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Aim:

To Develop a Java Program to implement the Diffie-Hellman Key exchange algorithm. Implement the Miller Rabin Primality checking algorithm to check the primality of the input prime number for. DH key exchange algorithm.

Algorithm:

(1) Diffie-Hellman Key exchange:

- 1.1) consider a prime 'q'.
- 1.2) select 'x' (Primitive root). such that  $(x < q)$   
 $\{x \ \& \ q\}$  is public known quantities.

1.3)

let  $x \rightarrow$  denotes Private.  
 $y \rightarrow$  denotes Public

- $\rightarrow$  now assume  $x_A$  (Private key for user A).  
such that  $x_A < q$
- $\rightarrow$  similarly assume  $x_B$  (Private key for user B).  
such that  $x_B < q$

1.4) now, Public key of A is given by

$$\left. \begin{aligned} y_A &= x^{x_A} \bmod q \\ \& \text{ Public key of B is given by} \\ y_B &= x^{x_B} \bmod q \end{aligned} \right\} \text{ - Public known quantities.}$$

1.5)

now the secret key is

$$(Y_B)^{X_A} \bmod q \quad - \text{for user A} \quad \&$$

$$(Y_A)^{X_B} \bmod q \quad - \text{for user B}$$

$$\text{note: } (Y_B)^{X_A} \bmod q = (Y_A)^{X_B} \bmod q. \quad -$$

Thus. The secret key is generated.

(2) Miller-Rabin Primality checking algorithm.

- Suppose 'n' is the number we want to check

step 1: find integers k, m such that

$$(n-1) = 2^k \cdot m$$

step 2: select a random integer a  
(s.t.)  $1 < a < n-1$

step 3: If  $a^m \bmod n = 1$ , Then return ("~~may be~~ prime")

step 4: for  $j = 0$  to  $k-1$  do.

step 5: if  $a^{2^j m} \bmod n = n-1$ , Then return ("prime")

step 6: Else return composite.

note: ~~The~~ If algorithm returns prime - it's not 100% true, (can also give false positive result)  
but if algorithm returns composite - it's 100% true  
(or) correct

~~no answer~~

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### **AIM:**

Develop a java program to implement the Diffie-Hellman Key exchange algorithm. Implement the Miller Rabin primality checking algorithm to check the primality of the input prime number for DH key exchange algorithm.

### **Code:**

```
import java.math.BigInteger;
import java.util.*;
public class Main {
    public static void main(String[] args) {
        Scanner in = new Scanner(System.in);
        // int P = BigInteger.probablePrime(30, new Random()).intValue();
        // int P = 29;
        System.out.println("enter value of P:");
        int P = in.nextInt();
        int G = primitiveRoot(P);
        System.out.println("P = "+P+" G = "+G);
        BigInteger g = new BigInteger(""+G);
        BigInteger p = new BigInteger(""+P);

        System.out.println("Enter A's secret key ");
        BigInteger xa = new BigInteger(in.next());
        BigInteger ya = g.modPow(xa, p);
        System.out.println("A's public key = " + ya);

        System.out.println("Enter B's secret key ");
        BigInteger xb = new BigInteger(in.next());
        BigInteger yb = g.modPow(xb, p);
        System.out.println("B's public key = " + yb);

        BigInteger A_sh = yb.modPow(xa, p);
        BigInteger B_sh = ya.modPow(xb, p);
    }
}
```

```

        System.out.println("A's shared secret = "+A_sh);
        System.out.println("B's shared secret = "+B_sh);

        in.close();

    }

    public static int primitiveRoot(int p)
    {
        if (!(new BigInteger(""+p).isProbablePrime(1))) return -1;
        // if(!(isPrime(p))) return -1;
        int phi = p-1;
        ArrayList<Integer> fact = primeFactors(phi);
        for (int res=2; res<=p; ++res) {
            Boolean ok = true;
            for (int i=0; i<fact.size() && ok; ++i)
                ok &= powmod (res, phi / fact.get(i), p) != 1;
            if (ok) return res;
        }
        return -1;
    }

    public static ArrayList<Integer> primeFactors(int n)
    {
        ArrayList<Integer> facts = new ArrayList<>();
        for (int i=2; i*i<=n; ++i)
            if (n % i == 0) {
                facts.add(i);
                while (n % i == 0)
                    n /= i;
            }

        return facts;
    }

    public static int powmod(int a,int b,int mod)
    {
        if (b==0)

```

```

        return 1;
    if (b==1)
        return a%mod;
    int temp = powmod(a,b/2,mod);
    temp = (temp*temp);
    if (b%2!=0)
        temp*= a;
    return temp%mod;
}

static boolean millerTest(int d, int n) {
    int a = 2 + (int) (Math.random() % (n - 4));
    int x = powmod(a, d, n);

    if (x == 1 || x == n - 1)
        return true;
    while (d != n - 1) {
        x = (x * x) % n;
        d *= 2;

        if (x == 1)
            return false;
        if (x == n - 1)
            return true;
    }
    return false;
}

static boolean isPrime(int n) {
    if (n <= 1 || n == 4)
        return false;
    if (n == 3)
        return true;
    int d = n - 1;
    int k=n-2;
    while (d % 2 == 0)
    {
        d /= 2;
        // k++;
    }
    for (int i = 0; i < k; i++)

```

```
        if (!millerTest(d, n))  
            return false;  
    }  
    return true;  
}  
}
```

## OUTPUT :

```
➤ javac -classpath ./run_dir/junit-4.12.jar:target/dependency/* -d . Main.java  
➤ java -classpath ./run_dir/junit-4.12.jar:target/dependency/* Main  
enter value of P:  
23  
P = 23 G = 5  
Enter A's secret key  
6  
A's public key = 8  
Enter B's secret key  
15  
B's public key = 19  
A's shared secret = 2  
B's shared secret = 2  
➤ █
```