124
Eicher Motors Limited (EICHERMOT.BO)	4.871302e+05	4176.938869
Power Grid Corporation of India Limited (POWERGRID.BO)	4.385605e+04	182.880386
Godrej Consumer Products Limited (GODREJCP.BO)	1.666803e+05	1019.015495
JSW Steel Limited (JSWSTEEL.BO)	6.193819e+04	690.202063
Hero MotoCorp Limited (HEROMOTOCO.BO)	6.283175e+05	5331.900871
Bajaj Auto Limited (BAJAJ-AUTO.BO)	6.928005e+05	3757.552833
Indian Oil Corporation Limited (IOC.BO)	2.826182e+04	399.655744
Grasim Industries Limited (GRASIM.BO)	1.826897e+05	1749.541205
Oil and Natural Gas Corporation Limited (ONGC.BO)	2.738557e+04	470.478320
SBI Life Insurance Company Limited (SBILIFE.BO)	1.934133e+05	2074.337447

### In [10]:

```
noa=50
nop=100000
```

### In [11]:

```
matrix=np.random.random(50*50).reshape(50,50)
```

### In [12]:

```
np.random.seed(123)
matrix=np.random.random(noa*nop).reshape(nop,noa)
matrix
```

### Out[12]:

```
array([[0.69646919, 0.28613933, 0.22685145, ..., 0.98555979, 0.51948512, 0.61289453],
[0.12062867, 0.8263408, 0.60306013, ..., 0.39887629, 0.2408559, 0.34345601],
[0.51312815, 0.66662455, 0.10590849, ..., 0.04857903, 0.7086974, 0.83924335],
...,
[0.771363, 0.66399452, 0.70980034, ..., 0.42080155, 0.18014488, 0.02020186],
[0.00555788, 0.05765405, 0.66167542, ..., 0.42020726, 0.05788854, 0.58869437],
[0.60038571, 0.05553236, 0.03331703, ..., 0.7533014, 0.86757063, 0.89091337]])
```

```
In [13]:
matrix.sum(axis=1,keepdims=True)
```

### In [14]:

```
w=matrix/matrix.sum(axis=1,keepdims=True)
```

### In [15]:

```
w.sum(axis=1,keepdims=True)
```

### Out[15]:

### In [16]:

```
port_ret=ret.dot(w.T)
port_ret
```

## Out[16]:

	0	1	2	3	4	5	6	7
Date								
26/11/2018	0.007291	0.007718	0.006313	0.007552	0.006554	0.007322	0.006797	0.00503
27/11/2018	0.001259	0.000681	0.000012	0.000965	0.003069	0.001739	-0.000603	0.001318
28/11/2018	-0.005058	-0.002140	-0.002731	-0.003834	-0.002574	-0.004331	-0.003971	-0.002473
29/11/2018	0.012058	0.012215	0.011260	0.011317	0.010556	0.012394	0.008232	0.01244
30/11/2018	0.000992	0.001542	-0.001507	-0.000282	0.001242	-0.000371	0.001277	0.003490
13/11/2020	0.005674	0.005512	0.004157	0.004223	0.004312	0.003810	0.003950	0.005058
17/11/2020	0.012795	0.011331	0.013553	0.012931	0.013622	0.010695	0.008955	0.011764
18/11/2020	0.013195	0.008809	0.006611	0.007659	0.011459	0.007995	0.004247	0.004968
19/11/2020	-0.010148	-0.008445	-0.007706	-0.008812	-0.009546	-0.012205	-0.009010	-0.007394
20/11/2020	0.011452	0.007921	0.009719	0.010568	0.010721	0.009641	0.008493	0.01112 <sup>-</sup>

491 rows × 100000 columns

## In [17]:

```
port_summary=ann_risk_return(port_ret)
port_summary
```

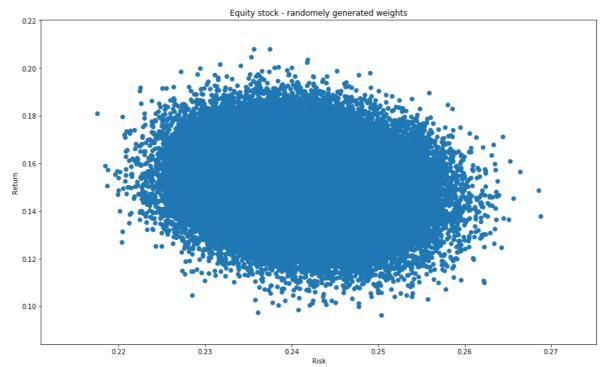
## Out[17]:

	Returns	Risk
0	0.136387	0.253552
1	0.147636	0.236920
2	0.144254	0.239222
3	0.137245	0.249108
4	0.121209	0.246982
99995	0.148680	0.242511
99996	0.147342	0.236842
99997	0.159729	0.231583
99998	0.165464	0.235063
99999	0.140038	0.236858

100000 rows × 2 columns

### In [19]:

```
plt.figure(figsize=(15,9))
plt.scatter(port_summary.loc[:,"Risk"], port_summary.loc[:,"Returns"])
plt.xlabel("Risk")
plt.ylabel("Return")
plt.title("Equity stock - randomely generated weights")
plt.show()
```



## ### Optimized portfolio

### In [ ]:

### In [21]:

```
model = Model('min_risk')
```

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### In [22]:

```
tickers = table.columns
variables = pd.Series(model.addVars(tickers),index=tickers)
```

## In [23]:

## variables

## Out[23]:

Bajaj Finserv Limited (BAJAJFINSV.BO)  *Awaiting Model Update*>	<gurobi.var< th=""></gurobi.var<>
Reliance Industries Limited (RELIANCE.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Bajaj Finance Limited (BAJFINANCE.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
State Bank of India (SBIN.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
<pre>IndusInd Bank Limited (INDUSINDBK.BO) *Awaiting Model Update*&gt;</pre>	<gurobi.var< td=""></gurobi.var<>
ICICI Bank Limited (ICICIBANK.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Tata Motors Limited (TATAMOTORS.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Axis Bank Limited (AXISBANK.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Tata Steel Limited (TATASTEEL.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Titan Company Limited (TITAN.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
<pre>Infosys Limited (INFY.BO) *Awaiting Model Update*&gt;</pre>	<gurobi.var< td=""></gurobi.var<>
ITC Limited (ITC.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Hindustan Unilever Limited (HINDUNILVR.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Tata Consultancy Services Limited (TCS.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Larsen & Toubro Limited (LT.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Kotak Mahindra Bank Limited (KOTAKBANK.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
HDFC Bank Limited (HDFCBANK.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Bharti Airtel Limited (BHARTIARTL.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Maruti Suzuki India Limited (MARUTI.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Housing Development Finance Corporation Limited (HDFC.BO) *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Vedanta Limited (VEDL.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Mahindra & Mahindra Limited (M&M.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Dabur India Limited (DABUR.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Hindalco Industries Limited (HINDALCO.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Nestlé India Limited (NESTLEIND.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Asian Paints Limited (ASIANPAINT.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Dr. Reddy's Laboratories Limited (DRREDDY.BO)  *Awaiting Model Update*>	<gurobi.var< td=""></gurobi.var<>
Wipro Limited (WIPRO.BO)	<gurobi.var< td=""></gurobi.var<>

```
*Awaiting Model Update*>
HDFC Life Insurance Company Limited (HDFCLIFE.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
HCL Technologies Limited (HCLTECH.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
NTPC Limited (NTPC.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Sun Pharmaceutical Industries Limited (SUNPHARMA.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Cipla Limited (CIPLA.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
UPL Limited (UPL.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Coal India Limited (COALINDIA.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Britannia Industries Limited (BRITANNIA.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Bharat Petroleum Corporation Limited (BPCL.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Tech Mahindra Limited (TECHM.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
UltraTech Cement Limited (ULTRACEMCO.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Adani Ports and Special Economic Zone Limited (ADANIPORTS.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Eicher Motors Limited (EICHERMOT.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Power Grid Corporation of India Limited (POWERGRID.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Godrej Consumer Products Limited (GODREJCP.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
JSW Steel Limited (JSWSTEEL.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Hero MotoCorp Limited (HEROMOTOCO.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Bajaj Auto Limited (BAJAJ-AUTO.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Indian Oil Corporation Limited (IOC.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Grasim Industries Limited (GRASIM.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
Oil and Natural Gas Corporation Limited (ONGC.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
SBI Life Insurance Company Limited (SBILIFE.BO)
                                                                  <gurobi.Var
*Awaiting Model Update*>
dtype: object
```

#### In [24]:

```
port_risk = cov.dot(variables).dot(variables)
```

### In [25]:

```
model.setObjective(port_risk,GRB.MINIMIZE)
```

### In [26]:

```
model.addConstr(variables.sum() == 1,'weights')
model.update()
```

```
In [27]:
```

```
model.setParam('OutputFlag',0)
model.update()
```

## In [28]:

model.optimize()

### In [29]:

```
n = 0
weights = {}
for v in variables:
    weights.update({tickers[n]:v.x})
    n = n + 1
weights = pd.DataFrame([weights])
weights = weights.transpose()
weights.columns = ['Weights']
print('\nMin Risk, Optimal Weights Per Stock')
print(weights['Weights'])
```

Min Risk, Optimal Weights Per Stock	
Bajaj Finserv Limited (BAJAJFINSV.BO) 9	1.002528e-0
Reliance Industries Limited (RELIANCE.BO) 9	2.152221e-0
Bajaj Finance Limited (BAJFINANCE.BO) 9	1.096568e-0
State Bank of India (SBIN.BO)	1.534637e-0
<pre>IndusInd Bank Limited (INDUSINDBK.BO) 0</pre>	4.771230e-1
ICICI Bank Limited (ICICIBANK.BO) 9	1.203805e-0
Tata Motors Limited (TATAMOTORS.BO)	6.935419e-1
Axis Bank Limited (AXISBANK.BO) 0	6.562343e-1
Tata Steel Limited (TATASTEEL.BO) 0	8.920722e-1
Titan Company Limited (TITAN.BO) 9	9.332683e-0
Infosys Limited (INFY.BO) 7	4.001331e-0
ITC Limited (ITC.BO) 2	6.688211e-0
Hindustan Unilever Limited (HINDUNILVR.BO) 2	5.338318e-0
Tata Consultancy Services Limited (TCS.BO)	1.379921e-0
1 Larsen & Toubro Limited (LT.BO)	3.805840e-0
9 Kotak Mahindra Bank Limited (KOTAKBANK.BO) 9	4.574176e-0
HDFC Bank Limited (HDFCBANK.BO)	3.466614e-0
Bharti Airtel Limited (BHARTIARTL.BO)	1.961138e-0
6 Maruti Suzuki India Limited (MARUTI.BO)	1.223135e-0
9 Housing Development Finance Corporation Limited (HDFC.BO)	2.734705e-0
9 Vedanta Limited (VEDL.BO)	7.207923e-1
Mahindra & Mahindra Limited (M&M.BO)	1.361930e-0
9 Dabur India Limited (DABUR.BO)	7.379489e-0

2	
Hindalco Industries Limited (HINDALCO.BO) 0	5.494724e-1
Nestlé India Limited (NESTLEIND.BO)	7.778221e-0
2 Asian Paints Limited (ASIANPAINT.BO) 2	5.926722e-0
Dr. Reddy's Laboratories Limited (DRREDDY.BO)	1.180732e-0
1 Wipro Limited (WIPRO.BO)	1.442046e-0
2 HDFC Life Insurance Company Limited (HDFCLIFE.BO) 9	3.420643e-0
HCL Technologies Limited (HCLTECH.BO)	5.170507e-0
A NTPC Limited (NTPC.BO)	1.413838e-0
8 Sun Pharmaceutical Industries Limited (SUNPHARMA.BO)	6.471203e-0
3 Cipla Limited (CIPLA.BO)	6.786587e-0
UPL Limited (UPL.BO)	1.831145e-0
9 Coal India Limited (COALINDIA.BO)	9.023214e-0
2 Britannia Industries Limited (BRITANNIA.BO)	1.695131e-0
8 Bharat Petroleum Corporation Limited (BPCL.BO)	1.280441e-0
9 Tech Mahindra Limited (TECHM.BO)	5.060378e-0
9 UltraTech Cement Limited (ULTRACEMCO.BO)	1.793656e-0
9 Adani Ports and Special Economic Zone Limited (ADANIPORTS.BO)	2.011598e-0
8 Eicher Motors Limited (EICHERMOT.BO) 7	1.639624e-0
Power Grid Corporation of India Limited (POWERGRID.BO)	1.648383e-0
Godrej Consumer Products Limited (GODREJCP.BO) 2	1.629266e-0
JSW Steel Limited (JSWSTEEL.BO)	6.679570e-1
0 Hero MotoCorp Limited (HEROMOTOCO.BO)	2.070724e-0
9 Bajaj Auto Limited (BAJAJ-AUTO.BO)	1.014335e-0
8 Indian Oil Corporation Limited (IOC.BO) 2	1.751865e-0
Grasim Industries Limited (GRASIM.BO)	8.227978e-1
0 Oil and Natural Gas Corporation Limited (ONGC.BO)	1.083425e-0
9 SBI Life Insurance Company Limited (SBILIFE.BO) 9	5.062407e-0
Name: Weights, dtype: float64	

```
In [30]:
```

```
print('\nMinimized Portfolio Variance : '+str(port_risk.getValue()))
```

Minimized Portfolio Variance: 0.007861859090797441

```
In [31]:
```

```
min_vol = math.sqrt(port_risk.getValue())
print('Volatility : '+str(min_vol))
```

Volatility: 0.08866712519754681

### In [32]:

```
port_return = avg.dot(variables)
Rmin = port_return.getValue()
print('Expected Return (Rmin) : '+str(Rmin))
```

Expected Return (Rmin): 0.040752730159228485

### In [33]:

```
Rmax = avg.max()
```

#### In [34]:

```
target = model.addConstr(port_return == Rmin, 'target')
```

#### In [35]:

```
eff = {}
iterations = 50
diff = (Rmax-Rmin)/(iterations-1)
Rrange = np.arange(Rmin,Rmax+diff,diff)
for r in Rrange:
    target.rhs = r
    model.optimize()
    temp = math.sqrt(port_risk.getValue())
    eff.update({temp:r})
```

### In [36]:

```
frontier = pd.DataFrame([eff]).transpose()
frontier.columns = ['Returns']
frontier['Risk'] = frontier.index
frontier = frontier.reset_index(drop=True)
```

### In [37]:

```
print('\nEfficient Frontier')
print(frontier)
```

#### Efficient Frontier Returns Risk 0 0.040753 0.088667 1 0.042344 0.088679 2 0.043935 0.088714 3 0.045527 0.088773 4 0.047118 0.088855 5 0.048709 0.088959 6 0.050301 0.089087 7 0.051892 0.089239 8 0.053483 0.089414 9 0.055075 0.089614 10 0.056666 0.089840 11 0.058258 0.090090 12 0.059849 0.090365 0.090667 13 0.061440 0.063032 14 0.090996 15 0.064623 0.091351 16 0.066214 0.091743 17 0.067806 0.092225 18 0.069397 0.092801 19 0.070988 0.093470 20 0.072580 0.094231 21 0.074171 0.095080 22 0.075762 0.096014 23 0.077354 0.097030 24 0.078945 0.098129 25 0.080536 0.099318 26 0.082128 0.100597 27 0.083719 0.101963 28 0.085310 0.103416 29 0.086902 0.104962 0.106677 30 0.088493 31 0.090084 0.108583 32 0.091676 0.110733 33 0.093267 0.113255 34 0.094858 0.116298 35 0.096450 0.120017 0.098041 36 0.124464 37 0.099632 0.129688 38 0.101224 0.135602 39 0.102815 0.142120 40 0.104406 0.149366 41 0.105998 0.157444 42 0.107589 0.166235 43 0.109181 0.175630 44 0.110772 0.185538 45 0.112363 0.195890 46 0.113955 0.207086 47 0.115546 0.219264 48 0.117137 0.232268

0.245967

49

0.118729

### In [38]:

```
frontier['Sharpe'] = frontier['Returns']/frontier['Risk']
idx = frontier['Sharpe'].max()
sharpeMax = frontier.loc[frontier['Sharpe'] == idx]
sharpeMax = sharpeMax.reset_index(drop=True)
```

### In [39]:

```
target.rhs = sharpeMax['Returns'][0]
model.optimize()
n = 0
sharpe_weights = {}
for v in variables:
    sharpe_weights.update({tickers[n]:v.x})
    n = n + 1
sharpe_weights = pd.DataFrame([sharpe_weights])
sharpe_weights = sharpe_weights.transpose()
sharpe_weights.columns = ['Weights']
```

### In [40]:

```
print('\nMaximum Sharpe Ratio')
print(sharpeMax)
print(sharpe_weights)
```

Maximum Sharpe Ratio
Returns Risk Sharpe
0 0.090084 0.108583 0.829634

0 0.090084 0.108583 0.829634	
	Weights
Bajaj Finserv Limited (BAJAJFINSV.BO)	2.484757e-11
Reliance Industries Limited (RELIANCE.BO)	1.445125e-02
Bajaj Finance Limited (BAJFINANCE.BO)	1.121958e-01
State Bank of India (SBIN.BO)	9.326079e-12
<pre>IndusInd Bank Limited (INDUSINDBK.BO)</pre>	5.038330e-12
ICICI Bank Limited (ICICIBANK.BO)	2.162615e-11
Tata Motors Limited (TATAMOTORS.BO)	1.318703e-11
Axis Bank Limited (AXISBANK.BO)	9.452994e-12
Tata Steel Limited (TATASTEEL.BO)	1.194007e-11
Titan Company Limited (TITAN.BO)	1.908272e-10
Infosys Limited (INFY.BO)	1.829915e-01
ITC Limited (ITC.BO)	9.883605e-12
Hindustan Unilever Limited (HINDUNILVR.BO)	2.252618e-11
Tata Consultancy Services Limited (TCS.BO)	1.956992e-02
Larsen & Toubro Limited (LT.BO)	9.419782e-12
Kotak Mahindra Bank Limited (KOTAKBANK.BO)	1.518004e-10
HDFC Bank Limited (HDFCBANK.BO)	4.606345e-11
Bharti Airtel Limited (BHARTIARTL.BO)	5.700317e-02
Maruti Suzuki India Limited (MARUTI.BO)	9.530653e-12
Housing Development Finance Corporation Limited	2.674650e-11
Vedanta Limited (VEDL.BO)	6.467916e-12
Mahindra & Mahindra Limited (M&M.BO)	1.130592e-11
Dabur India Limited (DABUR.BO)	2.901144e-11
Hindalco Industries Limited (HINDALCO.BO)	8.442361e-12
Nestlé India Limited (NESTLEIND.BO)	2.179800e-01
Asian Paints Limited (ASIANPAINT.BO)	5.563677e-02
Dr. Reddy's Laboratories Limited (DRREDDY.BO)	2.934738e-01
Wipro Limited (WIPRO.BO)	1.592416e-10
HDFC Life Insurance Company Limited (HDFCLIFE.BO)	9.114685e-10
HCL Technologies Limited (HCLTECH.BO)	4.669784e-02
NTPC Limited (NTPC.BO)	1.143688e-11
Sun Pharmaceutical Industries Limited (SUNPHARM	1.373288e-11
Cipla Limited (CIPLA.BO)	8.132539e-09
UPL Limited (UPL.BO)	8.544153e-12
Coal India Limited (COALINDIA.BO)	7.392791e-12
Britannia Industries Limited (BRITANNIA.BO)	1.751780e-11
Bharat Petroleum Corporation Limited (BPCL.BO)	5.370823e-11
Tech Mahindra Limited (TECHM.BO)	2.086865e-11
UltraTech Cement Limited (ULTRACEMCO.BO)	1.641260e-11
Adani Ports and Special Economic Zone Limited (	1.492028e-11
Eicher Motors Limited (EICHERMOT.BO)	1.894341e-11
Power Grid Corporation of India Limited (POWERG	7.129484e-11
Godrej Consumer Products Limited (GODREJCP.BO)	1.335122e-11
JSW Steel Limited (JSWSTEEL.BO)	1.056568e-11
Hero MotoCorp Limited (HEROMOTOCO.BO)	1.564208e-11
· · · · · · · · · · · · · · · · · · ·	
Bajaj Auto Limited (BAJAJ-AUTO.BO) Indian Oil Corporation Limited (IOC.BO)	2.365075e-11 8.699925e-12
Grasim Industries Limited (GRASIM.BO)	
Oil and Natural Gas Corporation Limited (ONGC.BO)	1.016842e-11 5.444682e-12
· · · · · · · · · · · · · · · · · · ·	
SBI Life Insurance Company Limited (SBILIFE.BO)	7.195355e-11

## In [41]:

# sharpe\_weights

## Out[41]:

	Weights
Bajaj Finserv Limited (BAJAJFINSV.BO)	2.484757e-11
Reliance Industries Limited (RELIANCE.BO)	1.445125e-02
Bajaj Finance Limited (BAJFINANCE.BO)	1.121958e-01
State Bank of India (SBIN.BO)	9.326079e-12
IndusInd Bank Limited (INDUSINDBK.BO)	5.038330e-12
ICICI Bank Limited (ICICIBANK.BO)	2.162615e-11
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Tata Consultancy Services Limited (TCS.BO)	1.956992e-02
Larsen & Toubro Limited (LT.BO)	9.419782e-12
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Maruti Suzuki India Limited (MARUTI.BO)	9.530653e-12
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Vedanta Limited (VEDL.BO)	6.467916e-12
Mahindra & Mahindra Limited (M&M.BO)	1.130592e-11
Dabur India Limited (DABUR.BO)	2.901144e-11
Hindalco Industries Limited (HINDALCO.BO)	8.442361e-12
Nestlé India Limited (NESTLEIND.BO)	2.179800e-01
Asian Paints Limited (ASIANPAINT.BO)	5.563677e-02
Dr. Reddy's Laboratories Limited (DRREDDY.BO)	2.934738e-01
Wipro Limited (WIPRO.BO)	1.592416e-10
HDFC Life Insurance Company Limited (HDFCLIFE.BO)	9.114685e-10
HCL Technologies Limited (HCLTECH.BO)	4.669784e-02
NTPC Limited (NTPC.BO)	1.143688e-11
Sun Pharmaceutical Industries Limited (SUNPHARMA.BO)	1.373288e-11
Cipla Limited (CIPLA.BO)	8.132539e-09
UPL Limited (UPL.BO)	8.544153e-12

### Weights

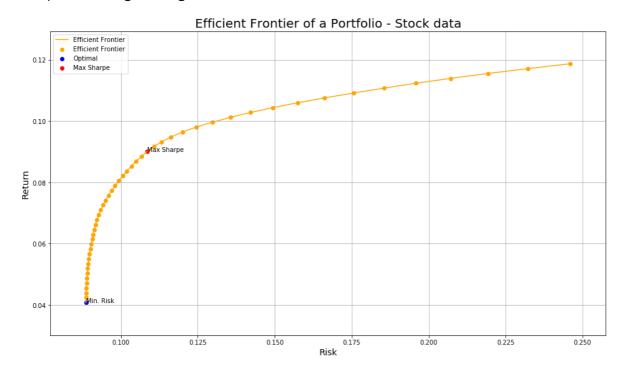
Coal India Limited (COALINDIA.BO)	7.392791e-12
Britannia Industries Limited (BRITANNIA.BO)	1.751780e-11
Bharat Petroleum Corporation Limited (BPCL.BO)	5.370823e-11
Tech Mahindra Limited (TECHM.BO)	2.086865e-11
UltraTech Cement Limited (ULTRACEMCO.BO)	1.641260e-11
Adani Ports and Special Economic Zone Limited (ADANIPORTS.BO)	1.492028e-11
Eicher Motors Limited (EICHERMOT.BO)	1.894341e-11
Power Grid Corporation of India Limited (POWERGRID.BO)	7.129484e-11
Godrej Consumer Products Limited (GODREJCP.BO)	1.335122e-11
JSW Steel Limited (JSWSTEEL.BO)	1.056568e-11
Hero MotoCorp Limited (HEROMOTOCO.BO)	1.564208e-11
Bajaj Auto Limited (BAJAJ-AUTO.BO)	2.365075e-11
Indian Oil Corporation Limited (IOC.BO)	8.699925e-12
Grasim Industries Limited (GRASIM.BO)	1.016842e-11
Oil and Natural Gas Corporation Limited (ONGC.BO)	5.444682e-12
SBI Life Insurance Company Limited (SBILIFE.BO)	7.195355e-11

#### In [42]:

```
fig, ax = plt.subplots(nrows=1,ncols=1)
fig.set_size_inches(16,9)
ax.set_title('Efficient Frontier of a Portfolio - Stock data',fontsize=20)
ax.set_xlabel('Risk',fontsize=14)
ax.set_ylabel('Return',fontsize=14)
ax.scatter(x=frontier['Risk'],y=frontier['Returns'],color='orange',label='Efficient Frontie
ax.plot()#x=frontier['Risk'],y=frontier['Returns'],color='orange')
temp = pd.DataFrame([eff]).transpose()
temp.columns = ['Efficient Frontier']
temp.plot(color='orange',label='Efficient Frontier',ax=ax)
#ax.scatter(x=std,y=avg,color='green',label='Stocks')
i = 0
#for stock in tickers:
     ax.annotate(stock,(std[i],avg[i]))
     i = i + 1
ax.scatter(x=min_vol,y=Rmin,color='blue',label='Optimal')
ax.annotate('Min. Risk',(min_vol,Rmin))
ax.scatter(x=sharpeMax['Risk'],y=sharpeMax['Returns'],color='red',label='Max Sharpe')
ax.annotate('Max Sharpe',(sharpeMax['Risk'],sharpeMax['Returns']))
ax.grid()
ax.legend(loc='upper left')
```

### Out[42]:

<matplotlib.legend.Legend at 0x1b378a81548>



#### In [31]:

```
# Calculate mean returns for each stock
avg_rets = returns_daily.mean()

# Calculate mean returns for portfolio overall,
# using dot product to
# normalize individual means against investment weights
# https://en.wikipedia.org/wiki/Dot_product#:~:targetText=In%20mathematics%2C%20the%20dot%
port_mean = avg_rets.dot(sharpe_weights)

# Calculate portfolio standard deviation
port_stdev = np.sqrt(sharpe_weights.T.dot(cov).dot(sharpe_weights))
```

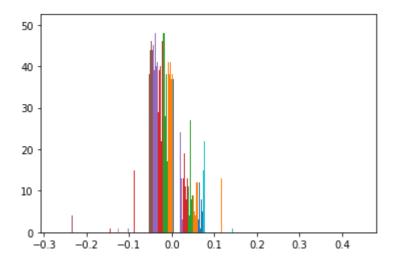
### In [32]:

```
import matplotlib.pyplot as plt
plt.hist(returns_daily)
plt.show
```

```
C:\Users\NGDRS-1\anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6743:
RuntimeWarning: All-NaN slice encountered
  xmin = min(xmin, np.nanmin(xi))
C:\Users\NGDRS-1\anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6744:
RuntimeWarning: All-NaN slice encountered
  xmax = max(xmax, np.nanmax(xi))
```

### Out[32]:

<function matplotlib.pyplot.show(\*args, \*\*kw)>



### In [33]:

```
initial_investment = 10000
# Calculate mean of investment
mean_investment = (1+port_mean) * initial_investment
# Calculate standard deviation of investmnet
stdev_investment = initial_investment * port_stdev
```

```
In [34]:
```

```
# Select our confidence interval (I'll choose 95% here)
conf_level1 = 0.05
# Using SciPy ppf method to generate values for the
# inverse cumulative distribution function to a normal distribution
# Plugging in the mean, standard deviation of our portfolio
# as calculated above
# https://docs.scipy.org/doc/scipy/reference/generated/scipy.stats.norm.html
from scipy.stats import norm
cutoff1 = norm.ppf(conf_level1, mean_investment, stdev_investment)
cutoff1
Out[34]:
array([[8228.37855592]])
In [35]:
#Finally, we can calculate the VaR at our confidence interval
var_1d1 = initial_investment - cutoff1
var_1d1
#output
Out[35]:
array([[1771.62144408]])
In [ ]:
```