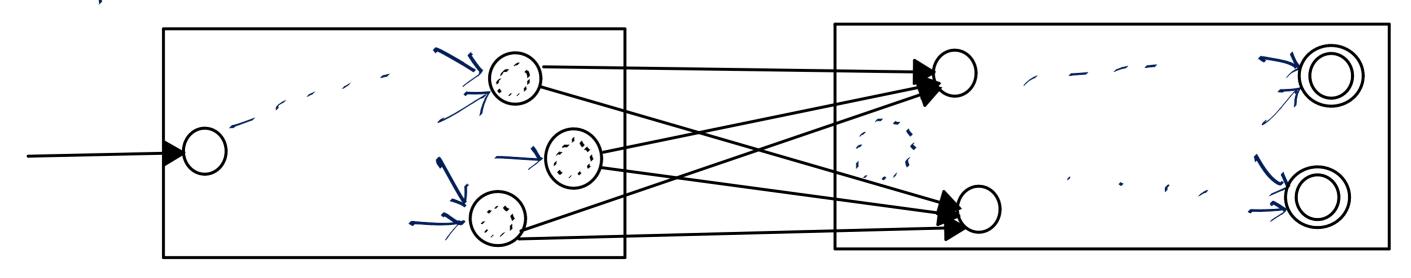
NONDETERMINISM

Recap: Reg is closed under union, intersection, and complementation Today: Other operations, wondeterminism

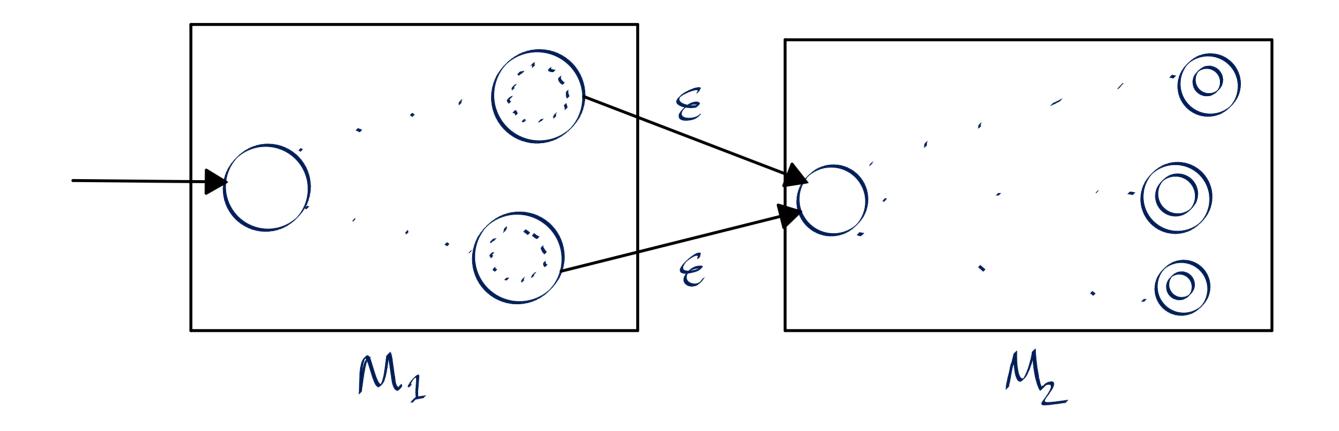
Concatenation:

If A and B are regular (s.t. A= L(M1) and B= L(M2)), is AoB = {xy | x ∈ A, y ∈ B} regular?

Suppose A.B is regular. How can we construct a DFAM for it?



Consider the following languages over $\Xi = \{a, b\}$ A: all strings containing at least one a (M_1) B: all strings containing at least one b (M_2) What do M_1 , M_2 , and M look like? The machine needs to "know" when a "relevant substring ends, and check membership in the appropriate language accordingly. How can it know such a thing? Magic! Suppose the machine could correctly guess when the substring x ends and y begins, s.t. $x \in A$ and $y \in B$. Then we add the transitions between the "appropriate" states, and done! The question is: What labels do these transitions take on? Must not affect the behaviour of M1 and M2, but still allow this "magically correct" guess! We more, therefore, to an extended model of computation, a Mondeterninistic finite-state automaton (NFA).



L= {wbl | west, les j over s= {a,b} All strings with bas the penultimate letter. $\begin{array}{c}
 & b \\
 & 0
\end{array}$ $\begin{array}{c}
 & a_1b \\
 & 0
\end{array}$ $(q_0, b, q_0) \in \Delta$ $(90,6,92) \in \Delta$

 $M = (Q, \leq, \delta, q_o, F)$ Q: finite set of states Z: alphabet — S: transition function $S: \mathbb{Q} \times \mathbb{Z} \to \mathbb{Q}$ 90: initial state E Q F: Set of final states CQ Maccepts a word w iff the run of M on w terminates in a final state from f. $M = (Q, \leq v, \leq f, \Delta, Qo, F)$ $= (2, \leq v, \leq f, \Delta, Qo, F)$ 1: transition relation $\Delta \subseteq Q \times Z_{\xi} \times Q$ Wo: Set of initial States CQ

Maccepts a word wiff Mhas at least me run on w which terminates in a state EF.