

## EE23BTECH11014- DEVARAKONDA GUNA VAISHNAVI\*

**Question:** The sum of the first  $n$  terms of two arithmetic progressions (AP) is in the ratio  $5n+4 : 9n+6$ . Find the ratio of their 18th terms.

**Solution:** :

Parameter	value	Description
$x_1(0)$	$\frac{9}{2}$	First term of the first arithmetic progression (AP).
$x_2(0)$	$\frac{15}{2}$	First term of the second arithmetic progression (AP).
$d_1$	5	Common difference of the first AP.
$d_2$	9	Common difference of the second AP.
$n$	-	Index of the term in the sequences.

TABLE I  
INPUT PARAMETERS

$$x_1(n) = (x_1(0) + nd_1)u(n) \quad (1)$$

$$x_2(n) = (x_2(0) + nd_2)u(n) \quad (2)$$

Applying Z transform: Taking Z-Transform:

1)  $\mathcal{Z}\{u(n)\}$

$$u(n) \xleftrightarrow{\mathcal{Z}} \frac{1}{1 - z^{-1}} \{|z| > 1\} \quad (3)$$

2)  $\mathcal{Z}\{nu(n)\}$

$$nu(n) \xleftrightarrow{\mathcal{Z}} \frac{z^{-1}}{(1 - z^{-1})^2} \{|z| > 1\} \quad (4)$$

$$\frac{\frac{n}{2} [2x_1(0) + (n-1)d_1]}{\frac{n}{2} [2x_2(0) + (n-1)d_2]} = \frac{5n+4}{9n+6} \quad (5)$$

$$\frac{2x_1(0) + nd_1 - d_1}{2x_2(0) + nd_2 - d_2} = \frac{5n+4}{9n+6} \quad (6)$$

On comparing we get,  $d_1 = 5$  and  $d_2 = 9$

$$2x_1(0) - d_1 = 4 \quad (7)$$

$$x_1(0) = \frac{9}{2} \quad (8)$$

$$2x_2(0) - d_2 = 6 \quad (9)$$

$$x_2(0) = \frac{15}{2} \quad (10)$$

$$\Rightarrow X_1(z) = \frac{9/2}{1 - z^{-1}} + \frac{5z^{-1}}{(1 - z^{-1})^2} \quad (11)$$

$$\Rightarrow X_2(z) = \frac{15/2}{1 - z^{-1}} + \frac{9z^{-1}}{(1 - z^{-1})^2} \quad (12)$$

$$x_1(n) = \{9/2, 19/2, 29/2, \dots\} \quad (13)$$

$$x_2(n) = \{15/2, 33/2, 51/2, \dots\} \quad (14)$$

$$\Rightarrow \frac{x_1(18)}{x_2(18)} = \frac{179}{321} \quad (15)$$

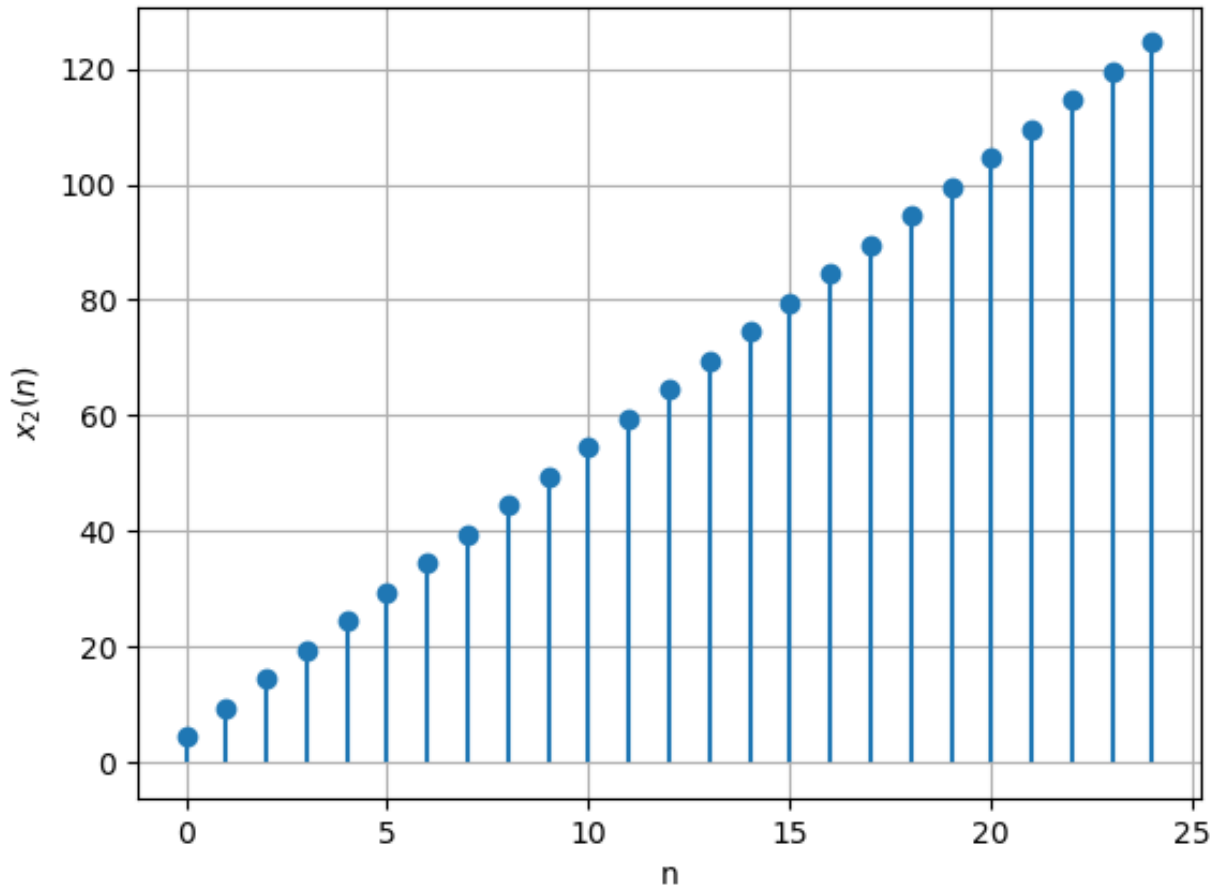


Fig. 1. stem plot of  $x_1(n)$

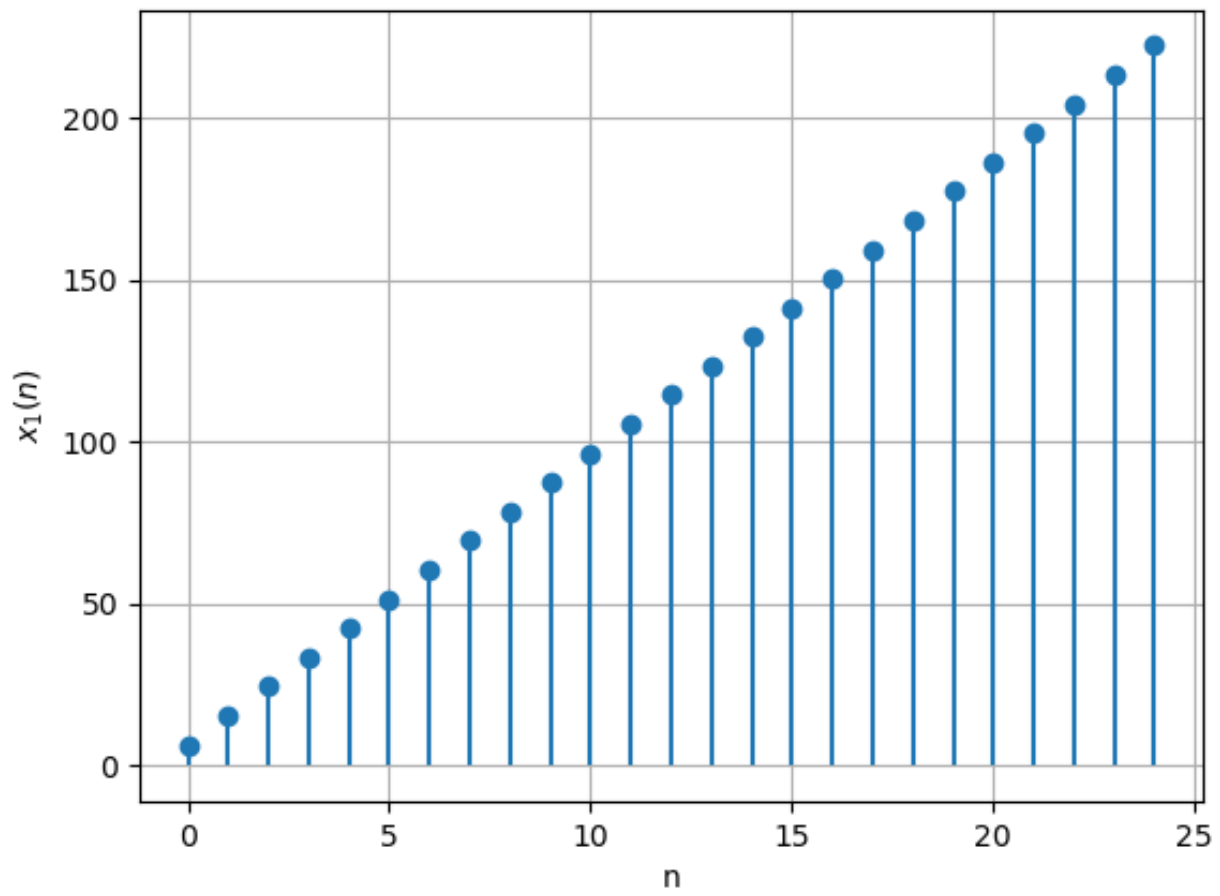


Fig. 2. stem plot of  $x_2(n)$