

Lectures for semester 1
 Course Module : Digital Signal Processing
 End course exam, December 19th 2014
 1.5 hour, documents and calculators allowed
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I. The exponential signal, defined as

$x_a(t) = e^{-t}$, if t is positive or zero,

$x_a(t) = 0$, if t is strictly negative,

is sampled at the rate $F_s = 20$ samples per second, and a block of $N = 64$ samples is used to calculate the spectrum.

- Draw the signal $x_a(t)$ versus time
- Calculate and draw versus frequency F the modulus of Fourier Transform $X_a(F)$ of $x_a(t)$.
- Give the sampled signal $x(n)$ as a series indexed by n .
- Give the analytical expression of $X(k)$, the discrete Fourier transform of $x(n)$. It is not required to calculate $X(k)$, but be aware in your relation with the different parameters: F_s , k , n and N ...
- Why is it interesting to choose $N = 64$? If N was initially equal to 60, how can we get 4 more samples to benefit from this interesting feature?

II. The first five points of DFT $X(k)$ of a real-valued sequence $x(n)$ of 8 samples are:

0.25; $0.125 - j 0.3018$; 0; $0.125 - j 0.0518$; 0; ...

Determine the remaining three points.

Indication: Remember that:

$$X(k) = \sum_{n=-p}^{-p+N-1} x(n) \cdot e^{-2ik\pi \frac{n}{N}}$$

And take $p = 4$. Then, because $x(n)$ is real-valued, use the symmetry of real part of $X(k)$ from one hand, then of the imaginary part from the another one.

III. Calculate the FFT of the signal:

$x(n) = \{ 1; 0; 0; -1; 1; -1; 0; 0 \}$.

And sketch its magnitude and phase.